HOW TO SOLVE IT WITH PROLOG

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ABSTRACT

Our purpose is to present the outstanding features of PROLOG through a collection of small problems and exercises, divided in general application areas such as deductive reasoning over data bases, natural language, symbolic calculus, etc.

KEY WORDS AND PHRASES: PROLOG, Logic Programming,
Problem Solving

SUMÁRIO

O nosso objectivo consiste em apresentar as características proeminentes da linguagem de programação PROLOG, através de uma colectânea de pequenos problemas e exercícios divididos em áreas gerais de aplicação, tais como raciocínio dedutivo sobre bases de dados, língua natural, cálculo simbólico, etc.

PALAVRAS E FRASES CHAVE: PROLOG, Programação em Lógica,
Resolução de Problemas
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CHAPTER 1

INTRODUCTION

Over the past nine years there has been a great deal of research work in logic programming (see Bibliography). A programming language, PROLOG, based on predicate calculus was developed, and several interpreters and two compilers were written for the main computer systems (see Appendix 1). A number of practical working systems have been implemented (see Appendix 2).

Our purpose is to present the outstanding features of PROLOG, and of the logic by the clause approach, through a collection of small problems and exercises, divided in general application areas such as deductive reasoning over data bases, natural language, theorem proving, planning and symbolic calculus. Our aim was motivated by the inexistence of a document to help people become initiated in PROLOG, and to learn it by the example.

The present text is not intended to be a complete and definite collection, although we consider that the major examples, taken from literature and duly referenced, have been included. The respective programs were adapted to the PROLOG
running on the DEC-10 systems. The programs for the problems and exercises not referenced were written by the authors.

All logic programs were written and tested on the DECSYSTEM-10 PROLOG (Warren, 1977; Pereira et al., 1978).

For your convenience we have included a list of PROLOG relevant addresses (Appendix 3), as well as a specification of system predicates (see Appendix 4).
CHAPTER 2

A BRIEF SURVEY OF PROLOG

PROLOG is a simple but powerful programming language founded on symbolic logic, developed at the University of Marseille (Roussel, 1975), as a practical tool for logic programming (Kowalski, 1974; 1979) (Colmerauer, 1975) (Emden, 1975). A major attraction of the language, from a user’s point of view, is ease of programming. Clear, readable, concise programs can be written quickly with minimum error. Recently, an efficient compiler and an interpreter were implemented on the DECSYSTEM-10 (Warren, 1977a; 1979). A user’s guide is available (Pereira et al., 1978).

Like LISP, PROLOG is an interactive language designed primarily for symbolic data processing. Both are founded on formal mathematical systems — LISP, on the lambda calculus, is typically used for the definition of functions, PROLOG, on a powerful subset of classical logic (Tarnlund, 1977), is typically used for the definition of relations. Pure LISP in fact can be viewed as a specialization of PROLOG (Warren et al., 1977).
2.1 SYNTAX

Here is a PROLOG program, consisting of two clauses, for specifying the concatenation relation of two lists:

\[
\text{concatenate([],L,L)}. \\
\text{concatenate([X|L1],[L2,[X|L3]]):- concatenate(L1,L2,L3).}
\]

In general, a PROLOG program consists of a set of procedures, where each procedure comprises a number of clauses. The procedure name is called a predicate ('concatenate' above), and has an arity which is the number of its arguments (3 above). A clause begins with a head or procedure entry point, and continues with a body. If the body is not empty it is separated from the head by ':-' (2nd clause above). Every clause terminates with a '.'. The head displays a possible form of the arguments to the procedure's predicate. The body consists of a number (possibly zero) of goals or procedure calls, which impose conditions for the head to be true. If the body is empty we speak of a unit clause (1st clause above).

In general, all PROLOG objects are terms. A clause is a term, a predicate or a goal with their respective arguments, and the arguments themselves are terms. For example, a tree of 5 categories of a classification system is represented by the following term,

\[
\text{t(t(void,linguistics,void),} \\
\text{ 'computing sciences',} \\
\text{ t(t(void,ai,void),applications,t(void,software,void)))}
\]
A term is either a variable (distinguished by an initial capital letter), an atom ("void" above), or a compound term. A compound term comprises a functor ("concatenate" or "t" above) of some arity \( N \geq 1 \), and a sequence of \( N \) terms as its arguments ("t(void,ai,void)" above). An atom is treated as a functor of arity 0. A term of the form \([H:T]\) stands for the list \((H,T)\), whose head is \( H \) and tail is \( T \). The empty list is denoted \([\ ]\), and a list with exactly two elements by \([A,B]\).

The second clause above is just infix notation for the term

\[
;(concatenate([X;L1],L2,[X;L3]),
    concatenate(L1,L2,L3))
\]

where "\( ; \)" is a binary functor. The functor "\( ; \)" takes as arguments the head and the body of the clause. If a body has more than one goal the comma separating the goals is just another binary functor used in infix notation. The above term stands for a clause because it figures in the set of clauses for a procedure. It is distinguished by a final ";".

Apart from syntax conventions, the names and arities of terms (and their number) are arbitrary, except for a pre-defined set of procedures which are built into the implementation of the language, and which achieve input, output, arithmetic, etc (a listing of system procedures will be found in Appendix 4).
2.2 SEMANTICS

PROLOG differs from most programming languages in that there are two quite distinct ways to understand its semantics. The procedural or operational semantics is the more conventional, and describes as usual the sequence of states passed through when executing a program. In addition a PROLOG program can be understood as a set of descriptive statements (one for each clause) about a problem. The declarative or denotational semantics, which PROLOG inherits from logic, provides a formal basis for such an understanding. Informally, one interprets terms as shorthand for natural language phrases by applying a uniform translation of each functor, e.g.,

\begin{align*}
\text{void} &= \text{"the empty tree"} \\
\text{t}(L,N,R) &= \text{"the binary tree with root } N, \text{ left subtree } L \text{ and right subtree } R\text{"}
\end{align*}

A clause \( E \leftarrow Q,R,S \) where \( E,Q,R \) and \( S \) are metavariables standing for terms, is interpreted as

\begin{quote}
\text{"E if } Q \text{ and } R \text{ and } S\text{"}
\end{quote}

A clause \( E \) is interpreted as \( E \text{ is true} \).
Each variable in a clause should be interpreted as some arbitrary object (i.e., variables are universally quantified). The type of the object conveyed by a variable will be appropriate to the functor(s) where the variable figures by using terms in a consistent way throughout the program.

The declarative semantics simply defines (recursively) the set of terms which are asserted to be true according to a program. A term is true if it is the head of some clause instance and each of the goals (if any) of that clause instance is true, where an instance of a clause (or term) is obtained by substituting, for each of zero or more of its variables, some term for all occurrences of the variable.

Thus the only instance of the goal:

\[
\text{concatenate([a],[b],[L]),}
\]

is

\[
\text{concatenate([a],[b],[a,b]).}
\]

It is the declarative aspect of PROLOG which is responsible for promoting clear, rapid, accurate programming. It allows a program to be broken down into small, independently meaningful units (clauses), and it allows some understanding of a program without looking into the details of how it is executed.
2.3 PROCEDURAL SEMANTICS

It is the procedural semantics that describes the way a goal is executed. The objective of execution is to produce true instances of the goal. It then becomes important to know that the ordering of clauses in a program, and of goals within a clause, which are irrelevant as far as the declarative semantics is concerned, constitute crucial control information for the procedural semantics.

To execute a goal, the system searches for the first clause whose head matches or unifies with the goal. The unification process (Robinson, 1965) finds the most general common instance of the two terms, which is unique if it exists. If a match is found, the matching clause instance is then activated by executing in turn, from left to right, each of the goals of its body (if any). If at any time the system fails to find a match for a goal it backtracks, i.e., it rejects the most recently activated clause, undoing any substitutions made by the match with the head of the clause. Next it reconsiders the original goal which activated the rejected clause, and tries to find a subsequent clause which also matches the goal. Execution terminates if no goals remain to be executed (the system has then found a true instance of the original goal). Backtracking may then be invoked to find other true instances of the goal. Execution fails when no true instances of the original goal are found, and terminates if it cannot find any more true instances. Termination however cannot be guaranteed, even if there are no
more true instances (e.g., if there are infinite branches).

Note that the execution just defined is a left to right depth-first process. Note also that because unification always provides the most general common instance between a goal and a matching clause, all the most general true instances of a goal can potentially be found (i.e., apart from termination issues).

Basically, each execution step is justified by Robinson's Resolution Principle (Robinson, 1965). This principle subsumes in a single inference rule the classical rules of "modus ponens" and "generalization" in formulations of first order predicate calculus. For example, from

\[ p(X) :\neg a(a,X), r(X). \]

and

\[ \alpha(Y,f(Y,Z)) :\neg s(a,Z). \]

it allows to conclude

\[ p(f(a,Z)) :\neg s(a,Z), r(f(a,Z)). \]

by "execution" of \( \alpha(a,X) \).

Besides the ordering of clauses and the sequencing of goals within clauses PROLOG provides just one other essential mechanism for specifying control information. This is the "cut" symbol, written "!". It is inserted in a program just like a goal, but it is not to be regarded as part of the logic of the program and should be ignored as far as the declarative semantics is concerned.
The effect of the 'cut' is as follows: when first encountered, as a goal, 'cut' succeeds immediately. If backtracking should later return to the 'cut', the effect is to fail the goal which caused the clause containing the 'cut' to be activated. In other words, the 'cut' operation commits the system to all choices made since execution of the goal activating the clause begun, i.e. other alternatives for that goal are not considered, as well as for all goals occurring in the matching clause before the 'cut'. By means of a 'cut' one can ensure that some goals, once partly executed by a clause up to a 'cut', either must continue that partial execution or fail. The 'cut' renders deterministic the whole partial execution made by the activated clause up to it.

Example of the effect of a 'cut' in the flow of control, when goal F fails,

where A, B, C, D, E, F, and P are metavariables standing for predicate instances.

If F fails, backtracking returns to goal A immediately before B, the goal that activated the clause with the 'cut'.

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2.4 OUTSTANDING FEATURES OF PROLOG

Let us briefly review the combination of features which make PROLOG a powerful but simple to use programming language.

(1) A declarative semantics inherited from logic in addition to the usual procedural semantics.

(2) Identity of form of program and data - clauses can be employed for expressing data, and can be manipulated as terms by interpreters written in Prolog.

(3) The input and output arguments of a procedure do not have to be distinguished in advance, but may vary from one call to another. Procedures can be multi-purpose.

(4) Procedures may have multiple outputs as well as multiple inputs.

(5) Procedures may generate, through backtracking, a sequence of alternative results. This amounts to a high level form of iteration.

(6) Terms provide general record structures with any number of fields. An unlimited number of record types may be used, and there are no type restrictions on the fields of a record.

(7) Pattern matching replaces the use of selector and constructor functions for operating on structured data.

(8) Incomplete data structures may be returned (i.e., structures containing free variables) which may later be filled in by other procedures.

(9) Prolog dispenses with do to, do for and while loops, assignment, and references (pointers).

(10) The procedural semantics of a syntactically correct program is totally defined. It is impossible for an error condition to arise or for an undefined operation to be performed. This totally defined semantics ensures that programming errors do not result in bizarre program behaviour or incomprehensible error messages.

(11) No part of the program is concerned with the details of the underlying machine or implementation.
3.1 UTILITIES (nos. 1 to 41)

PROBLEM 1

Verbal statement:
Check whether H is a member of a list L; search all members of a list L.

Logic program:
member(H,[H|_]),
member(I,[L|T]):- member(I,T).

PROBLEM 2

Verbal statement:
Check whether H is a member of a list L; search the first member of a list L. Consider L as [a,b,c].

Logic program:
member(H,[E|H1|L]):- !,
member(I,[L|T]):- member(I,T).

Execution:
The only result produced by executing:

?-member(X,[a,b,c]).

is X=a. The other two potential solutions are discarded on account of the cut symbol.
**PROBLEM 3**

Verbal statement:

Check whether \( U \) is the intersection of lists \( L_1 \) and \( L_2 \); search the intersection of lists \( L_1 \) and \( L_2 \).

Logic program:

\[
\begin{align*}
\text{intersect}([H;T],L,[H;U]) & : \text{member}(H,L), \text{intersect}(T,L,U), \\
\text{intersect}([_;T],L,U) & : \text{intersect}(T,L,U), \\
\text{intersect}([_;[]]) & : \\
\text{member}(H,[H;_]), \\
\text{member}(I,[_;T]) & : \text{member}(I,T).
\end{align*}
\]

**PROBLEM 4**

Verbal statement:

Write the 'Pickup the first n members of a list' relation.

Logic program:

\[
\begin{align*}
\text{set_till_n}([],[],_,_), \\
\text{set_till_n}([X;L],[X;P],C,N) & : (\text{var}(C), C=1 \# \text{true}), \\
& \text{C}\lt N, C \text{ is } C+1, \\
& \text{set_till_n}(L,P,C1,N), \\
\text{set_till_n}([_;[]],_,_) & : \\
\end{align*}
\]

**PROBLEM 5**

Verbal statement:

Write the set equality relation.

Logic program:

\[
\begin{align*}
\text{set_equal}(X,X) & : !, \\
\text{set_equal}(X,Y) & : \text{equal_lists}(X,Y), \\
\text{equal_lists}([],[]), \\
\text{equal_lists}([X;L1],[Y;L2]) & : \text{delete}(X,L2,L3), \\
& \text{equal_lists}(L1,L3), \\
\text{delete}(X,[X;Y],Y), \\
\text{delete}(X,[Y;L1],[Y;L2]) & : \text{delete}(X,L1,L2).
\end{align*}
\]

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PROBLEM 6

Verbal statement:

Write the subtraction relation of two lists.

Logic Program:

\[
\begin{align*}
\text{subtract}(L,[],L) & : - !, \\
\text{subtract}([H:T],L,U) & : - \text{member}(H,L), U, \text{subtract}(T,L,U). \\
\text{subtract}([H:T],L,[H:U]) & : - !, \text{subtract}(T,L,U). \\
\text{subtract}([],U,[]) & . \\
\text{member}(H,[H:]). \\
\text{member}(I,[I:T]) & : - \text{member}(I,T).
\end{align*}
\]

PROBLEM 7

Verbal statement:

Specify the relation \textit{append} (list concatenation) between three lists which holds if the last one is the result of appending the first two. Consider the last list as \([a,b]\).

Logic Program:

\[
\begin{align*}
\text{append}(L,L,L). \\
\text{append}([H:T],L,[H:U]) & : - \text{append}(T,L,U).
\end{align*}
\]

Execution:

For the example proposed, if we execute the goal expressed by the question:

\[
?-\text{append}(X,Y,[a,b]).
\]

the first solution is: \(Y=[a,b]\) and \(X=[]\)

If this solution is rejected by the user, backtracking will generate the further solutions:

\[
\begin{align*}
X=[a] & \\
Y=[] & \\
X=[a,b]
\end{align*}
\]

PROBLEM 8

Verbal statement:

Check whether \(T\) is a sublist of \(U\); search all incompletely specified sublists (patterns).
Logic program:

\[
\text{sublist}(T, U) :- \text{append}(H, T, V), \text{append}(V, W, U).
\]
\[
\text{append}([], L, L).
\]
\[
\text{append}([H:T], L, [H;U]) :- \text{append}(T, L, U).
\]

PROBLEM 9  [MELONI, 1976]

Verbal statement:

This problem is a sophisticated application of list concatenation. It is pretended to build, on basis of a list of French words (for instance, animal names), a list of new words, each one obtained from the ancestors by juxtaposition of the words whose final characters are the first ones of another. For example the words VACHE (cow) and CHEVAL (horse) give the word VACHEVAL (mutation problem).

Logic program

\[\begin{align*}
\text{begin} :- & \quad \text{mutation}(X), \text{name}(Nn,X), \text{write}(Nn), n1, \text{fail}. \\
\text{begin} :- & \quad n1, \text{write}(\text{'Done.'}), n1.
\end{align*}\]
\[
\text{mutation}(X) :- \quad \text{animal}(Y), \text{name}(Y,Ny), \text{animal}(Z), \text{name}(Z,Nz),
\]
\[
\text{append}(Y1,Y2,Ny), Y1=[], \text{append}(Y2,Z2,Nz),
\]
\[
Y2=[], \text{append}(Y1,Nz,X),
\]
\[
\text{append}([], X, X),
\text{append}([A;X], Y, [A;Z]) :- \text{append}(X, Y, Z).
\]

animal(alligator), /* crocodile */
animal(tortue),    /* turtle */
animal(caribou),   /* caribou */
animal(ours),      /* bear */
animal(cheval),    /* horse */
animal(vache),     /* cow */
animal(lapin),     /* rabbit */

Execution:

\[\begin{align*}
& \text{:- begin} \\\
& \text{alligator}
\text{tortue}
\text{caribous}
\text{cheval}
\text{vache}
\text{lapin}
\text{Done}.
\end{align*}\]

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PROBLEM 10

Verbal statement:

Check whether L1 is the reverse of list L; search the reverse of list L.

Logic programs:

/* Program 1 */
reverse([],[]).
reverse([H|T],L):- reverse(T,R),append(R,[H],L).

append([],L,L).
append([H|T],L,[H|U]):- append(T,L,U).

/* Program 2 */
reverse2(L1,L):- reverse_append(L1,[],L).
reverse_append([H|T],L,M):- reverse_append(T,[H|L],M), reverse_append([],L,M).

PROBLEM 11

Verbal statement:

Write a program where the main operations on sets are defined.

Logic program:

/* member of a set */
member(X,[X|_]).
member(X,[_|L]):- member(X,L).

/* subset */
subset([A|X],Y):- member(A,Y),subset(X,Y).
subset([],Y).

/* disjoint */
disjoint(X,Y):- member(Z,X),not(member(Z,Y)).

/* intersection */
intersection([],X,[]).
intersection([X|R],Y,[X|Z]):- member(X,Y),!,
                          intersection(R,Y,Z).
intersection([X:R],Y,Z):- intersection(R,Y,Z).

/* union */

union([],X,X).
union([X:R],Y,Z):- member(X,Y),!;union(R,Y,Z).
union([X:R],Y,[X:Z]):- union(R,Y,Z).

**Problem 12  [EMDEN, personal communication]**

Verbal statement:

Split a list with head H and tail [H1:T1] into two lists U1 and U2, where all the elements of U1 are =< H, all the elements of U2 are >H, and the original order is preserved.

Logic program:

`split(H,[H1:T1],[H1:U1],U2):- H1=<H,split(H,T1,U1,U2).`  
`split(H,[H1:T1],U1,[H1:U2]):- H1>=H,split(H,T1,U1,U2).`  
`split([],[],[]).`

**Problem 13  [EMDEN, personal communication]**

Verbal statement:

Define a quicksort relation using append.

Logic program:

`sort([H:T],S):- split(H,T,U1,U2),`  
`sort(U1,V1),`  
`sort(U2,V2),`  
`append(V1,[H1:V2],S).`  

`sort([],[]).`  

`append([],L,L).`  
`append([H:T],L,[H:U]):- append(T,L,U).`

Execution:

```
```

10
PROBLEM 14  [EMDEN, personal communication]

Verbal statement:

Define the quicksort relation without append (make \( X = [] \) in the input).

Logic program:

\[
\text{sort2}([H;T], S, X) \leftarrow \text{split}(H, T, U1, U2), \\
\quad \text{sort2}(U1, S, [H;Y]), \\
\quad \text{sort2}(U2, Y, X).
\]

\[
\text{sort2}([], X, X).
\]

\[
\text{split}(H, [H1;T1], [H1;U1], U2) \leftarrow H1 < H, \text{split}(H, T1, U1, U2).
\]

\[
\text{split}(H, [H1;T1], U1, [H1;U2]) \leftarrow H1 > H, \text{split}(H, T1, U1, U2), \\
\text{split}([], [], [], []). 
\]

PROBLEM 15  [EMDEN, personal communication]

Verbal statement:

Define the bubble sort relation.

Logic program:

\[
\text{sort3}(L, S) \leftarrow \text{append}(U, [A;B;V], L), \\
\quad B < A, \\
\quad \text{append}(U, [B;A;V], M), \\
\quad \text{sort3}(M, S). \\
\quad \text{sort3}(L, L).
\]

\[
\text{append}([], L, L).
\]

\[
\text{append}([H;T], L, [H;V]) \leftarrow \text{append}(T, L, U),
\]

PROBLEM 16  [EMDEN, personal communication]

Verbal statement:

Write a program to be compiled which defines the quicksort relation.

Apply your program to the list of 50 elements: 27, 74, 17, 33, 94, 18, 46, 83, 65, 2, 32, 53, 28, 85, 99, 47, 28, 82, 6, 11, 55, 29, 39, 81, 90, 37, 10, 0, 66, 51, 7, 21, 85, 27, 31, 63, 75, 4, 95, 99, 11, 28, 61, 74, 18, 92, 40, 53, 59, 8.
Logic program:

:- mode asort(+, +, +).
:- mode partition(+, +, +, +, +).

\text{asort}([X;L], R, R0) :- \text{partition}(L, X;L1, L2),
                        \text{asort}(L2, R1, R0),
                        \text{asort}(L1, R, [X;R1]).

\text{asort}([], R, R).

\text{partition}([X;L], Y, [X;L1], [X;L2]) :- X =\text{<} Y, \text{!}, \text{partition}(L, Y, L1, L2).
\text{partition}([X;L], Y, L1, [X;L2]) :- \text{partition}(L, Y, L1, L2).
\text{partition}([], [], []).

\text{list}_{-50}(27, 74, 17, 33, 94, 18, 46, 83, 65, 2,
            32, 53, 28, 85, 99, 47, 28, 82, 6, 11,
            55, 29, 39, 81, 90, 37, 10, 0, 66, 51,
            7, 21, 85, 27, 31, 63, 75, 4, 95, 99,
            11, 28, 61, 74, 18, 92, 40, 53, 59, 81).

Execution:

:- \text{list}_{-50}(L), \text{asort}(L, X, []).

\text{Problem 17} \quad \text{[EMDEN, Personal communication]}

Verbal statement:

Define the insert sort relation.

Logic program:

\text{sort}4([H;T], S) :- \text{sort}4(T, L), \text{insert}(H, L, S),
                       \text{sort}4([], []).

\text{insert}(X, [H;T], [H;L]) :- H =\text{<} X, \text{!}, \text{insert}(X, T, L),
                        \text{insert}(X, L, [X;L]).

\text{Problem 18}

Verbal statement:

Write a program for sorting a list as an ordered permutation of that list.

Logic program:

\text{sort}(L, S) :- \text{permute}(L, S), \text{ordered}(S),
                    \text{permute}([], []).
\texttt{permute(L,[H;S]):- delete(H,L,N2), \texttt{permute(NL,S)}.}

\texttt{delete(H,[H;L],L).}
\texttt{delete(X,[H;L],[H;NL]):- delete(X,L,NL).}

\texttt{ordered([]).}
\texttt{ordere([X]).}
\texttt{ordered([X,Y;Z]):- X \leq Y, \texttt{ordered([Y;Z]).}}

**PROBLEM 19 [EMDEN, personal communication]**

**Verbal statement:**

Define combinations of a list, where \( s(K) \) indicates the successor of \( K \). For example, 3 is written \( s(s(s(0))) \).

**Logic program:**

\texttt{combinations(s(K),[H;T],[H;U]):- combinations(K,T,U).}
\texttt{combinations(s(K),[L;T],U):- combinations(s(K),T,U).}
\texttt{combinations(0_,_,[]).}

**PROBLEM 20 [EMDEN, personal communication]**

**Verbal statement:**

Define permutations of a list.

**Logic program:**

\texttt{permutations(L,[H;T]):- append(V,[H;U],L),}
\texttt{append(V,U,W),}
\texttt{permute(W,T).}
\texttt{permutations([],[]).}
\texttt{append([],L,L).}
\texttt{append([H;T],L,[H;U]):- append(T,L,U).}

**PROBLEM 21**

**Verbal statement:**

Check whether a word is a palindrome, i.e., the same if read backwards, as for example "MADAM". Write a program able to check a palindrome for each word you give.
Logic program:

```
begin(X):- read(X), (X=stop ; test_palindrome(X), begin(Y)).
test_palindrome(X):- name(X,Nx), palindrome(Nn), write(X),
                  write(' is a palindrome'), nl !.
test_palindrome(X):- write(X),
                  write(' is not a palindrome'), nl.
palindrome(X):- reverse2(X,X).
reverse2(L1,L):- reverse_append(L1, [], L).
reverse_append([H|T], L, M):- reverse_append(T, [H|L], M),
        reverse_append([], L, L).
```

Execution:

*:-begin(X),
madam, john, astyuytsa, horse, bull, stop.
madam is a palindrome
john is not a palindrome
astyuytsa is a palindrome
horse is not a palindrome
bull is not a palindrome

PROBLEM 22

Verbal statement:

Given two lists, where the second one is the concatenation of a third one with the first one, find this third list and build up a palindrome with it.

Logic program:

```
palindrome(L1, L2):- list(L1, Y), list(L2, Z),
                  concatenate(X, Y, Z),
                  write('Third list: '), write(X), nl,
                  reverse(X, W),
                  concatenate(X, W, K),
                  write('Palindrome: '), write(K).

concatenate([], L, L),
concatenate([E|R], L2, [E|L]),
reverse([], [], L),
reverse([E|R], L):- reverse(R, R1),
                concatenate(R1, [E], L).
```
list(a,[1,3,5,7,9]).
list(b,[a,b,c,d,e,1,3,5,7,9]).

Execution:
The execution of :- palindrome(a,b).
saves us the following result:
Third list: [a,b,c,d,e]
Palindrome: [a,b,c,d,e,e,d,c,b,a]

PROBLEM 23  [KOWALSKI, 1974b]

Verbal statement:
Write a program for implementing the relation 'admissible' between two lists a and b,

\[ b_i = 2a_i \quad \text{and} \quad a_{i+1} = 3b_i \quad \text{for} \quad i < n \]

where \( a_i \) and \( b_i \) are the elements number \( i \) of lists \( a \) and \( b \) respectively.

Logic programs:
/* Program 1 */
admissible(X,Y):- double(X,Y), triple(X,Y).

double([],[]).
double([X,Y],[U:V]):- U is 2*X, double(Y,V),

triple([X],[U]),
triple([X,Y,Z],[U:V]):- Y is 3*U, triple([Y,Z],V),

/* Program 2 */
admissible([],[]),
admissible([X,Y,Z],[U:V]):- U is 2*X, Y is 3*U,
admissible([Y,Z],V),
admissible([X],[U]):- U is 2*X.

Execution:
The execution of
?- admissible([1:U],V), write([1:U]), write(’,’), write(V), fail.
saves us the following list pairs:
PROBLEM 24

Verbal statement:
Write a program to simplify a list whose members are lists, and to transform it into a list of single members. Note that each member is a node of a tree and that simplification means to extract all redundancies, even those brought up by domination of a node over several nodes. In this case, the dominant node is redundant.

Logic program:

simplify(L, NL) :- compact(L, L1), simplify1(L1, L2),
                 simplify2(L2, NL).

compact([L, []], L).
compact([L], L).
compact([L1, [L2]], L) :- concatenate(L1, L2, L).
compact(L1, L2, [L3], L) :- concatenate(L1, L2, X),
                           compact([X, L3], L).

concatenate([X; L1], L2, [X; L3]) :- concatenate(L1, L2, L3).
concatenate([], L, L).

simplify1([X; L], NL) :- member(X, L), !, simplify1(L, NL).
simplify1([X; L], [X; NL]) :- simplify1(L, NL).
simplify1([], L, L).

simplify2(L, NL) :- simplify3(L, L1), subtract(L, L1, NL).

simplify3([X; L], NL) :- compare(L, X, []), simplify3(L, NL).
simplify3([X; L], [Y; NL]) :- compare(L, X, Y), simplify3(L, NL).
simplify3([], [], []).

compare(_, _, _) :- !.
compare([Y; L], X, [Z; NL]) :- (linked(X, Y), Z=X ; linked(Y, X), Z=Y),
                               compare(L, X, NL).
compare([Y; L], X, NL) :- compare(L, X, NL).
compare([], _, []).  

subtract(L, [], L) :- !.
subtract([H; T], L, U) :- member(H, L), !, subtract(T, L, U).
subtract([H; T], [L; U], [H; U]) :- !, subtract(T, L, U).
subtract([], _, []).
member(A,[A|_]),
member(A,[_|L]):- member(A,L).

PROBLEM 25  [TÄRNLUND, 1976b]
Verbal statement:
Define a procedure for manipulating stacks. Consider a stack such as:

\[ \text{a} \rightarrow \text{b} \rightarrow \text{c} \]

Write the goal statements for deleting an element from the stack, and for inserting a new element e.

Logic program:
\[ \text{stack}(s(X,Y),X,Y). \]

Execution:
This program pops-up a stack.
The goal statement for deleting is:
\[ :-\text{stack}(s(a,s(b,s(c,0))),X,Y). \]
The result is \( X=a \) and \( Y=s(b,s(c,0)) \)
The goal statement for inserting is:
\[ :-\text{stack}(Z,e,s(a,s(b,s(c,0)))). \]
The result is: \( Z=s(e,s(a,s(b,s(c,0)))) \)
The goal statement for inserting is obtained by dual programming, and it is achieved by shifting the roles between input and output variables in a goal statement.

PROBLEM 26  [TÄRNLUND, 1976b]
Verbal statement:
Define a procedure for manipulating queues.

Consider the following queue:

\[ \text{head} \rightarrow \text{a} \rightarrow \text{b} \rightarrow \text{c} \rightarrow \text{rear} \]

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Write the goal statements for deleting the head element of a queue, for inserting an element in the rear of a queue, and for inserting a new element into the queue.

Logic program:

\[ \text{delete}(a(X,Y), X, Y). \]
\[ \text{insert}(Y, a(W,X1), W, Y). \]
\[ \text{insert}(Y, a(W,X1), W, X1, Y). \]

Execution:

The goal statement for deleting the first element of queue \(a(a(a(b,a(c,X))))\) is:

\[ \leftarrow \text{delete}(a(a(a(b,a(c,Z)))), X, Y). \]

The result is: \(Y = a(b,a(c,Z))\)

The goal statement for inserting an element d in the rear of the queue is:

\[ \leftarrow \text{insert}(a(a(a(b,a(c,X)))), X, d, Z). \]

The result is: \(Z = a(a(a(b,a(c,a(d,X1))))))\)

The goal statement for inserting a new element into the queue is:

\[ \leftarrow \text{insert}(a(a(a(b,a(c,X)))), X, d, X1, Z). \]

PROBLEM 27  [TÄRNLUUND, 1976b]

Verbal statement:

A fundamental data base operation is to search for a record \(R_i\) (node) in a tree given a key \(K_i\), and insert it as a new record if the record is not in the tree. Define an algorithm for binary tree search.

Logic program:

\[ \text{binary}(t(X,K,Z), K, t(X,K,Z)). \]
\[ \text{binary}(t(X,Y,Z), K, t(X1,Y,Z)): \leftarrow \text{name}(K,NK), \text{name}(Y,NY), NK < NY, \]
\[ \quad \text{binary}(X,K,X1). \]
\[ \text{binary}(t(X,Y,Z), K, t(X,Y,Z1)): \leftarrow \text{name}(K,NK), \text{name}(Y,NY), NK > NY, \]
\[ \quad \text{binary}(Z,K,Z1). \]
\[ \text{binary}(\text{void}, K, t(\text{void}, K, \text{void})). \]
PROBLEM 28  [TÄRLUND, 1976b]

Verbal statement:

Suppose we have the following binary tree:

```
  e
 / \
c   n
```

Construct an algorithm able to search for a key m, and able to insert it if it is not in the tree.

Execution:

the goal statement,

```prolog
:-binary(t(t(void,c,void),e,t(void,n,void)),m,Z).
```

consists in the call of the previous program. The result is a new tree Z,

```
t(t(void,c,void),e,t(t(void,m,void),n,void))
```

PROBLEM 29  [TÄRLUND, 1976b]

Verbal statement:

A frequent data base operation is to delete a node in a tree. Define an algorithm for binary tree deletion.

Logic program:

```
delete(t(X,K,void),K,X).
delete(t(X,K,t(void,Y1,Z1)),K,t(X,Y1,Z1)).
delete(t(X,K,t(X1,Y1,Z1)),K,t(X,Y,t(X2,Y1,Z1))):-
  successor(X1,Y,X2).
delete(t(X,Y,Z),K,t(X1,Y,Z)):- K<Y,delete(X,K,X1).
delete(t(X,Y,Z),K,t(X,Y,Z1)):- K>Y,delete(Z,K,Z1).
delete(void,K,void).

successor(t(void,Y,Z),Y,Z).
successor(t(X,Y,Z),Y1,t(X1,Y,Z)):- successor(X,Y1,X1).
```

PROBLEM 30  [TÄRLUND, 1976b]

Verbal statement:

Consider the tree,
and delete node m.

Execution:

the goal statement,

\[-\text{binary}(Z, m, t(t(\text{void}, c, \text{void}), \text{est}(t(\text{void}, m, \text{void}), n, \text{void}))), \]

consists in the call of the previous program ‘binary’. However, the dual programming technique, shift the role of the input and output arguments in the goal statement, does not give a complete solution to the deletion problem, as the program ‘delete’.

**Problem 31** [TÄRNKLUND, 1976b]

Verbal statement:

Write an algorithm for inserting a new node at its right position in a three-dimensional tree:

\[ t(X, r(U, U1, U2), Z) \]

where X and Z are left and right subtrees respectively and \( r(U, U1, U2) \) is a root having the attributes U, U1, and U2.

Logic program:

\[
\begin{align*}
\text{insert}(t(X, r(U, U1, U2), Z), K, K1, K2, t(X1, r(U, U1, U2), Z)) :- \\
& \quad K < U, \text{insert}(X, K1, K2, K, X1), \\
\text{insert}(t(X, r(U, U1, U2), Z), K, K1, K2, t(X, r(U, U1, U2), Z1)) :- \\
& \quad K > U, \text{insert}(Z, K1, K2, K, Z1), \\
\text{insert}(\text{void}, K, K1, K2, t(\text{void}, r(K, K1, K2), \text{void})), \\
\text{insert}(t(X, r(K, K1, K2), Z), K, K1, K2, t(X, r(K, K1, K2), Z)).
\end{align*}
\]

**Problem 32**

Verbal statement:

Get all nodes of a tree above and below a specified node.

Logic program:

\[
\begin{align*}
\text{set_node}(X, [M:R], \text{above}) :- & \quad \text{node}(M, X), \text{set_node}(M, R, \_), \\
\text{set_node}(\_, [\_], \text{above}).
\end{align*}
\]

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set_node(X,L,below) :- (down_nodes(X); recorded(c(L),P), erase(P)).

down_nodes(X) :- record(c([])), node(X,M), replace(c(L), c([M:L])), fail.

replace(X,Y) :- recorded(X,P), !, erase(P), record(Y).
replace(_, Y) :- record(Y).

PROBLEM 33

Verbal statement:
Verify if two nodes of a tree are connected.

Logic program:

set_branched(X,Y) :- connected(X,Y); connected(Y,X).

connected(X,Y) :- node(X,Y).
connected(X,Z) :- node(X,Y), connected(Y,Z).

PROBLEM 34

Verbal statement:

Write a term for representing the following structured data object:

```
  line
   /     /
  Point  Point
     /     /
    X1    Z
    /     /
   Y1    X2
   /     /
  Z     Y2
```

Logic program:

line(point(X1,Y1,Z), point(X2,Y2,Z)).

PROBLEM 35  [WARREN,1977b]

Verbal statement:

Write a term 'dictionary' for representing an alphabetically ordered dictionary pairing English words with French equivalents.

Consider the following example:
Write also procedures for:

- 'look up' a name in a dictionary and find it paired value
- 'look up' a name which is before a certain name
- 'look up' a name which is after a certain name

and take into account that those procedures may also serve for constructing the dictionary.

Logic program:

dictionary(void),
dictionary(dic(X,Y,D1,D2)):- dictionary(D1),
dictionary(D2).

dic(salt,sel,
dic(mustard,moutarde,
   void,
dic(pepper,poire,voive,voive)),
dic(vinage,vin agriculture,voive,voive)).

lookup(Name,dic(Name,Value,_,_),Value):- !.
lookup(Name,dic(Name1,_,Before,_,),Value):- Name<Name1,
   lookup(Name,Before,Value).

lookup(Name,dic(Name1,_,_,After),Value):- Name>Nome1,
   lookup(Name,After,Value).

Execution:

:-lookup(salt,D,X1).

is interpreted as: construct a dictionary D such that 'salt' is paired with X1.

The execution gives:

D=dic(salt,X1,D1,D2)

:-lookup(mustard,D,X2).

gives as result:

D=dic(salt,X1,dic(mustard,X,D,D4),D2),
In this way 'lookup' is inserting new entries in a partially specified dictionary.

After executing:

:-lookup(vinegar,D,X3), lookup(pepper,D,X4), lookup(salt,D,X5).

D is instantiated to a dictionary which may be pictured as:

```
salt:X1
  
mustard:X2
     D3
  pepper:X4
     D7
  vinegar:X3
     D5
  pepper:X4
     D8
```

PROBLEM 36

Verbal statement:

Suppose you have an universe of eight animals

\[ U = \{a1, a2, r1, b1, b2, h1, o1, o2\} \]

classified in the following way:

\[
\begin{align*}
\text{aquatics: a1, a2} \\
\text{animals} & \quad \text{reptiles: r1} \\
\text{terrestrials} & \quad \text{birds: b1, b2} \\
\text{mammals} & \quad \text{herbivores: h1} \\
\text{omnivores: o1, o2}
\end{align*}
\]

Write a data structure representing this classification, and build up a program for answering the following questions:

1) What is the classification of animal \( X \) ?
2) What animals have the classification $Y$?

Logic program:

```
classification(A,C) :- animal(C,L), member(A,L).
animal(animal(V),X) :- aquatic(V,X) ; terrestrial(V,X).
aquatic(aquatic,[a1,a2]).
terrestrial(terrestrial(V),X) :- reptile(V,X) ; bird(V,X) ; mammal(V,X).
reptile(reptile,[r1]).
bird(bird,[b1,b2]).
mammal(mammal(V),X) :- herbivore(V,X) ; omnivore(V,X).
herbivore(herbivore,[h1]).
omnivore(omnivore,[o1,o2]).
```

Remark: The predicate "member(X,Y)" is defined as in PROBLEM 1, and it tests if X is a member of list Y.

The question "1) What is the classification of animal X?" where X is instantiated, corresponds to the command ":-classification(X,C).". The other question "2) What animals have the classification Y?", where Y is instantiated, corresponds to the command ":-animal(Y,X).".

Execution:

The execution is top-down, as represented on the tree:

```
animal
  aquatic [a1,a2]
  terrestrial
    reptile [r1]
    bird [b1,b2]
    mammal
      herbivore [h1]
      omnivore [o1,o2]
```

Remark: This problem was suggested by [Dahl, 1977b].
PROBLEM 37  [MELONI, 1976]

Verbal statement:

Write a program able to sort a list of words by alphabetic order.

The list of words obeys the syntax: word1, word2, ... , wordn, stop, , where 'stop' means that there are no more words to sort.

Suggestion: Imagine a tree having each node as a function of 3 arguments nd(L, W, R), where L represents the left descendent of the node, R, its right descendent and W, the word just read. The input word is read and compared to the word associated to the node, beginning by the root, and afterwards compared recursively to its left or right descendant. The whole process finishes when the descendent is a free variable or when the word already exists in the tree. In the first case, a new node representing the word is created, in the place of the variable.

Example: The list John, Mary, James, Edward, stop, will generate the tree:

```
                     nd
                    /   \
                   nd    nd
                  /     |
                 John  Z
                /   |
               nd   nd
              /     |
             James Mary
            /     |   |
           X    edward   Y
```

Logic program:

order(X) :- reading(W), name(W, W1), classify(W1, X, Y), order(Y).
order(X) :- nl, write('ordered words:
', nl, write_tree(X), nl, nl, write('Done.'), nl.

reading(W) :- read(W), (W = stop, !, fail; true).

classify(W, nd(L, W, R), nd(L, W, R)) :- !.
classify(W, nd(L, W1, R), nd(U, W1, R)) :- lower(W, W1),
  classify(W, L, U).
classify(W, nd(L, W1, R), nd(L, W1, U)) :- !, classify(W, R, U).
lower([], _ ) :- !.
lower([X;Y],[X;T]) :- !, lower(Y,T).
lower([X;Y],[Z;T]) :- X < Z.

write_tree(X) :- var(X), !,
write_tree(nd(L,W,R)) :- !, write_tree(L), name(W1,W), write(W1),
                      write(‘, ‘), write_tree(R).

Execution:

To run the program just give the command `!-order(X),` followed by the list of words.

%!-order(X),

helder, antonio, luis, jose, fernando, jorge, carlos, stop.

ordered words:

antonio, carlos, fernando, helder, jorge, jose, luis.

Done.

PROBLEM 38

Verbal statement:

Write a program that builds up a tree on a given list of numbers, and then outputs the list in an ordered way.

The way of building the tree is:

1) The root is the first member of the list.

2) The left branch will consist of the less or equal nodes, and the right branch will consist of the greater or equal ones.

3) Each node is represented by t(L,N,R) where N is the node, L is the left subtree and R is the right subtree.

For example:

[3,2,1] will give

```
  3
 / 
2   1
```


Apply your program to the list:
[14,12,16,21,19,9,0,15,13,6,3,2,5,1,4,7,11,18,17].

Logic program:

\[
\text{goal}(X):- \text{make_tree}(X,T), \text{nl}, \text{write}(T), \text{nl}, \text{nl}, \text{liste_tree}(T,L,[[]]), \\
\text{write}(L), \text{nl}, \text{nl}.
\]

\[
\text{make_tree}([H:T], t(T1,H,T2)):- \text{split}(T,H,U1,U2), \\
\text{make_tree}(U1,T1), \\
\text{make_tree}(U2,T2).
\]

\[
\text{make_tree}([], [], []). \\
\text{make_tree}([[]], []). \\
\text{make_tree}([[]], []). \\
\text{make_tree}([[]], []). \\
\text{list_tree}(t(T1,H,T2), S, X):- \text{list_tree}(T1, S, [H; Y]), \\
\text{list_tree}(T2, Y, X).
\]

\[
\text{split}(A:L), C, [A; U1], U2):- A=C, !, \text{split}(L, C, U1, U2), \\
\text{split}(A:L), C, [U1; [A; U2]], :- A>C, !, \text{split}(L, C, U1, U2), \\
\text{split}([], [], []). \\
\]

Execution:

\[
\text{-goal}([14,12,16,21,19,9,0,15,13,6,3,2,1,4,7,11,18,17]).
\]

\[
t(t(t([], 0), t(t(t([], 1, []), 2, []), 3, t([], 4, []))), 6, t([], 7, [])), \\
9, t([], 11, []), 12, t([], 13, []), 14, t([], 15, []), 16, t(t(t([], 17, []), 18, []), 19, []), 21, []))
\]

\[
[0, 1, 2, 3, 4, 6, 7, 9, 11, 12, 13, 14, 15, 16, 17, 18, 19, 21]
\]

PROBLEM 39 [WARREN et al, 1977]

Verbal statement:

Generate a list of serial numbers for the items of a given list, the members of which are to be numbered in alphabetical order.

Logic program:

\[
\text{serialise}(L,R):- \text{pairlists}(L,R,A), \text{arrange}(A,T), 
\text{numbered}(T,1,N).
\]

\[
\text{pairlists}([X; L],[Y; R],[\text{pair}(X,Y); A]):- \text{pairlist}(L,R,A), 
\text{pairlists}([], []). \\
\text{arrange}([X; L], \text{tree}(T1,X,T2)):\text{- partition}(L,X,L1,L2), 
\text{arrange}(L1,T1), 
\text{arrange}(L2,T2).
\]

\[
\text{arrange}([], []). 
\]
Partition([X:L],X,L1,L2):- Partition(L,X,L1,L2).
Partition([X:L],Y,[X:L1],L2):- before(X,Y),
Partition(L,Y,L1,L2).
Partition([X:L],Y,L1,[X:L2]):- before(Y,X),
Partition(L,Y,L1,L2).
Partition([],_,[],[]).

before(pair(X1,Y1),pair(X2,Y2)):- X1<X2.

numbered(tree(T1,pair(X,N1),T2),NO,N):- numbered(T1,NO,N1),
N2 is N1+1,
numbered(T2,N2,N).

numbered(void,N,N).

**Problem 40**  [Pereira; Monteiro, 1978]

Verbal statement:

Construct a program for relating a binary tree with the list of its leaves (terminal nodes), and another one for testing whether two binary trees have the same leaves.

Logic program:

leaves(t(void,N,void),[N]:-Z).
leaves(t(ST1,N,STR),L:-Z):- leaves(ST1,L-X),
leaves(STR,X-Z).

same_leaves(T1,T2):- leaves(T1,L-[]),
leaves(T2,L-[]),

Comments:

void="the empty tree"

t(ST1,N,STR)="the binary tree with root N,
left subtree ST1, and right subtree STR"

The term [N:Z]-Z, where "-" is a binary functor, stands for a "difference list". It denotes the list whose sole member is N, obtained from the list [N:Z] "minus" Z.

The empty difference list is X-X. Difference lists allow for easy concatenation of lists. Because a variable stands in place of the usual "nil", the list may expand by unifying the variable at the end, which is individuated after the "minus" sign, with another list. Thus, in the second clause, the (difference) list L-Z is expressed as a concatenation of L-X and X-Z. Since X terminates with Z, L will also terminate with Z. A call to this procedure is

leaves(t(t(void,a,void),b,STR),[A, c]-[])
Notice that the '[]' in the call has the effect of 'closins' the final list obtained.

Execution:

Let us now briefly look at how this goal is actually executed. The goal matches only the second clause for 'leaves'. The body of the matching clause instance is leaves(t(void,a,void),[A,c]-X), leaves(ST1,X-[]). The result of executing the first of these two goals against the only clause which solves it is to instantiate A to a and X to c. The second goal matches the first clause, thereby instantiating ST1 to t(void,c,void), because X is already instantiated to c.

PROBLEM 41

Verbal statement:

Find a subtree ST in a tree T and change it by another subtree CH. Call R the final tree. Apply your program to the tree:

```
  X
 / \   
Y   Z
```

which may be represented by:

```
T = t(t(T1,X,T2),X,t(v,Z,v))
  = t(t(t(v,W,v),Y,v),X,t(v,Z,v)).
```

Logic program:

```
change(CH,ST,ST,CH),
change(CH,ST,t(T1,X,T2),t(R1,X,T2)):- change(CH,ST,T1,R1).
```

Execution:

```
:- change(CH,ST,T,R).
```

where CH stands for the initial tree and R for the result tree.
3.2 DEDUCTIVE REASONING OVER DATA BASES (nos. 42 to 59)

PROBLEM 42 [WARREN et al, 1977]

Verbal statement:
Calculate the population density per square mile and find countries of similar population density (differing by less than 5%).

Logic Program:

density(C,D):- pop(C,D), area(C,A), D is (P*1000)/A.

answer(C1,D1,C2,D2):- density(C1,D1), density(C2,D2),
D1>D2, 20*D1<21*D2.

pop(china,825), area(china,3380),
pop(india,586), area(india,1139),
pop(ussr,252), area(ussr,8709),
pop(usa,212), area(usa,3609).

PROBLEM 43 [EMDEN, 1977]

Verbal statement:
Design a deductive information retrieval system concerning some aspects of the operation of a university department, such as those presented under set notation:

<table>
<thead>
<tr>
<th>Takes</th>
<th>Math</th>
</tr>
</thead>
<tbody>
<tr>
<td>M. : Adiri</td>
<td>Math!129</td>
</tr>
<tr>
<td>C.Y.K : Chenk</td>
<td>Math!225</td>
</tr>
<tr>
<td>T.L. : Cook</td>
<td>Math!129</td>
</tr>
<tr>
<td>T.L. : Cook</td>
<td>Math!225</td>
</tr>
</tbody>
</table>
### Teaches

<table>
<thead>
<tr>
<th>Teacher</th>
<th>Course</th>
</tr>
</thead>
<tbody>
<tr>
<td>J.F. Glotz</td>
<td>Math!129</td>
</tr>
<tr>
<td>J.F. Glotz</td>
<td>Math!225</td>
</tr>
<tr>
<td>C. Twill</td>
<td>Math!170</td>
</tr>
</tbody>
</table>

### Student

<table>
<thead>
<tr>
<th>Student</th>
<th>Major</th>
<th>Year</th>
</tr>
</thead>
<tbody>
<tr>
<td>M. Adiri</td>
<td>Biology</td>
<td>1974</td>
</tr>
<tr>
<td>N.A. Buczek</td>
<td>Recreation</td>
<td>1976</td>
</tr>
<tr>
<td>C.Y.K Chenk</td>
<td>Physics</td>
<td>1976</td>
</tr>
<tr>
<td>T.L Cook</td>
<td>Engineering</td>
<td>1975</td>
</tr>
<tr>
<td>G.C Giusti</td>
<td>Engineering</td>
<td>1976</td>
</tr>
<tr>
<td>A Hammer</td>
<td>Child Care</td>
<td>1973</td>
</tr>
<tr>
<td>K.L Mensink</td>
<td>Kinesiology</td>
<td>1973</td>
</tr>
</tbody>
</table>

### Scheduled

<table>
<thead>
<tr>
<th>Course</th>
<th>Code</th>
<th>Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Math!129</td>
<td>Phy@3009</td>
<td>2.30</td>
</tr>
<tr>
<td>Math!301</td>
<td>Phy@3009</td>
<td>2.30</td>
</tr>
</tbody>
</table>

Logic Program:

```prolog
:- op(500, xfy, :-).
:- op(300, xfy, -).
:- op(300, xfy, :-).
:- op(100, xfy, :-).

takes(X, Math!129) :- year(X, 1), program(X, engineering).
year(X, Z) :- student(X, Y, Z1), Z is 1977-Z1.
program(X, Y) :- student(X, Y, Z).
course_prefix(X!Y, X).
course_number(X!Y, Y).
initials(X!Y, X).
lastname(X!Y, Y).
graduate_course(X) :- course_number(X, Y), Y > 499.
```
conflict(X1,X2):- scheduled(X1,Y,Z),
        scheduled(X2,Y,Z),
        X1=\=X2.

teaches(X,Y):- takes(Z,Y).

takes(m:adiri,math!129),
takes(c.y.k:chenk,math!225),
takes(t.l:cook,math!129),
takes(t.l:cook,math!225).

teaches(j.f:slotz,math!129),
teaches(j.f:slotz,math!225),
teaches(c:twill,math!170).

student(m:adiri,biology,1974),
student(n.a:buczek,recreation,1976),
student(c.j.k:chenk,physics,1976),
student(t.l:cook,engineering,1975),
student(s.c:siusti,engineering,1976),
student(a:hammer,child care,1973),

scheduled(math!129,phy@3009,2,30),
scheduled(math!301,phy@3009,2,30).

PROBLEM 44 [WARREN,1975a]

Verbal statement:

The number of days in a year is 366 each four years; otherwise it is 365. How many days have years 1975, 1976 and 2000?

Logic program:

:-op(300,fxy,'no_of_days_in'),
:-op(500,xfy,'IS').

no_of_days_in_{Y 'IS' 366:- 0 is Y mod 4,
                not(0 is Y mod 100),!},
no_of_day_in_{Y 'IS' 365}.

:-X 'IS' no_of_days_in Y, write(X).

Execution:

:-X 'IS' no_of_days_in 1975, write(X).
365

:-X 'IS' no_of_days_in 1976, write(X).
366
:-X 'IS' no-of-days-in 2000, write(X).

PROBLEM 45  [WARREN,1975a]

Verbal statement:

Logic program:
:-op(900,xfy, '&').
:-op(700,xfy, 'likes').

John likes mary.
John likes Jane.
Mary likes Pete.
Pete likes Kate.
Jane likes John.
Kate likes ..

:-X likes Y, Y likes X, write(('X&Y')), fail.

Execution:

John & Jane
Pete & Kate
Jane & John
Kate & Pete
Kate & Kate
?

PROBLEM 46  [WARREN,1975a]

Verbal statement:
Suppose we are given the following family tree, with each person's age in brackets:

```
  John (57)
     /    \
    /      \
Mark (25)  Paul (36)
       /    \    \
      /      \
     Tom (15)
```


and we wish to find all solutions to the question: "Does John have two descendents whose ages differ by ten years?"

Write a program to solve this problem.

Logic program:

\[
\text{has\_descendant}(X,Z) :- \text{begat}(X,Z), \\
\text{has\_descendant}(X,Z) :- \text{has\_descendant}(X,Y), \\
\hspace{1cm} \text{begat}(Y,Z).
\]

\[
\text{begat}(\text{John}, \text{Mark}), \\
\text{begat}(\text{John}, \text{Paul}), \\
\text{begat}(\text{Paul}, \text{Tom}), \\
\]

\[
\text{is\_aged}(\text{John}, 57), \\
\text{is\_aged}(\text{Mark}, 25), \\
\text{is\_aged}(\text{Paul}, 36), \\
\text{is\_aged}(\text{Tom}, 15).
\]

\[
\text{?-has\_descendant}(\text{John}, X), \text{is\_aged}(X,N), \\
\hspace{1cm} \text{has\_descendant}(\text{John}, Y), \text{is\_aged}(Y,M), M \text{ is } N+10.
\]

**PROBLEM 47** [PEREIRA et al., 1978]

Verbal statement:

Construct a small data base obeying to:

- the goal 'descendant(X,Y)' is true if Y is a descendant of X

Consider that Ishmael and Isaac are descendents of Abraham, and Esau and Jacob are descendents of Isaac.

Logic program:

\[
\text{descendant}(X,Y) :- \text{offspring}(X,Y), \\
\text{descendant}(X,Z) :- \text{offspring}(X,Y), \text{descendant}(Y,Z).
\]

\[
\text{offspring}(\text{abraham}, \text{ishmael}), \\
\text{offspring}(\text{abraham}, \text{isaac}), \\
\text{offspring}(\text{isaac}, \text{esau}), \\
\text{offspring}(\text{isaac}, \text{jacob}).
\]

Execution:

If for example the question:

\[
?-\text{descendant}(\text{abraham}, X).
\]

is executed, Prolog's backtracking results in different descendents of Abraham being returned as successive instances of the variable X, i.e.,
\[ X = \text{ishmael} \]
\[ X = \text{isaac} \]
\[ X = \text{esau} \]
\[ X = \text{Jacob} \]

**PROBLEM 48**

**Verbal statement:**

There were three departures for a Monte Carlo rally:

**London**: John (BMW), Tommy (FORD), Fred (BMW), Anne (FORD) and Teddy (BMC)

**Paris**: Guy (FIAT), Claude (FORD), Jean (FIAT), and Brigitte (BMC)

**Lisbon**: Luis (FIAT), Carlos (BMW), Lucas (BMC), Pedro (FORD), and Nuno (FIAT).

and only four pilots, Tommy, Fred, Pedro and Nuno, arrived to Monte Carlo.

Which cars did arrive to Monte Carlo?

From where did the pilots that arrived to Monte Carlo leave?

**Logic Program:**

```plaintext
rally:- pilots(A,london),
       pilots(B, lisbon),
       pilots(C, paris),
       pilots(D, bmv),
       pilots(E, fiat),
       pilots(F, ford),
       pilots(G, bmc),
       pilots(H, monte-carlo),
       intersection(A, H, Lon),
       intersection(B, H, Lis),
       intersection(C, H, Par),
       intersection(D, H, Bmw),
       intersection(E, H, Fiat),
       intersection(F, H, Ford),
       intersection(G, H, Bmc),
       write('Arrived: '),
       write('From London: '), write(Lon),
       write('From Lisbon: '), write(Lis),
       write('From Paris: '), write(Par),
       write('in BMW: '), write(Bmv),
       write('in FIAT: '), write(Fiat),
       write('in FORD: '), write(Ford),
       write('in BMC: '), write(Bmc).
```

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intersection([],X,[]).
intersection([X|Y],Y,[X|Z]) :- member(X,Y),! 
intersection(R,Y,Z),
intersection([X|R],Y,Z) :- intersection(R,Y,Z).

member(X,[X|_]).
member(I,[_|I]) :- member(I,I).

pilots([John,tommy,fred,anne,teddy],london).
pilots([guy,claire,jean,brigitte],paris).
pilots([luis,carlos,lucas,pedro,nuno],lisboa).
pilots([fred,carlos,john],bmw).
pilots([luis,nuno,jane,guy],fiat).
pilots([anne,tommy,claire,pedro],ford).
pilots([teddy,brigitte,lucas],bmc).
pilots([tommy,fred,pedro,nuno],monte_carlo).

Execution:
The execution of ?-rally,
gives us the following results:

Arrived:
From London : [tommy,fred]
From Lisbon : [nuno,pedro]
From Paris : []
in BMW : [fred]
in FIAT : [nuno]
in FORD : [pedro,tommy]
in BMC : []

PROBLEM 49

Verbal statement:
Write a program considering the following facts:
- number(X,N) means that person X can be reached by calling phone number N.
- visits(X,Y) means that person X is visiting person Y.
- at(X,Y) means that person X is at the residence of person Y.
- Phone(X,N) mean that person X has phone number N.

and the following premises:

1) \( (WX) \& (WY) \& (WZ) \& \text{visits}(X,Y) \& \text{at}(Y,Z) \implies \text{at}(X,Z) \)

2) \( (WU) \& (WV) \& (WN) \& \text{at}(U,V) \& \text{phone}(V,N) \implies \text{number}(U,N) \)

able to find the way of reaching a person, having a particular phone number base and knowing who visits whom and where is the visited person.

Logic Program

*/ Finding Process */

find(X):- number(X,N),write('Phone: '),write(N),nl.
find(_):- write('Don't Know'),nl.

number(X,N):- at(X,Y),phone(Y,N),!.
number(X,N):- phone(X,N),!.

at(X,Z):- visits(X,Y),at(Y,Z),!.

*/ Phone numbers data base */

phone(coleman,'100001').
phone(gordon,'100002').
phone(wagner,'100003').
phone(smith,'100004').

Execution:

Suppose you want to reach Coleman and you know he is visiting with Wagner and that Wagner is at Gordon's house.
You just have to write:

visits(coleman,wagner).
at(wagner,gordon).

:-find(coleman).

the answer would be:

Phone: 100002

Remark: This problem was suggested from 'The Thinking Computer', by B. Raphael.
PROBLEM 50

Verbal statement:

Consider a fact deduction machine which takes a collection of known facts and makes new conclusions, over a domain of animals in a zoo.

Suppose the machine knowledge is composed of 15 recognition productions:

P1
If the animal has hair, then it is a mammal.

P2
If the animal gives milk then it is a mammal.

P3
If the animal has feathers then it is a bird.

P4
If the animal flies, and it lays eggs, then it is a bird.

P5
If the animal is a mammal, and it eats meat, then it is a carnivore.

P6
If the animal is a mammal, it has pointed teeth it has claws, and its eyes point forward, then it is a carnivore.

P7
If the animal is a mammal, and it has hoofs, then it is an ungulate.
If the animal is a mammal, and it chews curd, then it is an ungulate, and it is even toed.

If the animal is a carnivore, it has a tawny color, and it has dark spots, then it is a cheetah.

If the animal is a carnivore, it has a tawny color, and it has black stripes, then it is a tiger.

If the animal is an ungulate, it has long legs and a long neck, it has a tawny color, and it has dark spots, then it is a giraffe.

If the animal is an ungulate, it has a white color, and it has black stripes, then it is a zebra.

If the animal is a bird, it does not fly, it has long legs and a long neck, and it is black and white, then it is an ostrich.

If the animal is a bird, it does not fly, it swims, and it is black and white, then it is a penguin.
If the animal is a bird and it is a good flyer then it is an albatross.

Write a program (simulating that machine) able to discover a certain animal by means of asking its characteristics using the recognition productions, and to describe the properties of any animal in its knowledge base.

Logic program:

```prolog
/* Knowledge base */
rule(1, animal, mammal, [c1]).
rule(2, animal, mammal, [c2]).
rule(3, animal, bird, [c3]).
rule(4, animal, bird, [c4, c5]).
rule(5, mammal, carnivore, [c6]).
rule(6, mammal, carnivore, [c7, c8, c9]).
rule(7, mammal, undulate, [c10]).
rule(8, mammal, undulate_toed, [c11]).
rule(9, carnivore, cheetah, [c12, c13]).
rule(10, carnivore, tiger, [c12, c14]).
rule(11, undulate, giraffe, [c15, c16, c12, c13]).
rule(12, undulate, zebra, [c17, c14]).
rule(13, bird, ostrich, [c18, c15, c16, c19]).
rule(14, bird, penguin, [c18, c20, c19]).
rule(15, bird, albatross, [c21]).

/* Recognition process: discover animal's name */
recognition(X):- rule(N, X, Y, Z), discover(Z), found(rule),
    conclusion(X, Y, N), recognition(Y),
    retractall(fact(_, _)),
recognition(_):- retract(rule), write('Done.'), nl.
recognition(_):- write('Don't know this animal.'), nl.

found(X):- X, !.
found(X):- assert(X).

/* Discovering process */
discover([]).
discover([X; Y]):- ask(X), discover(Y).
ask(X):- fact(X, yes), !.
ask(X):- fact(X, no), !, fail.
ask(c1):- write('has it hair?') nl, !, complete(c1).
ask(c2):- write('does it give milk?') nl, !, complete(c2).
```

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ask(c3):- write('has it feathers?'),nl,!,complete(c3). ask(c4):- write('does it fly?'),nl,!,complete(c4). ask(c5):- write('does it lay eggs?'),nl,!,complete(c5). ask(c6):- write('does it eat meat?'),nl,!,complete(c6). ask(c7):- write('has it pointed teeth?'),nl,!,complete(c7). ask(c8):- write('has it claws?'),nl,!,complete(c8). ask(c9):- write('has it eyes pointing forward?'), nl,!,complete(c9). ask(c10):- write('has it hoofs?'),nl,!,complete(c10). ask(c11):- write('does it chew cud?'),nl,!,complete(c11). ask(c12):- write('has it a tawny color?'),nl,!,complete(c12). ask(c13):- write('has it dark spots?'),nl,!,complete(c13). ask(c14):- write('has it black stripes?'),nl,!,complete(c14). ask(c15):- write('has it long legs?'),nl,!,complete(c15). ask(c16):- write('has it a long neck?'),nl,!,complete(c16). ask(c17):- write('has it a white color?'),nl,!,complete(c17). ask(c18):- write('does it not fly?'),nl,!,complete(c18). ask(c19):- write('is it black and white?'),nl,!,complete(c19). ask(c20):- write('does it swim?'),nl,!,complete(c20). ask(c21):- write('is it a good flyer?'),nl,!,complete(c21). complete(X):- read(Y),assert(fact(X,Y)),Y=yes./* Conclusion of the recognition process */ conclusion(X,Y,N):- nl,tab(4),write('--- the '),write(X), write(' is a '),write(Y),write(' by rule '), write(N),nl,nl. /* Description process: discover animal's properties */ description(X):- rule(N,Y,X,Z),description1(Y,L,[]), conclusion1(X,L,Y,Z,N), description(_,_):- nl,write('Don't know this animal.'),nl. description1(Y,L,Ls):- rule(_,Y,_,_),description1(X,L,[X|Ls]), description1(_,L,L). /* Conclusions of the description process */ conclusion1(X,L,Y,Z,N):- nl,write('a '),write(X), write(' is an '), output(L),write(Y), write('satisfying conditions: '),nl, output(Z),nl,write('by rule '),write(N), write(''),nl. output([]), output([A:B]):- write(A),tab(1),output(B).
Execution:

When discovering the animal's name

1) Successful recognition

:-recognition(animal).

has it hair?
  ! yes.

  ---the animal is a mammal by rule 1

does it eat meat?
  ! yes.

  ---the mammal is a carnivore by rule 5

has it a tawny color?
  ! yes.
has it dark spots?
  ! no.
has it black stripes?
  ! yes.

  ---the carnivore is a tiger by rule 10

Done.

2) Unsuccessful recognition

:-recognition(animal).

has it hair?
  ! no.
does it give milk?
  ! no.
has it feathers?
  ! no.
does it fly?
  ! no.

Don't know this animal.

When discovering the animal's properties

1) Successful description

:- description(tiger).

A tiger is an animal mammal carnivore satisfying conditions:

  c12    c14
by rule 10

2) unsuccessful description

: description(horse).
Don't know this animal.

Remark:

The program answers only with the numbers of the conditions for
comodity of the programmer. A procedure may be written to
translate these numbers into the sentences of the conditions.

(This problem was suggested from 'Artificial Intelligence', by
P. Winston.

PROBLEM 51

Verbal statement:

Write a simple question-answering system for the exploration of
a data base with transistor information (transistor name,
material, polarity, function, power, collector base voltage,
collector emitter voltage, amplification factor and capsula
type), and according to the table:

<table>
<thead>
<tr>
<th>characteristics</th>
<th>mat</th>
<th>pol</th>
<th>fun</th>
<th>pow</th>
<th>vcb</th>
<th>vce</th>
<th>hfe</th>
<th>cap</th>
</tr>
</thead>
<tbody>
<tr>
<td>Transistor Name</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2n2219</td>
<td>si</td>
<td>n</td>
<td>hsa</td>
<td>800</td>
<td>60</td>
<td>30</td>
<td>120</td>
<td>T05</td>
</tr>
<tr>
<td>2n2904</td>
<td>si</td>
<td>p</td>
<td>hss</td>
<td>300</td>
<td>60</td>
<td>40</td>
<td>120</td>
<td>T05</td>
</tr>
<tr>
<td>2n3055</td>
<td>si</td>
<td>n</td>
<td>lpa</td>
<td>11500</td>
<td>100</td>
<td>70</td>
<td>70</td>
<td>T03</td>
</tr>
<tr>
<td>2n3904</td>
<td>si</td>
<td>n</td>
<td>hss</td>
<td>310</td>
<td>60</td>
<td>40</td>
<td>300</td>
<td>T092</td>
</tr>
<tr>
<td>2n3906</td>
<td>si</td>
<td>p</td>
<td>hss</td>
<td>310</td>
<td>40</td>
<td>40</td>
<td>300</td>
<td>T092</td>
</tr>
</tbody>
</table>

The system is requested to deal with user's changes of mind,
translation of user's unities, and output of all characteristics
for a given transistor, specified by the user.

Logic program:

begin:- write('Characteristics(value)'), nl, repeat, nl,
       continue(_).

continue(L):- write('- '), ttyflush, read(C), Process(C,L).

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Process('Goodbye',_).
Process(stop,L):- ( trans(X,L),nl,write(trans(X,L)),nl,
        write('Do you want it(Yes or no)?'),
        nl,read(S),S=yes,!,
        write('New characteristics'),nl,fail ;
        write('No transistors available'),nl,continue(L) ).

Process(C,L):- ( subs(C,L),L=L1 ; replace(C,L,L1) ),
        continue(L1).

subst(C,L):- reduct(C,C1),match(C1,L).

reduct(C,C1):-C=..[X,N,mili],C1=..[X,N].
reduct(C,C1):-C=..[X,N,w],C1=..[X,M],M is N*1000.
reduct(C,C1):-C=..[X,N,-],C1=..[X,N].
reduct(C,C).

match(mat(A),[A;_]),
match(pol(B),[_,B;_]),
match(fun(C),[_,_;C;_]),
match(pow(D),[_,_,D;_]),
match(vcb(E),[_,_,_,E;_]),
match(vce(F),[_,_,_,_,F;_]),
match(hfe(G),[_,_,_,_,_,G;_]),
match(cap(H),[_,_,_,_,_,_,H]).

replace(C,L,L1):- subst(C,L1),replace1(L,L1).

replace1(X,X):- var(X),!.
replace1([],[]):- !.
replace1([HITJ],[H1;T1]):- !,replace1(H,H1),replace1(T,T1),
replace1(_,_).

/* Transistor information */
trans(t2n2219,[si,n,hsa,300,60,30,120,'T05']).
trans(t2n2904,[si,p,hsa,300,60,40,120,'T05']).
trans(t2n3055,[si,n,ipa,115000,100,70,70,'T03']).
trans(t2n3904,[si,n,hsa,310,60,40,300,'T092']).
trans(t2n3906,[si,p,hsa,310,40,40,300,'T092']).

Execution:
To run the system, just perform the command: ':-begin.'
:-begin.

Characteristics(value)
  - mat(si),
  - pol(p),
  - fun(hsa),
  - pot(300,mili),
  - vcb(60).
- stop.

trans(t2n2904,[si,r,hss,300,60,40,120,T05])

Do you want it (yes or no)?

no.

No transistors available
- fun(hsa).
- pol(n).
- pot(800).
- stop.

trans(t2n2219,[si,n,hss,800,60,30,120,T05])

Do you want it (yes or no)?

yes.

New characteristics
- Goodbye.

PROBLEM 52 [MELLISH, 1977]

Verbal statement:

Write a program that behaves as a travel agent and holds an interface with an user in order to determine his precise travel requirements and to present him with information enabling him to choose air flights.

Imagine a question-asking strategy determined by the requirements to fill in slots in a system of frames in a depth-first manner. To prevent unnecessary questions imagine a system of default values and a mechanism that can avoid asking questions whose answers have been provided either implicitly or explicitly at some earlier time.

The program must also be able to cope with the client changing his mind by means of dealing with the contradictions arising from his inputs.

Suppose you have the following flight information, already written as a PROLOG database:

flight(edinburgh,paris,jan,morn,f1),
flight(edinburgh,paris,jan,aft,f2),
flight(edinburgh,paris,jan,aft,f3),
flight(paris,rome,feb,morn,f4),
flight(paris,rome,feb,morn,f5),
flight(paris,rome,feb,aft,f6),
flight(rome,edinburgh,mar,morn,f7),

where flight(F,T,D,Ti,Fl) means a flight from F to T in month D at time Ti with number Fl.
Logic program:
:- op(410,xy, ",").

/* Overall control of the dialogue */
talk:- default(trip(1),exists),default(trip(2),exists),
default(homeport(1),edinburgh),
repeat,discussion(X),nl,nl,
display('trips booked:'),nl,nl,
output(X),nl.
discussion(X):- nextafter(0,M),trip specification(M,X).

/* Gathering of trip information */

trip specification(N,trip(d(A),t(B),f(C),to(D),f1(E),tr(F)),Ts):-
discover(date(N,A), discover(time(N),B),
discover(homeport(N),C), discover(foreignport(N),D),
schedule(C,D,A,B,E,N), discover(traveller(N),F),!,
continue(D,F,N,Ts).

continue(Dest,Trav,N,Ts):- nextafter(N,M),!,
default(homeport(M),Dest),
recall(homeport(1),H), default(foreignport(M),H),
default(traveller(M),Trav),!,
trip specification(M,Ts),
continue(_,_,_,[]).

schedule(F,T,D,Ti,F1,N):- fact(ok(F1,N)yes),
feasible(F,T,D,Ti,F1,N),!.
schedule(F,T,D,Ti,F1,N):- flight(F,T,D,Ti,F1),
scheduleok(F1,N,Con),!, Con = 0.
schedule(_,_,_,_,_):- display('no flights available'),
nl, discover(changed,Z).

scheduleok(F1,N,0):- discover(ok(F1,N),R),!, R = yes,
scheduleok(_,1).

feasible(F,T,D,Ti,F1,N):- flight(F,T,D,Ti,F1),!.
feasible(_,_,_,_,_,N):- retract(fact(ok(F,N),X)),fail.

/* Manipulation of facts */
discover(lit,Val):- fact(lit,Val),!.
discover(lit,Val):- repeat,askclient(lit,Val,Con),!
    Con = 0.

default(Lit,Val):- fact(Lit,Newval),!.
default(Lit,Val):- assert(fact(Lit,Val)),!.

recall(Lit,Val):- fact(Lit,Val),!.

55
/* Communication with user */

askclient(Lit, Val, Con):-
    display(Lit), display(' ?'), nl,
    read(Input), interpret(Input, Con), !,
    notaskagain(Lit, Val, Con), !.

notaskagain(Lit, Val, 0):- !, fact(Lit, Val).

interpret([], 0).
interpret(A, B, R):- dealwith(A, S), interpret(B, T),
                  R is S + T.

dealwith(A, B, 0):- fact(A, B), !.
dealwith(A, B, 1):- fact(A, C), retract(fact(A, C)),
                  assert(fact(A, B)), !.
dealwith(A, B, _):- assert(fact(A, B)), !.

/* Miscellaneous */

nextafter(N, M):- fact(trip(M), exists), N < M,
                  P is N + 1, nonebetween(P, M), !.

nonebetween(X, X):- !.
nonebetween(X, Y):- fact(trip(X), exists), !, fail.
nonebetween(X, Y):- Z is X + 1, nonebetween(Z, Y).

output(A, B):- display(A), nl, output(B).

/* Flight information */

flight(edinburgh, paris, jan, morn, f1).
flight(edinburgh, paris, jan, aft, f2).
flight(edinburgh, paris, jan, aft, f3).
flight(paris, rome, feb, morn, f4).
flight(paris, rome, feb, morn, f5).
flight(paris, rome, feb, aft, f6).
flight(rome, edinburgh, mar, morn, f7).

Execution:

:- talk.

date(1)?
: [trip(3), exists, foreignport(1), paris, foreignport(2), rome].

date(1)?
: [date(1), jan, traveller(1), me].

time(1)?
: [time(1), morn].

ok(f1, 1)?
: [ok(f1, 1), no].

no flights available
change?
: [time(1), aft, date(2), feb],
ok(f2, 1)?
: [ok(f2, 1), no],
ok(f3, 1)?
: [ok(f3, 1), yes],
time(2)?
: [time(2), morn, traveller(2), fred],
ok(f4, 2)?
: [ok(f4, 2), yes],
date(3)?
: [date(3), mar, trip(1), notexists, ok(f4, 2), no],
ok(f5, 2)?
: [time(2), aft],
ok(f6, 2)?
: [ok(f6, 2), yes],
time(3)?
: [time(3), morn],
ok(f7, 3)?
: [ok(f7, 3), yes].

trips booked:
tr(d(feb), t(aft), f(Paris), to(rome), fl(f6), tr(fred))
tr(d(mar), t(morn), f(rome), to(edinburgh), fl(f7), tr(fred))

PROBLEM 53  [SILVA&COTTA, 1978]

Verbal statement:

In the preceding problem, the program has two ways of achieving a situation in which there are "no flight available".

The first way corresponds to the inexistence of a flight in the database for the user's specifications, and the other corresponds to a disagreement about all the flights the program knows for the user's specifications.

Write a new version of that program where these situations are distinguished. For the first situation output the literals whose values are preventing the attainment of a flight.

Logic program:

The procedure "setflight" has now the following form:

setflight(F, T, D, Ti, Fl, N):- fact(ok(Fl, N), yes),
feable(F, T, D, Ti, Fl, N), !.
setflight(F, T, D, Ti, Fl, N):- flight(F, T, D, Ti, Fl),
flighthk(Fl, N, Con), !, Con=0.
setflight(F,T,D,Ti,F1,N):- (flight(F,T,D,Ti,_)),
    display('no more flights available'), nl, !,
    discover(change,Z).
setflight(F,T,D,Ti,F1,N):- display('no flights available'), nl,
    display('possible changes'), nl, alterations(F,T,D,Ti),
setflight(_,_,_,_,_,N):- read(Input), interpret(Input, Con), fail.

The new procedure alteration has the form:

alterations(F,T,D,Ti):- first(flight(F,T,D,_,_)),
    display('time'), nl, fail.
alterations(F,T,D,Ti):- first(flight(F,T,_,Ti,_,_)),
    display('date'), nl, fail.
alterations(F,T,D,Ti):- first(flight(F,_,D,Ti,_,_)),
    display('foreign port'), nl, fail.
alterations(F,T,D,Ti):- first((flight(F,T,X,Y,_,_),X==D, Y\==Ti)),
    display('time and date'), nl, fail.
alterations(F,T,D,Ti):- first((flight(F,X,D,Y,_,_),X==T, Y\==Ti)),
    display('time and foreign port'), nl, fail.
alterations(F,T,D,Ti):- first((flight(F,X,Y,Ti,_,_),X==T, display('date and foreign port'), nl, fail.
alterations(F,T,D,Ti):- first((flight(F,X,Y,Z,_,_),X==T, Y\==D, Z\==Ti)),
    display('time, date and foreign port'), nl, fail.

first(F):- F, !.
first((P,Q)):- P, first(Q), !.

PROBLEM 54

Verbal statement:

Specify a virtual relational database for the kinship facts.
Take the following family tree for facts:

```
  Fred   Sue
    /   |
   /    |
  Henry Bill Barb
  /     /     |
Cathy  Bob   Barb
```
Logic program:

grandparent(X,Z) : - grandfather(X,Z); grandmother(X,Z).

grandfather(X,Z) : - father(X,Y); parent(Y,Z).

grandmother(X,Z) : - mother(X,Y); parent(Y,Z).

parent(X,Y) : - father(X,Y); mother(X,Y).

brother(X,Y) : - male(X); parent(Z,X); parent(Z,Y), X \neq Y.

sister(X,Y) : - female(X); parent(Z,X); parent(Z,Y), X \neq Y.

uncle(X,Y) : - male(X); parent(Z,X); grandparent(Z,Y).

aunt(X,Y) : - female(X); parent(Z,X); grandparent(Z,Y).

cousin(X,Y) : - parent(Z,X); parent(T,Y),

(brother(Z,T) ; sister(Z,T)).

husband(X,Y) : - father(X,Z); mother(Y,Z).

wife(X,Y) : - husband(Y,X).

father(fred,henry),
mother(sue,henry),
father(fred,bill),
mother(sue,bill),
father(fred,barb),
mother(sue,barb),
father(henry,cat),
mother(barb,bob),
male(fred),
female(barb),
male(bob),
female(sue),
male(henry),
female(cathy),
male(bill).

PROBLEM 55 [TOWNSEND, 1979]

Verbal statement:

Write a program to implement a pre-registration appointments matching scheme. It covers the allocation of the pre-registration six-month surgical and medical appointments that the law requires (here called jobs, or 'posts' with a particular consultant's firm) to newly qualified doctors (here referred to as applicants).

A general representation of a job might be: the 'Job number', the special restrictions on the applicants to be allocated to this job, the numbers of posts available in the six-month periods starting in August and February, the 'Job preference list', the list of the reference numbers of applicants for the posts in that job, ranked by the consultant in charge in the
order of his preference and the result lists. The corresponding record for an applicant might be: the 'Job number', the sex, the season, the preference lists and the corresponding result lists. The problem of assigning the members of two sets to one another is dealt according to the following definition of a 'stable marriage'. 'Consider two distinct sets A and B. An assignment of the members of A to the members of B is said to be a stable marriage if and only if there exists no elements a and b (belonging to A and B respectively) who are not assigned to each other but who would both prefer each other to their present partners'.

Logic Program:

/* PRAMS PART 1 in PROLOG */

program:- Jobs(Jobslist), apps(Appslist),
prepare(Jobslist),
alloc1(Joblist,Appslist,Jobslist).

alloc1([Job:JL],Appslist,Jobslist):-
offer(Job,Appslist,Jobslist),
alloc(JL,Appslist,Jobslist),
alloc([],Appslist,Jobslist):- show(Jobslist).

offer(Job(J,Lim,NA,NF,JPrefs,As,Af,All),Appslist,Jobslist):-
write(J),
N is NA+NF,
offer1(Job,JPrefs,N,0,All,Appslist,Jobslist).

offer1(_,[],_,_,_,_),
offer1(_,N,_,N,_,_),
offer1(Job,[A]JPrefs,N,K,All,Appslist,Jobslist):-
member(A,All),
accept(A,Job,Appslist,Jobslist),
K1 is K+1,
offer1(Job,JPrefs,N,Kl,All,Appslist,Jobslist),
offer1(Job,[A]JPrefs,N,K,All,Appslist,Jobslist):-
offer1(Job,JPrefs,N,K,All,Appslist,Jobslist).

accept(A,Job,Appslist,Jobslist):-
member(app(A,-,-,Maprefs,X,Saprefs,Y),Appslist),
accept1(A,Maprefs,Saprefs,X,Y,J,Appslist,Jobslist).

accept1(A,Maprefs,Saprefs,X,Y,J,Appslist,Jobslist):-
member(J,Maprefs),!
accept2(A,J,Maprefs,X,Appslist,Jobslist),
accept1(A,Maprefs,Saprefs,X,Y,J,Appslist,Jobslist):-
member(J,Saprefs),!
accept2(A,J,Saprefs,Y,Appslist,Jobslist).
accept2(_, J, X, _):= nonvar(X), X=J, !.
accept2(_, J, X, _):= nonvar(X), !, fail.
accept2(A, J, Prefs, X, Appslist, Jobslist):= 
  accept3(A, J, Prefs, X, Appslist, Jobslist).

accept3(_, J, [J|_], J, _).
accept3(A, J, [J|Prefs], X, Appslist, Jobslist):= 
  not(ask(A, J, X, Appslist, Jobslist)),
  accept3(A, J, Prefs, X, Appslist, Jobslist).

ask(A, J, Appslist, Jobslist):= 
  member(Job(J, Lim, NA, NF, J, Prefs, As, Af, All), Jobslist),
  N is NA+NF,
  ask1(A, J, NF, Prefs, N, All, Appslist, Jobslist),
  ask1(A, J, J, Prefs, N, All, Appslist, Jobslist):= 
    ismember(A, All),
  ask1(A, J, Prefs, N, All, Appslist, Jobslist):= 
    offer1(J, J, Prefs, N, 0, All, Appslist, Jobslist), !,
    ismember(A, All).

prepare([], Job(No, Lim, NA, NF, Prefs, As, Af, All)!: JL):= 
  makelist(NA, [], As),
  makelist(NF, [], Af),
  N is NA+NF,
  makelist(N, [], All),
  prepare(JL).
prepare([]).

member(X, [X|_])!: !.
member(X, [X|L]):= member(X, L).
ismember(X, [Y|_])!: nonvar(Y), X=Y, !.
ismember(X, [X|L])!: ismember(X, L).

Jobs([], 
  Job(1,0,1,1,[1,9,4,6,2,7,3,5,8],_,_),
  Job(2,0,1,1,[3,2,1,5,7,6,10],_,_),
  Job(3,0,1,1,[9,6,7,5,3,4,1,2],_,_),
  Job(4,0,1,2,[4,7,1,6,2,5,3,10],_,_),
  Job(5,0,2,2,[1,4,8,3,2,5,10,7,6],_,_),
  Job(6,0,3,3,[9,10,4,6,5,3,2,13],_,_),
  Job(7,0,2,2,[1,2,9,10,6,4,3,5],_,_),
  Job(8,0,3,0,[7,8,1,2,6,4,3,5],_,_),
  Job(9,0,0,3,[4,3,8,10,9],_,_))].


```prolog
apps([  
  app(1, m, 0, [1, 2, 3, 4], _, [5, 6, 7, 8], _),  
  app(2, f, 0, [1, 4, 2, 3], _, [6, 7, 8, 5], _),  
  app(3, m, 1, [1, 3, 2, 4], _, [5, 8, 7, 9], _),  
  app(4, m, 0, [1, 3, 4, 9], _, [6, 5, 8, 7], _),  
  app(5, m, 2, [3, 1, 4, 2], _, [5, 6, 8, 7], _),  
  app(6, f, 3, [4, 1, 2, 3], _, [7, 5, 6, 8], _),  
  app(7, m, 0, [2, 4, 1, 3], _, [8, 5], _),  
  app(8, m, 0, [1], _, [5, 8, 9], _),  
  app(9, f, 1, [3, 1], _, [6, 7, 9], _),  
  app(10, m, 0, [2, 4, 9], _, [5, 6, 7], _)  
]).
```

Execution:

`:- program.`

`123456789`

RESULTS

1 [ 1 4 ]
2 [ 3 5 ]
3 [ 9 ]
4 [ 7 6 2 ]
5 [ 1 8 3 5 ]
6 [ 9 10 4 2 _ _ ]
7 [ 6 _ _ ]
8 [ 7 _ _ ]
9 [ 10 _ _ ]

PROBLEM 56 [PEREIRA&PORTO,1980]

Verbal statement:

Write a program for colouring any planar map with at most four colours, such that no two adjacent regions have the same colour.

Logic program:

The program consists of a complete list of pairs of different colours, taken from a collection of form. These constitute the admissible pairs of colours for regions next to each other.

next(blue, yellow).
next(blue, red).
next(blue, green).
next(yellow,blue).
next(yellow,red).
next(yellow,green).
next(red,blue).
next(red,yellow).
next(red,green).
next(green,blue).
next(green,yellow).
next(green,red).

To obtain a colouring of the map below, we give as a goal to the program all the pairs of regions that are next to each other. This can be done systematically by first pairing region 1 with higher numbered regions next to it, then region 2, etc.

goal(R1,R2,R3,R4,R5,R6):- next(R1,R2),next(R1,R3),
next(R1,R5),next(R1,R6),
next(R2,R3),next(R2,R4),
next(R2,R5),next(R2,R6),
next(R3,R4),next(R3,R6),
next(R5,R6).

PROBLEM 57 [MÁRKUSZ, 1978]
Verbal statement:
Write a program for designing an architectural unit obeying to the following specifications:

- Two rectangular rooms.
- Each room has a window and interior door.
- Rooms are connected by interior door.
- One room also has an exterior door.
- A wall can have only one door or window.
- No window can face north.
- Windows cannot be on opposite sides of the unit.
Logic Program:

\[ \text{plan}(FD,D1,W1,D2,W2) :- \text{frontroom}(FD,D1,W1), \]
\[ \text{opposite}(D1,D2), \]
\[ \text{room}(D2,W2), \]
\[ \text{notopposite}(W1,W2). \]

\[ \text{frontroom}(FD,D,W) :- \text{room}(D,W), \]
\[ \text{direction}(FD), \]
\[ \text{FD} = \neg = \neg W. \]

\[ \text{room}(D,W) :- \text{direction}(D), \]
\[ \text{direction}(W), \]
\[ D = \neg W, W = \neg \text{north}. \]

\[ \text{direction(north)}, \]
\[ \text{direction(south)}, \]
\[ \text{direction(east)}, \]
\[ \text{direction(west)}, \]

\[ \text{opposite(north,south)}, \]
\[ \text{opposite(south,north)}, \]
\[ \text{opposite(east,west)}, \]
\[ \text{opposite(west,east)}. \]

\[ \text{notopposite}(D1,D2) :- \text{opposite}(D1,D3), \]
\[ D2 = \neg = D3. \]

Execution:
Planning a unit entered from the west:

?-plan(west,D1,W1,D2,W2).

D1 = east,
W1 = south,
D2 = west,
W2 = south

PROBLEM 58  [PEREIRA & PORTO, 1980]

Verbal statement:

Write the following query:

"Is there a student such that a professor teaches him two different courses in the same room?"

for a data base of students who take courses, professors who teach courses, and courses held on certain weekdays and rooms.

Logic program:

query(S,P):- student(S,C1),
course(C1,D1,R),
professor(P,C1),
student(S,C2),
course(C2,D2,R),
professor(P,C2), C1 \= C2.

student(robert,prolog).
student(john,music).
student(john,prolog).
student(john,surf).
student(mary,science).
student(mary,art).
student(mary,physics).

professor(luis,prolog).
professor(luis,surf).
professor(antonio,prolog).
professor(eureka,music).
professor(eureka,art).
professor(eureka,science).
professor(eureka,physics).

course(prolog,monday,room1).
course(prolog,friday,room1).
course(surf,sunday,beach).
course(maths,tuesday,room1).
course(maths,friday,room2).
course(science, thursday, room1).
course(science, friday, room2).
course(art, tuesday, room1).
course(physics, thursday, room3).
course(physics, saturday, room2).

PROBLEM 59  [DARVAS et al, 1978]

Verbal statement:

Write a data base for predicting drug interactions.

Logic program:

/* Facts about chemistry */
contains(Procaine, amino_group).
base(X) :- contains(X, amino_group).

/* Data on various drugs */
inredient(aspirin, salicylic acid).
inredient(whisky, ethanol).

/* General rules about drug interactions */
interaction(Drug1, Drug2,
increased_absorption_by_ion_pair_formation(Agent1, Agent2)) :-
inredient(Drug1, Agent1),
inredient(Drug2, Agent2),
quaternary_ammonium_salt(Agent1),
anti_arrhythmic(Agent1),
salicylate(Agent2).

Execution:

?- interaction(aspirin, whisky, What).
3.3 PROBLEM SOLVING (nos. 60 to 65)

PROBLEM 60 [WARREN, 1975b]

Verbal statement:

Write a program that receives a scenery as input and produces an interpretation of the scenery as output.

Consider a scenery composed by a certain disposition of solids. The input for the program is a description of the solids in terms of their edges, and the output will be an interpretation in terms of what solids constitute the scenery and how are their faces.

Consider only vertical edges, positive and negative slope edges, and that a face may be left, right or horizontal.

Apply your program to the scenery:

![Diagram of scenery with numbered edges and faces](image)

Figure 2

Where the edges and the faces are numbered (E1,...,E35 and R1,...,R13, respectively) in an arbitrary order.
Suggestion: 1) When defining the scenario begin by the edges that limit it, that is, begin by the frontier edges.

2) Define a set of rules characterizing the different kinds of edges in terms of convexity or concavity of the regions they establish.

3) Label the contour edges clockwise.

Logic program:

:- op(500,xfy,';').
:- op(300,xfy,':').

goal:- solution(X),nl,nl,write(X),nl,nl.

/* Set of interpretation rules */

vertical_edge(left:B,right:B,positive).
vertical_edge(left:B1,right:B2,positive).
vertical_edge(right:B,X,down).
vertical_edge(X,left:B,up).

positive_edge(horizonal:B,right:B,positive).
positive_edge(right:B1,horizontal:B2,positive).
positive_edge(X,horizontal:B,up).
positive_edge(right:B,X,down).

negative_edge(left:B,horizontal:B,positive).
negative_edge(horizontal:B1,left:B2,positive).
negative_edge(horizontal:B,X,down).
negative_edge(X,left:B,up).

/* Defining the scenario */

solution(R1;R2;R3;R4;R5;R6;R7;R8;R9;R10;R11;R12;R13):-
  positive_edge(background,R1,E1),
  negative_edge(background,R1,E2),
  positive_edge(background,R2,E3),
  negative_edge(background,R2,E4),
  vertical_edge(R9,background,E5),
  positive_edge(R9,background,E6),
  vertical_edge(R12,background,E7),
  positive_edge(R12,background,E8),
  negative_edge(background,R13,E9),
  vertical_edge(background,R13,E10),
  positive_edge(background,R10,E11),
  vertical_edge(background,R3,E12),
  negative_edge(R3,R1,E13),
  positive_edge(R1,R4,E14),
  negative_edge(R6,R1,E15),
  positive_edge(R1,R7,E16),
  negative_edge(R8,R2,E17),
  positive_edge(R2,R9,E18),
  vertical_edge(R3,R4,E19),
positive_edge(R4,R5,E20),
vertical_edge(R4,R6,E21),
negative_edge(R5,R6,E22),
vertical_edge(R6,R7,E23),
negative_edge(R3,R5,E24),
vertical_edge(R3,R7,E25),
positive_edge(R5,R7,E26),
vertical_edge(R8,R9,E27),
negative_edge(R10,R3,E28),
negative_edge(R13,R10,E29),
positive_edge(R7,R11,E30),
negative_edge(R11,R8,E31),
vertical_edge(R7,R8,E32),
negative_edge(R13,R11,E33),
vertical_edge(R13,R12,E34),
positive_edge(R11,R12,E35).

Execution:
:-soal.

horizontal:X1; horizontal:X2; left:X1; right:X1;
horizontal:X1; left:X1; right:X1; left:X2;
right:X2; horizontal:X3; horizontal:X3; right:X3;
left:X3

this interpretation corresponds to the scenery:
**PROBLEM 61  [ROUSSEL,1975]**

**Verbal statement:**

There are three pegs, A, B, and C, and three disks of different sizes a, b, and c. The disks have holes in their centers so that they can be stacked on the pegs.

Initially all the disks are on peg A; the largest, disk c, is on the bottom, and the smallest, disk a, is on the top.

It is desired to transfer all of the disks to peg C by moving disks one at a time. Only the top disk on a peg can be moved, but it can never be placed on top of a smaller disk (Tower-of-Hanoi puzzle).

**Logic program:**

```haskell
hanoi(N) :- hanoi(N,L,[]), nl, write(L), nl.

hanoi(N) --> put(N,a,b,c).

put(0,-,-,-) --> [].
put(N,A,B,C) --> {M is N-1},
                  put(M,A,C,B), move(A,B), put(M,C,B,A).

move(X,Y) --> [from,X,to,Y].
```

**PROBLEM 62  [EMDEN,1978]**

**Verbal statement:**

Consider the abstract game of Mastermind with 6 colours and 4 places to combine them. Consider that, in the score, a black key peg means strong match (right colour in a right place) and a white key peg means weak match (right colour in a wrong place). Write a program able to perform the Codemaker when you play the Codebreaker and vice-versa.

**Suggestion:** Consider that the Codebreaker constructs a sequence $p_1, \ldots, p_n$ of probes with $p_i \neq C$ for $i \neq n$ and $p_n = C$, where $C$ means the key code. The Codemaker constructs a sequence $s_1, \ldots, s_n$ such that $s_i = f(p_i, C)$ where $f$ is the score function. The selection of $p_i$ by the Codebreaker may depend on $(p_1, s_1), \ldots, (p_{i-1}, s_{i-1})$. It is the Codebreaker's objective to make $n$ as small as possible.
Logic Program

/* Program for the Mastermind game */
:- op(300,xfy,',').
:- op(150,xfy,'s').

/* Interactive manager */

play :- write('Mastermind at your service.'), nl,
        write('Enter an arbitrary number between 0 and 164.'), nl,
        read(X), assert(seed(X)),
        write('Example format for entering code: '), nl,
        write(['[yellow]blue,white,black']['), nl,
        write('Example format for the score: '), nl,
        write(['s s s 0,s 0'], nl,
        write('Meaning 3 blacks and 1 white.'), nl,
        repeat, play1.

play1 :- write('Do you want to make or to break codes?'), nl,
        write('Answer make or answer break.'), nl,
        read(X), start(X).

ask :- write('Do you want another game?'), nl,
       write('Answer yes or answer no.'), nl,
       read(X), answer(X).

answer(yes) :- !, fail.
answer(no) :- retract(seed(_)), nl,
             write('Mastermind was pleased to serve you.'), nl, nl.

/* User performs the Codemaker */

start(make) :- write('Enter code: I promise not to look.'), nl,
              read(C), assert(code(C)),
              generate_code(P), score(P,S),
              write('My first probe is: '), write(P), nl,
              write('Score: '), write(S), nl,
              extendable([P,S],[],s s s s 0),
              retract(code(_)), !, ask.

extendable((P,[s s s s _]),...):- write('The code must be! '),
                              write(P), nl.

extendable(Cs,Ns):- can_code(Cs,Cc),
                   write('My next probe is! '), write(Cc), nl,
                   write('Score: '), score(Cc,S), write(S), nl,
                   extendable((Cc,S),Cs,Ns).

can_code([],_).
can_code([P1,S1],Ps,P):- mm(P1,P,S1), can_code(Ps,P).
/* User performs the Codebreaker */

start(break):- generate_code(C), assert(code(C)),
       write('Enter first probe: '), nl,
       read(P), score(P,S), continue_break(S), !, ask.

continue_break(s s s s ...):- write('You got it: '), nl,
                   retract(code(_)).

continue_break(S):- write('Your score: '), write(S), nl,
                    write('Enter next probe or type stop: '), nl,
                    read(X), respond_to(X).

respond_to(stop):- !, write('I assume you give up!'),
                   write('the code is: '),
                   retract(code(C)), write(C), nl.

respond_to(P):- score(P,S), continue_break(S).

/* Score function */

score(Probe,Score):- code(C), mm(Probe,C,Score).

mm(P,C,S1,S2,[[]]:- blacks(P,C,P1,C1,S1),
          whites(P1,C1,S2,C1).

blacks([],[],[],[],[]):.
blacks(U,P,U,C,P1,C1,S)- blacks(P,C,P1,C1,S),
blacks(U,P,V,C,U,P1,V,C1,S):- diff(U,V),
                              blacks(P,C,P1,C1,S).

whites([],C,[],[],[]): tuple(C,M).
whites(U,P,C,S,S1,M1,Ms)- del(U,C,C1,Ms),
                         whites(P,C1,S1,Ms1).
whites(U,P,C,S,Ms):- nonmem(U,C,Ms), whites(P,C,S,Ms).

/* Code generator */

generate_code(U,V,W,X,[[]):- random_colour(U),
                      random_colour(V),
                      random_colour(W),
                      random_colour(X).

random_colour(X):- random_number(R), N is R mod 6,
                  N1 is N+1, colour(N1,X).

random_number(R1):- retract(seed(R)), X is R*125,
                    Y is X+1, R1 is Y mod 165,
                    assert(seed(R1)).

colour(1,black),
colour(2,blue),
colour(3,green),
colour(4,red),
colour(5,white),
colour(6,yellow).
/** Miscellaneous */

/* del(U,Y,Y1) is the result of deleting U from list Y */

del(U,Y,Y,Y,Ms):- tuple(Y,Ms).
del(U,Y,Y,Y1,Ms1,Ms):- diff(U,Y), del(U,Y,Y1,Ms).

/* nonmem(U,V) if U is not a member of list V */

nonmem(_,[],[]),
nonmem(U,V1,V,W):- diff(U,V1), nonmem(U,V,W).

tuple([],[]),
tuple(U1,U,V1,V):- colour(_,U1), tuple(U,V).
diff(C1,C2):- colour(_,C1), colour(_,C2), not(C1=C2).

Execution:

:- play.
Mastermind at your service.
Enter an arbitrary number between 0 and 164.
: 123.
Example format for entering code: [yellow,blue,white,black]
Example format for the score: [s s s 0, r 0]
Meaning 3 blacks and 1 white.
Do you want to make or to break codes?
Answer make or answer break.
: make.
Enter code; I promise not to look.
: [blue,white,blue,white].
My first probe is: [blue,red,blue,black]
Score: [s s 0,0]
My next probe is: [blue,red,green,green]
Score: [s 0,0]
My next probe is: [blue,black,black,black]
Score: [s 0,0]
My next probe is: [blue,blue,blue,blue]
Score: [s s 0,0]
My next probe is: [blue,white,blue,white]
Score: [s s s 0,0]
The code must be: [blue,white,blue,white]
Do you want another game?
Answer yes or answer no.
: yes.
Do you want to make or to break codes?
Answer make or answer break.
: break.
Enter first probe.
: [blue,blue,red,red].
Your score: [0,0,0]
Enter next probe or type stop.
: [white,white,white,white].
Your score: [s s 0,0]
Enter next probe or type stop.
; [white,white,blue,black].
Your score : [s s 0 s 0]
Enter next probe or type stop.
; [white,white,green,blue].
Your score : [s 0 s 0]
Enter next probe or type stop.
; [white,red,white,black].
You got it.
Do you want another game?
Answer yes or answer no.
; no.

Mastermind was pleased to serve you.

PROBLEM 63 [BRUYNNOGHE, 1978]

Verbal statement:

Write a program to solve the n-queens problem (where n=4).

Consider a chess table 4x4 and put four queens on it, obeying to the condition that each of them cannot attack any of the others.

Suggestion: Consider the following representation of the chess table where each square is '$p$ (number of line, number of column)'.

```
  4 3 2 1
 4 0 0 0 0
 3 0 0 0 0
 2 0 0 0 0
 1 0 0 0 0
```

Figure 4

Logic Program 1:

```
begin:- perm([4,3,2,1],L),pair([4,3,2,1],L,R),
safe(R),write(R),nl,nl.
/* Generator of permutations */
perm([],[]).
perm([X|Y],[U|V]) :- del(U,[X|Y],W),perm(W,V).
del(X,[X|Y],Y),
del(U,[X|Y],[X|V]) :- del(U,Y,V).
```
/* Pairing lines with columns */

pair([],[],[]).
pair([X;Y],[U;V],[P(X,U);W]):- pair(Y,V,W).

/* Check if the queen positions are compatible */
safe([]),
safe([P;Q]):- check(P,Q), safe(Q),
check([P;[]]),
check([P,[],R]):- diag(P,Q), check(P,R).

/* non-attacking condition on diagonals */
diag([P(X1,Y1),P(X2,Y2)]:- Dy is Y1-Y2,  
   Dx is X1-X2, 
   Dy =\= Dy,  
   Dx =\= -Dy.

Logic program 2: (more efficient version)

queens(L,[C1;RC],R):- del(L,L,RL), safe([L1,C1],R),
   queens(RL,RC,[P(L1,C1);R]),
queens([],[],R).

Execution:
:-queens([1,2,3,4],[1,2,3,4],[]).

PROBLEM 64

Verbal statement:

Three missionaries and three cannibals seek to cross a river. A boat is available which holds two people, and which can be navigated by any combination of missionaries and cannibals involving one or two people. If the missionaries on either bank of the river, or 'en route' in the river, are outnumbered at any time by the cannibals, the cannibals will indulge their anthropophagic tendencies and do away with the missionaries. Find the simplest schedule of crossings that will permit all the missionaries and cannibals to cross the river safely.

Suggestion: Consider the representation of the left side of the river (for example) as s(M,C,B) where M is the number of missionaries, C is the number of cannibals, and B takes the value 0 or 1 accordingly with the position of the boat (left side or right side respectively).
Logic program:
:- or(300,xfy,=》).

plan:- movements(s(3,3,1),P),print(P).

movements(s(0,0,0),done).
movements(X,Y=G=Y=G,Z):- move(X,Y),move_back(Y,Y1),
                           test(X,Y1),
                           movements(Y1,Z).
move(X,Y):- move(X,Y,2);move(X,Y,1);move11(X,Y).
move_back(s(0,0,0),s(0,0,0)).
move_back(X,Y):- move_back(X,Y,2);move_back(X,Y,1);
               moveback11(X,Y).

move(s(M,C,X),s(M1,C,Y),N):- (M=N ;
                                M>N, M-N>C),
                               M1 is M-N, M1=<3,
                               Y is 1-X.
move(s(M,C,X),s(M,C1,Y),N):- C>=N, C1 is C-N,
                        C1=<3, Y is 1-X.
move11(s(M,C,X),s(M1,C1,Y)):- M>=1, C>=1,
                       M1 is M-1, C1 is C-1,
                       Y is 1-X.
move_back(s(M,C,X),s(M1,C,Y),N):- N=<3-M, M+N=C,
                     M1 is M+N, Y is 1-X.
move_back(s(M,C,X),s(M,C1,Y),N):- N=<3-C,
                          (M=0 ; M>=C+N),
                         C1 is C+N, Y is 1-X.
move_back11(s(M,C,X),s(M1,C1,Y)):- M>=1, C>=1,
                      M1 is M+1, C1 is C+1,
                      Y is 1-X.

test(s(M,C,_),s(M,C,_)):- !,fail.
test(_,_).

print(X=G=Y):- write(X),nl,print(Y).
print(X):- nl,write(X),nl.

Execution:
:- plan.
s(3,3,1)
s(3,1,0)
s(3,2,1)

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s(3,0,0)
s(3,1,1)
s(1,1,0)
s(2,2,1)
s(0,2,0)
s(0,3,1)
s(0,1,0)
s(0,2,1)
s(0,0,0)
done

PROBLEM 65 [EMDEN, 1980]

Verbal statement:

Write a program for the game of Nim defined as follows.

A position of the game of Nim can be visualized as a set of heaps of matches. Two players, called US and THEM, alternate making a move. As soon as a player, whose turn it is to move, is unable to make a move, the game is over and that player has lost; the other player is said to have won. A move consists of taking at least one match from exactly one heap.

Logic program:

:- op(300,xf,+).

s(X,Y):- move(X,Y), not(t(Y,Z)).
t(X,Y):- move(X,Y), not(s(Y,Z)).

append([],Y,Y).
append([U|X],Y,[U|Z]):- append(X,Y,Z).

move(X,Y):- append(U,[X1:V],X),
            takesome(X1,X2),
            append(U,[X2:V],Y).

takesome(X,Y).
takesome(X,Y):- takesome(X,Y).
3.4 THEOREM PROVING (nos. 66 to 70)

PROBLEM 66

Verbal statement:

Write a simple Propositional Calculus Theorem Prover, covering equivalence, implication, disjunction, conjunction and negation.

Logic program:

/* Propositional Calculus Theorem Prover */

:-op(700,xfy,eqv). /* equivalence */
:-op(650,xfy,imp). /* implication */
:-op(600,xfy,or). /* disjunction */
:-op(550,xfy,and). /* conjunction */
:-op(500,xfy,not). /* negation */

formulas:- repeat,read(T), ( T==stop ; theorem(T), fail ).

theorem(T):- ttynl,
    ( false(T), display('not valid')!,
    display('valid')
    ),
    ttynl,ttynl.

false( 'FALSE' ):!.
false( not 'TRUE' ):!.
false( P eqv Q ):-false(( P imp Q ) and ( Q imp P )).
false( P imp Q ):false( not P or Q ).
false( P or Q ):false( P ),false( Q ).
false( P and Q ):false( P );false( Q ).
false( not not P ):false( P ).
false( not(P eqv Q)):-false( not(P imp Q) or not(Q imp P)).
false( not(P imp Q)):-false( not(not P or Q)).
false( not(P or Q)):-false( not P and not Q).
false( not(P and Q)):-false( not P or not Q).

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PROBLEM 67

Verbal statement:

Program Wand’s algorithm for proving theorems of propositional calculus.

The Wand’s algorithm consists of writing down a series of lines, each simpler than the previous one, until a proof is completed -- or shown to be impossible. Each line consists of any number of wff’s, separated by commas, on each side of an arrow.

Wand’s algorithm:

1. As the first line, write the premises to the left of the arrow and the theorem to the right of the arrow:
   \[ \text{premise}_1, \text{premise}_2, \text{premise}_3 \rightarrow \text{theorem} \]

2. If the principal connective of a wff is a negation, drop the negation sign and move the wff to the other side of the arrow; for example,
   \[ \neg (S \vee R) \rightarrow Q, \neg P \]
   is changed into
   \[ S \vee R, P \rightarrow \neg Q, \neg \neg P \]

3. If the principal connective of a wff on the left of the arrow is \( \land \) or on the right of the arrow is \( \lor \), replace the connective by a comma; for example,
   \[ \neg (Q \lor R \land S) \rightarrow \neg P \]
   is changed into
   \[ \neg Q, \neg R, \neg S \rightarrow \neg P \]

4. If the principal connective of a wff on the left of the arrow is \( \lor \) or that on the right of the arrow is \( \land \), then produce two new lines, each with one of the two sub-wff’s replacing the wff; for example,
   \[ \neg Q \lor R \land S \rightarrow \neg Q, \neg R, S \]
   \[ \neg Q \lor R \rightarrow \neg Q, \neg R \]
   All the resulting lines must be proved in order to prove the original theorem.
5. If the same wff occurs on both sides of an arrow, the line is proved.

6. If no connectives remain in a line and no propositional variable occurs on both sides of the arrow, the line is not provable. In fact, assigning all the variables on the left to be TRUE and all the variables on the right to be FALSE will provide an example of the falsity of the theorem.

Logic program:

```/* Operations */
:- op(700,xy<=>), /* equivalence */
:- op(650,xy=>), /* implication */
:- op(600,xy\lor), /* disjunction */
:- op(550,xy\&), /* conjunction */
:- op(500,xy,-), /* negation */

/* Read in and try to prove formula: */
write('valid or' not valid' accordingly */

formulas:- repeat,write('Formula:'),nl,
          read(T), (T=stop;theorem(T),fail).

theorem(T):- nl,nl,
           (prove([],[]],[],[T]),!,nl,
           write('Formula is valid');
           nl,write('Formula is not valid'),nl,nl.

prove(T):- write(' prove,'),nl,write(T),nl,nl,
          prove(T).

prove(E1):- rule(E1,E2,Rule),!,
           write(E2),by_rule(Rule),nl,
           prove(E2).

/* Case for \lor on l.h.s. */

prove(L & [H\lor I:T] => R):- !,
                           first_branch,prove(L & [H:T] => R),
                           branch_proved;
                           second_branch,prove(L & [I:T] => R),
                           branch_proved.

/* Case for \& on r.h.s. */

prove(L => R & [H \& I:T]):- !,
                           first_branch, prove(L => R & [H:T]),
                           branch_proved;
                           second_branch, prove(L => R & [I:T]),
                           branch_proved.

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/* Case for atom */
prove(L & [H;T] => R):- !,prove([H;L] & T => R).
prove(L => R & [H;T]):- !,prove(L => [H;R]& T).

/* Finally, check whether tautology */
prove(T):- tautology(T),write('Tautology,'),nl,
prove(_):- write('This branch is not provable.'),fail.

/* Cases where => appears in one of the sides */
rule(L & [H => I;T] => R,
     L & [-H V I;T] => R, rule_5).
rule(L => R & [H => I;T],
     L => R & [-H V I;T],rule_6).

/* Cases where <= appears in one of the sides */
rule(L & [H <= I;T] => R,
     L & [(H => I)&(I => H);T] => R, rule_7).
rule(L => R & [H <= I;T],
     L => R & [(H => I) & (I => H);T],rule_8).

/* Cases where - appears */
rule(L & [-H;T] => R & R2,
     L & T => R & [H;R2],rule_2).
rule(L1 & L2 => R & [-H & T],
     L1 & [H;L2] => R & T,rule_2).

/* Case for & on l.h.s. */
rule(L & [H & I;T] => R,
     L & [H;I;T] => R,rule_3).

/* Case for V on r.h.s. */
rule(L => R & [H V I ;T],
     L => R & [H;I;T],rule_3).

tautology(L & []) => R & [] :- member(H,L),
                         member(M,R),
branch_proved:write('This branch has been proved.'),nl.
first_branch:- nl,write('First branch:').
second_branch:- nl,write('Second branch:').
by_rule(R):- write('by'),write(R),nl,nl.
member(H,[H;_]),
member(I,[I;T]) :- member(I;T).

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Execution:

Formula:

\[ a \Rightarrow a. \]

\([\ ] \& [\ ] \Rightarrow [\ ] \& [-a \lor a] \quad \text{by rule}_6 \)

\([\ ] \& [\ ] \Rightarrow [\ ] \& [-a,a] \quad \text{by rule}_3 \)

\([\ ] \& [a] \Rightarrow [\ ] \& [a] \quad \text{by rule}_2 \)

Tautology

Formula is valid

Formula:

\((a \Rightarrow b) \& (b \Rightarrow c) \Rightarrow (a \Rightarrow c),\)

\([\ ] \& [\ ] \Rightarrow [\ ] \& [-((a \Rightarrow b) \& (b \Rightarrow c)) \lor (a \Rightarrow c)] \quad \text{by rule}_6 \)

\([\ ] \& [\ ] \Rightarrow [\ ] \& [-((a \Rightarrow b) \& (b \Rightarrow c)),a \Rightarrow c] \quad \text{by rule}_3 \)

\([\ ] \& [(a \Rightarrow b) \& (b \Rightarrow c)] \Rightarrow [\ ] \& [a \Rightarrow c] \quad \text{by rule}_2 \)

\([\ ] \& [(a \Rightarrow b) \& (b \Rightarrow c)] \Rightarrow [\ ] \& [-a \lor c] \quad \text{by rule}_6 \)

\([\ ] \& [a \Rightarrow b,b \Rightarrow c] \Rightarrow [\ ] \& [-a \lor c] \quad \text{by rule}_3 \)

\([\ ] \& [-a \lor b,b \Rightarrow c] \Rightarrow [\ ] \& [-a \lor c] \quad \text{by rule}_5 \)

\([\ ] \& [-a \lor b,b \Rightarrow c] \Rightarrow [\ ] \& [-a,c] \quad \text{by rule}_3 \)

\([\ ] \& [a,-a \lor b,b \Rightarrow c] \Rightarrow [\ ] \& [c] \quad \text{by rule}_2 \)

First branch: prove,

\([a] \& [-a,b \Rightarrow c] \Rightarrow [\ ] \& [c] \quad \text{by rule}_2 \)

\([a] \& [b \Rightarrow c] \Rightarrow [\ ] \& [a,c] \quad \text{by rule}_2 \)

\([a] \& [-b \lor c] \Rightarrow [\ ] \& [a,c] \quad \text{by rule}_5 \)

First branch: prove,

\([a] \& [-b] \Rightarrow [\ ] \& [a,c] \quad \text{by rule}_2 \)

\([a] \& [\ ] \Rightarrow [\ ] \& [b,a,c] \quad \text{by rule}_2 \)

Tautology.

This branch has been proved.
Second branch : prove,
[a] & [c] => [] & [a,c]
Tautology.
This branch has been proved.
Second branch : prove,
[a] & [b,b => c] => [] & [c]
[b,a] & [-b v c] => [] & [c] by rule_5
First branch : prove,
[b,a] & [-b] => [] & [c]
[b,a] & [] => [] & [b,c] by rule_2
Tautology.
This branch has been proved.
Second branch : prove,
[b,a] & [c] => [] & [c]
Tautology.
This branch has been proved.
Formula is valid.

Formula:
(a => b) <=> (-a v b)
[[]] & [()] & [((a=>b)=>-a V b) & (-a V b=>a=>b)] by rule_8
First branch : prove,
[[]] & [()] => [] & [(a => b) => -a V b]
[[]] & [()] => [] & [-(a => b) V -a V b] by rule_6
[[]] & [()] => [] & [-(a => b), -a V b] by rule_3
[[]] & [a => b] => [] & [-a V b] by rule_2
[[]] & [-a V b] => [] & [-(a V b)] by rule_3
[[]] & [-a V b] => [] & [-a, b] by rule_3

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\[ \{ \} \land \{ a, -a \land V \ b \} \rightarrow \{ \} \land \{ b \} \]

First branch: prove,

\[ \{ a \} \land \{ -a \} \rightarrow \{ \} \land \{ b \} \]

\[ \{ a \} \land \{ \} \rightarrow \{ \} \land \{ a, b \} \]

Tautology.

This branch has been proved.

Second branch: prove,

\[ \{ a \} \land \{ b \} \rightarrow \{ \} \land \{ b \} \]

Tautology.

This branch has been proved.

Second branch: prove,

\[ \{ \} \land \{ \} \rightarrow \{ \} \land \{ -a \land V \ b \rightarrow a \rightarrow b \} \]

\[ \{ \} \land \{ \} \rightarrow \{ \} \land \{ -(a \land V \ b) \lor (a \rightarrow b) \} \]

\[ \{ \} \land \{ \} \rightarrow \{ \} \land \{ -(a \land V \ b), a \rightarrow b \} \]

\[ \{ \} \land \{ -a \land V \ b \} \rightarrow \{ \} \land \{ a \rightarrow b \} \]

\[ \{ \} \land \{ -a \land V \ b \} \rightarrow \{ \} \land \{ -a \land V \ b \} \]

\[ \{ \} \land \{ -a \land V \ b \} \rightarrow \{ \} \land \{ -a, b \} \]

\[ \{ \} \land \{ a, -a \land V \ b \} \rightarrow \{ \} \land \{ b \} \]

First branch: prove,

\[ \{ a \} \land \{ -a \} \rightarrow \{ \} \land \{ b \} \]

\[ \{ a \} \land \{ \} \rightarrow \{ \} \land \{ a, b \} \]

Tautology.

This branch has been proved.

Second branch: prove,

\[ \{ a \} \land \{ b \} \rightarrow \{ \} \land \{ b \} \]

Tautology.

This branch has been proved.

Formula is valid.
PROBLEM 68

Verbal statement:

The facts:

The maid said that she saw the butler in the living room.
The living room adjoins the kitchen.
The shot was fired in the kitchen, and could be heard in all nearby rooms.
The butler, who had good hearing, said he did not hear the shot.

To prove:

If the maid told the truth, the butler lied.

Logic program:

Use the previous program for Wand’s algorithm.

Execution:

Use the following representation:

\( p \) = The maid told the truth
\( q \) = The butler was in the living room
\( r \) = The butler was near the kitchen
\( s \) = The butler heard the shot
\( u \) = The butler told the truth

The premises are written:

\[-p \lor q \quad \text{(If the maid told the truth, the butler was in the living room.)}\]

\[-q \lor r \quad \text{(If the butler was in the living room, he was near the kitchen.)}\]

\[-r \lor s \quad \text{(If he was near the kitchen, he heard the shot.)}\]

\[-u \lor \neg s \quad \text{(If he told the truth, he did not hear the shot.)}\]

The theorem is written:

\[-p \lor \neg u \quad \text{(If the maid told the truth, the butler did not.)}\]
The formula input to the program is:

\((-p \lor a) \& (-a \lor r) \& (-r \lor s) \& (-u \lor s) \Rightarrow (-p \lor -u)\)

**Problem 69**

**Verbal statement:**

The facts:

The following chemical equations:

\[
\begin{align*}
\text{MgO} + \text{H}_2 & \Rightarrow \text{Mg} + \text{H}_2\text{O} \\
\text{C} + \text{O}_2 & \Rightarrow \text{CO}_2 \\
\text{CO}_2 + \text{H}_2\text{O} & \Rightarrow \text{H}_2\text{CO}_3
\end{align*}
\]

The existing components:

MgO, H2, O2 and C

To prove:

It is possible to compose H2CO3.

**Logic program:**

Use any of the previous Propositional Calculus theorem provers.

**Execution:**

The premises are written:

\[
\begin{align*}
(MgO \& H2) \Rightarrow (Mg \& H2O) \\
(C \& O2) \Rightarrow CO2 \\
(CO2 \& H2O) \Rightarrow H2CO3
\end{align*}
\]

The theorem is written:

\[
\begin{align*}
& ((MgO \& H2) \Rightarrow (Mg \& H2O)) \\
& \& ((C \& O2) \Rightarrow CO2) \\
& \& ((CO2 \& H2O) \Rightarrow H2CO3) \& MgO \& H2 \& O2 \& C) \Rightarrow H2CO3
\end{align*}
\]
**Problem 70 [EMDEN, 1976a]**

**Verbal statement:**

Consider a machine defined as a set of commands, each of which is a binary relation over some supposedly given set of states.

In the set notation for the commands of this example, the variables $u, v, w, u', v', w'$ are considered to range over the rational numbers.

The set of states: $\{ (u, v, w) \} \cup \{ (u, v) \} \cup \{ (w) \}$

The commands: (Figure 5)

<table>
<thead>
<tr>
<th>set notation for command</th>
<th>&quot;Algol&quot; notation for command</th>
</tr>
</thead>
<tbody>
<tr>
<td>$((u, v, w), u, v', w')$: $v'=v-1 \land w'=u \times w$</td>
<td>$v, w := v-1, u \times w$</td>
</tr>
<tr>
<td>$((u, v, w), u', v', w): u'=u \times u \land v'=v/2$</td>
<td>$u, v := u \times u, v/2$</td>
</tr>
<tr>
<td>(E.W. Dijkstra's &quot;parallel assignment&quot;)</td>
<td></td>
</tr>
<tr>
<td>$((u, v), (u, v, l))$</td>
<td></td>
</tr>
<tr>
<td>(&quot;initializing declaration&quot;)</td>
<td></td>
</tr>
<tr>
<td>$((u, v, w), (w))$</td>
<td></td>
</tr>
<tr>
<td>(&quot;undeclaration&quot;)</td>
<td></td>
</tr>
<tr>
<td>$((u, 0, w), (u, 0, w))$</td>
<td></td>
</tr>
<tr>
<td>$((u, v, w), (u, v, w))$: $\neg v=0$</td>
<td>$\neg v=0$</td>
</tr>
<tr>
<td>(&quot;guard&quot;)</td>
<td></td>
</tr>
<tr>
<td>$((u, v, w), u', v', w): even(v) \land u'=u \times u \land v'=v/2$</td>
<td>even(v); $u, v := u \times u, v/2$</td>
</tr>
<tr>
<td>$((u, 0, w), (w))$</td>
<td></td>
</tr>
<tr>
<td>(&quot;guarded command&quot;)</td>
<td></td>
</tr>
</tbody>
</table>

Figure 5

The machine: some set closed under product containing the above commands

The program schema =

\[
(\text{nonterminals}: \{ S, P, R \})
\]

\[
(\text{terminals}: \{ W1, VO, UV, VW \})
\]

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\textbf{Productions:}

\begin{quote}
\begin{itemize}
\item \texttt{S} \rightarrow \texttt{W1} \texttt{P}
\item \texttt{P} \rightarrow \texttt{VO}
\item \texttt{P} \rightarrow \texttt{UV} \texttt{P}
\item \texttt{P} \rightarrow \texttt{VW} \texttt{P}
\end{itemize}
\end{quote}

\textbf{Start symbol:} \texttt{S}

\textbf{The program is obtained by the following identifications:}

\begin{quote}
\begin{itemize}
\item \texttt{W1} = (\texttt{real w1=1})
\item \texttt{VO} = (v=0; \texttt{uand u,v})
\item \texttt{UV} = (even(v); u,v:=u \times u,v/2)
\item \texttt{VW} = (v,w:=v-1,u \times w)
\end{itemize}
\end{quote}

\textbf{Some 'computations':} (Figure 6)

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|}
\hline
\textbf{i} & \textbf{\textit{t}_i} & \textbf{\textit{x}_i} & \textbf{\textit{t}_i} & \textbf{\textit{x}_i} & \textbf{\textit{t}_i} & \textbf{\textit{x}_i} \\
\hline
0  & --   & (2,10)  & --   & (2,10)  & --   & (2,10)  \\
1  & W1   & (2,10,1) & W1   & (2,10,1) & W1   & (2,10,1) \\
2  & UV   & (4,5,1)  & UV   & (4,5,1)  & UV   & (4,5,1)  \\
3  & WW   & (4,4,4)  & WW   & (4,4,4)  & WW   & (4,4,4)  \\
4  & UV   & (16,2,4) & UV   & (16,2,4) & UV   & (16,2,4) \\
5  & UV   & (256,1,4) & VW   & (16,1,64) & WW   & (16,1,64) \\
6  & VW   & (256,0,1024) & VW   & (16,0,1024) & WW   & (16,0,1024) \\
7  & VO   & (1024) & VO   & (1024)   & VW   & (16,-1,2-14) \\
8  &     &         &     &         & VW   & (16,-1,2-18) \\
\hline
\end{tabular}
\caption{Figure 6}
\end{table}

Two representations of this machine, the flowgraph (Figure 7) and the flowdiagram (Figure 8), are given.
Write a program implementing this machine.

Logic program:
\[ :- op(600, yfx, ', '). \]

\[ s(X) :- w1(X,Y), p(Y,Z), write(Z), nl. \]

\[ p(X,Y) :- v0(X,Y). \]
\[ p(X,Z) :- uv(X,Y), p(Y,Z). \]
\[ p(X,Z) :- vw(X,Y), p(Y,Z). \]

\[ w1(U,V,U,V,1). \]
\[ v0(U,0,W,W). \]

\[ even(V) :- V1 \text{ is } V \mod 2, \ V1 \equiv 0. \]

\[ uv(U,V,W,U1,V1,W) :- even(V), \]
\[ \quad U1 \text{ is } U*U, \]
\[ \quad V1 \text{ is } V/2. \]

\[ vw(U,V,W,U,V1,W1) :- V1 \text{ is } V-1, \]
\[ \quad W1 \text{ is } U*W. \]

Execution:
\[ ?- s(2,10). \]
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3.5 PLANNING (nos. 71 to 79)

PROBLEM 71 [WARREN, 1974a]

Verbal statement:

Many problem domains can naturally be formalised as a world with
a set of actions which transform that world from one state to
another.

A particular problem is then specified by describing an initial
state and a desired goal state; the problem solver is required
to generate a plan, a simple sequence of actions which
transforms the world from the initial state to the goal state.

Write a problem solver (WARPLAN), independent from any
particular problem and able to generate a plan of actions (in
order to transform an initial state into a goal state) for each
data base (world description) you give it.

Logic program:

:- op(700,xfy, &).
:- op(650,yfx, =>).

/* Problem solver entry: Generation and output of a plan */
 plans(C,T):- not(consistent(C, true)), !, nl,
 write('impossible'),nl,nl.
 plans(C,T):- plan(C, true, T, T1), nl, output(T1), nl, nl.
 output(Xs => X):- !, output1(Xs), write(X), write(’,’), nl.
 output1(Xs => X):- !, output1(Xs), write(X), write(‘;’), nl.
 output1(X):- write(X), write(‘;’), nl.

/* Entry point to the main recursive loop */
 plan(X&C, P, T, T2):- !, solve(X, P, T, P1, T1) plan(C, P1, T1, T2).
 plan(X, P, T, T1):- solve(X, P, T, P1, T1).

/* Ways of solving a goal */
 solve(X, P, T, P, T):- always(X); X.
 solve(X, P, T, P1, T):- holds(X, T), and(X, P, P1).
 solve(X, P, T, X&P, T1):- add(X, U), achieve(X, U, P, T, T1).
/* Methods of achieving an action */
/* By extension */
achieve(X,U,P,T,T1=>U):- preserves(U,P),
    can(U,C),
    consistent(C,P),
    plan(C,P,T,T1),
    preserves(U,P).

/* By insertion */
achieve(X,U,P,T=>U,T1=>U):- preserved(X,U),
    retrace(P,V,P1),
    achieve(X,U,P1,T,T1),
    preserved(X,U).

/* Check if a fact holds in a certain state */
holds(X,T=>U):- add(X,U).
holds(X,T=>U):- !, preserved(X,U),
    holds(X,T),
    preserved(X,U).
holds(X,T):- given(T,X).

/* Prove that an action preserves a fact */
preserves(U,X&C):- preserved(X,U), preserves(U,C),
    preserves(_,true).
preserves(X,V):- numvars(X&V,0,N),
    del(X,V), !, fail.
preserves(_,true).

/* Retracing a goal already achieved */
retrace(P,V,P2):- can(V,C),
    retrace1(P,V,C,P1),
    append(C,P1,P2).
retrace1(X&P,V,C,P1):- add(Y,V), equiv(X,Y), !,
    retrace1(P,V,C,P1).
retrace1(X&P,V,C,P1):- elem(Y,C), equiv(X,Y), !,
    retrace1(P,V,C,P1).
retrace1(true,V,C,true).

/* Consistency with a goal already achieved */
consistent(C,P):- numvars(C&P,0,N),
    imp(S),
    not(not(intersect(C,S))),
    implied(S,C&P), !, fail.
consistent(_,_).
/* Utility routines */

and(X,P,P) :- elem(Y,P),equiv(X,Y),!
and(X,P,X&P).

append(X&P,P1):- !,append(C,F,P1),
append(X,F,X&P).

elem(X,Y&C):- elem(X,Y),
elem(X,Y&C):- !,elem(X,C),
elem(X,X).

implied(S1&S2,C):- !,implied(S1,C),implied(S2,C),
implied(X,C):- elem(X,C),
implied(X,C):- X.

intersect(S1,S2):- elem(X,S1),elem(X,S2).

not_equal(X,Y):- not(X=Y),
not(X='$VAR'(N)),
not(Y='$VAR'(N)).
equiv(X,Y):- not(nonequiv(X,Y)).
nonequiv(X,Y):- numbervars(X@Y,0,N),X=Y,!,fail.
nonequiv(_,_).

Remarks on the logical program :

0) Operators interpretation:

'X@Y' is 'X and Y'
'X==>Y' is 'the state after doing Y in X'

1) The central predicate is 'Plan(C,P,T,0)', it has 4 arguments:

C is a conjunction of goals to be solved;
T is a (already generated) partial plan;
P is a conjunction of goals already solved by T which must be protected;
T1 is a new plan, which contain T as a subplan and preserves the already solved goals P, and which also solves the new goals C.

Essentially this predicate states that a plan can be produced by 'solve'-ing each goal in the given order (C,P,T behave as input variables and T1 as output variable).
2) The predicate \( \text{solve}(X,P,T,P_1,T_1) \)' has the following arguments:

- \( X \) is an atomic goal;
- \( T \) is a partial plan;
- \( P \) is a conjunction of goals achieved by \( T \);
- \( T_1 \) is a plan, containing \( T \) as a sub-plan, which solves \( P_1 \);
- \( P_1 \) is a conjunction comprising \( P \) and \( X \), where \( X \) is not repeated.

There are three ways in which a goal may be 'solve'-d: It may be 'always' true in the world. It may be that it already 'holds' in the state produced by the current partial plan. Finally, we may look in the database for action \( U \) which 'add'-s the goal \( X \) and then 'solve' \( X \) by 'achieve'-ing \( U \) (\( X,P,T \) behave as input variables and \( P,T_1 \) as output variables).

3) The predicate \( \text{achieve}(X,U,P,T,T_1) \)' has two clauses corresponding to two methods of 'achieve'-ing an action: extension and insertion.

The clause for the extension method (the first one) checks that the action \( U \) 'preserves' (i.e., does not delete) the protected facts \( P \). Then we lookup the preconditions \( C \) in the database and check that \( C \) is consistent with the protected facts. All being well, we call 'plan' recursively to modify the current plan \( T \) to a new \( T_1 \) which produces a state in which \( C \) and \( P \) are attained. \( U \) can then be applied in \( T_1 \), corresponding to the plan resulting from this call of 'achieve'.

Finally, the check that \( U \) preserves \( P \) is repeated, for the reason that \( U \) and \( P \) may not have been instantiated to ground terms at the time of the original check.

The clause for the insertion method (the second one) follows the axiom: If the last action \( V \) in the current partial plan does not delete the current goal \( X \), we can try to insert the action \( U \) somewhere before \( V \), provided we retrace the set of protected facts to the point before \( V \).

4) \( \text{holds}(X,Y) \)' follows the method: everything that 'holds' in a state of the world can be determined from the plan which produces that state of the world. The system chains backwards through the sequence of actions, so long as none of these actions deletes the sought-for facts, until the fact is found in the 'add'-set of an action or was given in the initial state.
PROBLEM 72  [WARREN, 1974b]

Verbal statement:

Using the problem solver WARPLAN, introduced in the previous problem, write the world description and the initial state for the 3 blocks shown in Figure 9.

![Figure 9](image)

Achieve the goal state on(a,b) & on(b,c).

Suggestion:

Use the predicates

\[
\text{add}(X,U) \quad \text{with the meaning} \quad \text{fact } X \text{ is added by action } U; \text{ i.e., } X \text{ is true in any state resulting from } U \text{ (and } U \text{ is a possible action in some state in which } X \text{ is not true)}
\]

\[
\text{del}(X,U) \quad \text{fact } X \text{ is deleted by action } U; \text{ i.e., it is not the case that } X \text{ is preserved by } U. \text{ ( } X \text{ is preserved by } U \text{ if and only if } X \text{ is not added by } U \text{ and } X \text{ is true in a state resulting from } U \text{ whenever } X \text{ is true in the preceding state)}
\]

\[
\text{can}(U,C) \quad \text{the conjunction of facts } C \text{ is the precondition of action } U; \text{ i.e., } U \text{ is possible in any state in which } C \text{ is true}
\]

\[
\text{always}(X) \quad \text{fact } X \text{ is true in any state}
\]

\[
\text{impossible}(X) \quad \text{the conjunction of facts } X \text{ is impossible in any state}
\]
given(T,X) with the meaning fact X is true in the initial state T (but it is not the case that X is true in all states).

Logic program:

In order to use WARPLAN we have just to write the data base according to the block situation above.

/* Data Base for the three blocks problem */

add(on(U,W),move(U,V,W)).
add(clear(V),move(U,V,W)).
del(on(U,Z),move(U,V,W)).
del(clear(W),move(U,V,W)).
can(move(U,V,floor),on(U,V)&not_equal(V,floor)&clear(U)).
can(move(U,V,W),clear(W)&on(U,V)&not_equal(U,W)&clear(U)).

impos(on(X,Y)&clear(Y)).
impos(on(X,Y)&on(X,Z)&not_equal(Y,Z)).
impos(on(X,X)).
given(start,on(a,floor)).
given(start,on(b,floor)).
given(start,on(c,a)).
given(start,clear(b)).
given(start,clear(c)).

Execution:

After adding this database to WARPLAN you just have to give the command:

:- plans(on(a,b)&on(b,c),start).

the solution is:

    start ;
    move(c,a,floor) ;
    move(b,floor,c) ;
    move(a,floor,b) .
PROBLEM 73

Verbal statement:

Consider the initial state of 5 blocks as shown in Figure 10 below, apply the program WARPLAN, presented in PROBLEM 63, to achieve the goal state:

\[
\text{on}(a,b) \& \text{on}(b,c) \& \text{on}(c,d) \& \text{on}(d,e),
\]

as it was done in the preceding problem.

![Figure 10](image)

Logic program:

Same facts 'add', 'del', 'can', and 'imposs' as those in the preceding problem.

The description of the initial state is:

/* Data Base for the five blocks problem */

given(start, on(e, floor)).
given(start, on(c, e)).
given(start, clear(c)).
given(start, on(a, floor)).
given(start, clear(a)).
given(start, on(d, floor)).
given(start, on(b, d)).
given(start, clear(b)).

Execution:

The command "!- plans(on(a,b) & on(b,c) & on(c,d) & on(d,e), start)."

runs the WARPLAN program and produces:

```
start ;
move(b,d,floor) ;
move(c,e,floor) ;
move(d,floor,e) ;
move(c,floor,d) ;
move(b,floor,c) ;
move(a,floor,b) .
```
Problem 74 [Warren, 1974a]

Verbal statement:

Consider a world comprising two areas 'inside' and 'outside'. In the area 'inside' there are four distinct locations, namely 'table', 'box1', 'box2', 'door'. There is a robot which is able to move about and transport objects. If the robot attempts to pick up an object at a location, all that can be ascertained is that it will be holding one of the objects, if any, at that location. The robot is only allowed to pick up an object if it is the only object at a location. Consider 3 objects 'key1', 'key2' and 'red1' and two actions 'go' and 'take'. The robot is only allowed to 'go' or 'take' something 'outside' if both the objects 'key1' and 'key2' are at the 'door'.

Consider the initial state given in Figure 11:

![Figure 11](image-url)

Use the program WARPLAN to achieve the goal: to have 'red1' outside.

Logic program:

```
:-op(300,xf,'IS'),
:-op(200,fx,'set '),
:-op(200,fx,'placed '),
:-op(200,fx,'only '),
:-op(100,xf,'at '),

add(position 'IS' P,go(P)),
add(X 'IS' placed Q,take(X,P,Q)),
add(set placed P 'IS' nothing,take(X,P,Q)),
add(set placed Q 'IS' only X,take1(X,P,Q)).
```
add(Z,\text{take}(X,P,Q)) \leftarrow \text{add}(Z,\text{take}(X,P,Q)).

del(\text{position 'IS' Z,go(P)}),
del(X \ 'IS' \ \text{placed Z,\text{take}(X,P,Q)}),
del(\text{position 'IS' Z,\text{take}(X,P,Q)}),
del(\text{set placed O 'IS' Z,\text{take}(X,P,Q)}),
del(\text{set placed P 'IS' Z,\text{take}(X,P,Q)}).

del(Z,\text{take}(X,P,Q)) \leftarrow \text{del}(Z,\text{take}(X,P,Q)).

can(\text{go(inside at L)}, \text{true}),
can(\text{take(X,inside at L1,inside at L2)},
    \text{set placed inside at L1 'IS' only X & position 'IS' inside at L1}),
can(\text{take1(X,inside at L1,inside at L2)},
    \text{set placed inside at L2 'IS' nothing &}
    \text{set placed inside at L1 'IS' only X & position 'IS' inside at L1}),
can(\text{take(X,inside at L,outside)},
    \text{set placed inside at L 'IS' only X & position 'IS' inside at L &}
    \text{key1 'IS' placed inside at door &}
    \text{key2 'IS' placed inside at door}),

given(start,\text{set placed inside at table 'IS' nothing}),
given(start,\text{set placed inside at box1 'IS' only key1}),
given(start,\text{set placed inside at box2 'IS' only key2}),
given(start,\text{set placed inside at door 'IS' only red1}).

\text{imposs(\text{position 'IS' P \& position 'IS' Q \& not_equal(P,Q))}).

Execution:

The command ':- plans(red1 'IS' placed outside,start).' runs WARPLAN after having added this data base.

The answer is:

\begin{verbatim}
start ;
\text{so(inside at door)} ;
\text{take1(red1, inside at door, inside at table)} ;
\text{so(inside at box1)} ;
\text{take(key1, inside at box1, inside at door)} ;
\text{so(inside at box2)} ;
\text{take(key2, inside at box2, inside at door)} ;
\text{so(inside at table)} ;
\text{take(red1, inside at table, outside)} .
\end{verbatim}

Remark:

The reason for the two versions of 'take' is that an action must have a unique set of preconditions, and the effects of 'take' depend on the set of objects at the destination. (See clauses 'can' in the logic program).
PROBLEM 75  [WARREN, 1974a]

Verbal statement:

Consider a very simple computer, comprising an accumulator and an unspecified number of general purpose registers. There are just four instructions 'load', 'store', 'add' and 'subtract'. To axiomatise the domain in order to use the program WARPLAN, presented in PROBLEM 63, it is necessary to follow each instruction in an assembly language program by a comment. The comment is introduced by '!' and states the value which will be in the accumulator after the instruction has been executed.

Describe such a machine and make it solve:

(1) acc is (c1-c2) + (c3-c4)

(2) acc is (c1-c2) + (c1-c2)

(3) acc is c1 + (c2-c3) &
    res2 is c2-c3 &
    res3 is c4 + c4

(4) res1 is c1 + (c2-c3) &
    res2 is c2-c3 &
    acc is c1

from the initial state: res1 is c1
                    res2 is c2
                    res3 is c3
                    res4 is c4

Logic program:

:-op(250,xyfxy,'!').
:-op(250,xyfxy,'IS').
:-op(150,xyfxy,'+').
:-op(150,xyfxy,'-').
:-op(150,fx,'load').
:-op(250,fx,'add').
:-op(150,fx,'subtract').
:-op(150,fx,'store').
:-op(150,fx,'res').

/*@ Machine code generation */

add(acc 'IS' V1+V2, add R $ V1+V2).
add(acc 'IS' V1-V2, subtract R $ V1-V2).
add(acc 'IS' V, load R $ V).
add(res R 'IS' V, store R $V).

del(acc 'IS' Z,U):- add(acc 'IS' V,U).
del(res R 'IS' Z,U):- add(res R 'IS' V,U).

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can(load R # V, res R 'IS' V),
can(store R # V, acc 'IS' V),
can(add R # V1+V2, res R 'IS' V2 & acc 'IS' V1),
can(subtract R # V1-V2, res R 'IS' V2 & acc 'IS' V1),

given(start, res1 'IS' c1),
given(start, res2 'IS' c2),
given(start, res3 'IS' c3),
given(start, res4 'IS' c4).

Execution:

(1) :- plans(acc 'IS' (c1-c2)+(c3-c4), start).

Answer:

\[
\begin{align*}
\text{start} ; \\
\text{load} 3 \# c3 ; \\
\text{subtract} 4 \# c3-c4 ; \\
\text{store} X1 \# c3-c4 ; \\
\text{load} 1 \# c1 ; \\
\text{subtract} 2 \# c1-c2 ; \\
\text{add} X1 \# (c1-c2)+(c3-c4) . 
\end{align*}
\]

(2) :- plans(acc 'IS' (c1-c2)+(c1-c2), start).

Answer:

\[
\begin{align*}
\text{start} ; \\
\text{load} 1 \# c1 \\
\text{subtract} 2 \# c1-c2 \\
\text{store} X1 \# c1-c2 \\
\text{add} X1 \# (c1-c2)+(c1-c2) . 
\end{align*}
\]

(3) :- plans(res1 'IS' c1+(c2-c3) & res2 'IS' c2-c3 & res3 'IS' c4+c4, start).

Answer:

\[
\begin{align*}
\text{start} ; \\
\text{load} 2 \# c2; \\
\text{subtract} 3 \# c2-c3; \\
\text{store} 2 \# c2-c3; \\
\text{load} 1 \# c1; \\
\text{add} 2 \# c1+(c2-c3); \\
\text{store} 1 \# c1+(c2-c3); \\
\text{load} 4 \# c4; \\
\text{add} 4 \# c4+c4; \\
\text{store} 3 \# c4+c4 . 
\end{align*}
\]
(4) :- plans(red1 'IS' c1+(c2-c3) &
   red2 'IS' c2-c3 &
   acc 'IS' c1,start).

Answer:

start ;
load 2 # c2 ;
subtract 3 # c2-c3 ;
store 2 # c2-c3 ;
load 1 # c1 ;
store X1 # c1 ;
add 2 # c1+(c2-c3) ;
store 1 # c1+(c2-c3) ;
load X1 # c1 .

Remark: The first branch in WARPLAN’S search space for question (4) is infinite. Interactive intervention to block this branch resulted in the above solution being found without any further assistance.

PROBLEM 76 [WARREN, 1974a]

Verbal statement:

Consider the world presented in Figure 12, belonging to STRIPS1.

Describe it and use WARPLAN to achieve the goals:

(1) status(lightswitch(1),on)
(2) nextto(box(1),box(2)) & nextto(box(2),box(3))
(3) at(robot,Point(6))

(4) nextto(box(2),box(3)) & nextto(box(3),door(1)) &
    status(lightswitch(1),on) & nextto(box(1),box(2)) &
    inroom(robot,room(2))

Logic Program:

/* Data Base for the STRIPS problem */

add(at(robot,P),soto1(P,R)),
add(nextto(robot,X),soto2(X,R)),
add(nextto(X,Y),pusho(X,Y,R)),
add(nextto(Y,X),pusho(X,Y,R)),
add(status(S,on),turnon(S)),
add(on(robot,B),climbon(B)),
add(onfloor(climboff(B)),
add(inroom(robot,R2),sothru(D,R1,R2)),

del(at(X,Z),U):- moved(X,U),
del(nextto(Z,robot),U):- !,del(nextto(robot,Z),U),
del(nextto(robot,X),pusho(X,Y,R)):- !, fail,
del(nextto(robot,B),climb(B)):- !, fail,
del(nextto(robot,B),climboff(B)):- !, fail,
del(nextto(X,Z),U):- moved(X,U),
del(on(X,Z),U):- moved(X,U),
del(onfloor,climb(B)),
del(inroom(robot,Z),sothru(D,R1,R2)),
del(status(S,Z),turnon(S)),

moved(robot,soto1(P,R)),
moved(robot,soto2(X,R)),
moved(robot,pusho(X,Y,R)),
moved(X,pusho(X,Y,R)),
moved(robot,climb(B)),
moved(robot,climboff(B)),
moved(robot,sothru(D,R1,R2)),

can(soto1(P,R),locinroom(P,R) & inroom(robot,R) & onfloor),
can(soto2(X,R),inroom(X,R) & inroom(robot,R) & onfloor),
can(pusho(X,Y,R),pushable(X) & inroom(Y,R) & inroom(X,R) &
    nextto(robot,X) & onfloor),
can(turnon(lightswitch(S)),on(robot,box(1)) &
    nextto(box(1),lightswitch(S))),
can(climb(B),nextto(robot,box(B)) & onfloor),
can(climboff(box(B)),on(robot,box(B))),
can(sothru(D,R1,R2),connects(D,R1,R2) & inroom(robot,R1) &
    nextto(robot,D) & onfloor),

always(connects(D,R1,R2)):- connects1(D,R1,R2),
always(connects(D,R2,R1)):- connects1(D,R1,R2),
always(inroom(D,R1)):- always(connects(D,R0,R1)).
always(pushable(box(N))),
always(locinroom(point(6),room(4))),
always(inroom(lightswitch(1),room(1))),
always(at(lightswitch(1),point(4))),
connects1(door(N),room(N),room(5)):- range(N,1,4).

range(M,M,N),
range(M,L,N):- not_equal(L,N), L1 is L+1, range(M,L1,N).
given(strips1,at(box(N),point(N))):- range(N,1,3),
given(strips1,at(robot,point(5))),
given(strips1,inroom(box(N),room(1))):- range(N,1,3),
given(strips1,inroom(robot,room(1))),
given(strips1,onfloor),
given(strips1,status(lightswitch(1),off)).

Execution:

(1) :- plans(status(lightswitch(1),on),start).
Answer:

start ;
goto2(box(1),room(1)) ;
push_to(box(1),lightswitch(1),room(1)) ;
climb_on(box(1)) ;
turn_on(lightswitch(1)) .

(2) :- plans(next_to(box(1),box(2) & next_to(box(2),box(3)),start).
Answer:

start ;
goto2(box(2),room(1)) ;
push_to(box(2),box(3),room(1)) ;
goto2(box(1),room(1)) ;
push_to(box(1),box(2),room(1)) .

(3) :- plans(at(robot,point(6)),start).
Answer:

start ;
goto2(door(1),room(1)) ;
softmax(door(1),room(1),room(5)) ;
goto2(door(4),room(5)) ;
softmax(door(4),room(5),room(4)) ;
goto1(point(6),room(4)) .
(4) :- plans(nextto(box(2),box(3)) & 
nextto(box(3),door(1)) &
status(lightswitch(1),on) &
nextto(box(1),box(2)) &
inroom(robot,room(2)),start).

Answer:

start;
soto2(box(3),room(1));
pushto(box(3),door(1),room(1));
soto2(box(2),room(1));
pusho(box(2),box(3),room(1));
soto2(box(1),room(1));
pusho(box(1),lightswitch(1),room(1));
climbon(box(1));
turnon(lightswitch(1));
climboff(box(1));
soto2(box(1),room(1));
pusho(box(1),box(2),room(1));
soto2(door(1),room(1));
sothru(door(1),room(1),room(5));
soto2(door(2),room(5));
sothru(door(2),room(5),room(2)).

PROBLEM 77 [WARREN,1975b]

Verbal statement:

Consider a world consisting of the following objects, facts and actions:

Objects:

numbers, N = <1,2,...,etc>
directions, D = <left,right>
wheels, W = <wheel1, wheel2,...,wheelN>
axles, A = <axle1,...,axle N>
endofaxles, E = <Blendof A1> where D1 D and A1 A
holes, H = <hole1,...,hole N>
vice, V = <vice>

Facts:

Static, D1 is opposite of D2, where D1,D2∈D

Dynamic, W1 is attached to E1, where W1∈W and E1∈E
Dynamic, A1 is thru H1, where A1∈A and H1∈H
Dynamic, E1 points D1, where E1∈E and D1∈D
Dynamic, carbody is blocked to D1, where D1∈D
Dynamic, carbody is unblocked to D1, where D1∈D
Dynamic, W1+A1+H1+V1 is free, where W1∈W,A1∈A,H1∈H and V1∈V

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Actions:

insert E1 into W,  
push W1 from D1 to D2 onto E1 in H1,  
slide E1 into H1 from D1,  
block carbody to D1,  
unblock carbody to D1,  
clamp W1,  
unclamp W1+A1,

where E1 ∈ E and W1 ∈ W
where W1 ∈ W, H1 ∈ H, E1 ∈ E
where E1 ∈ E, H1 ∈ H and D1 ∈ D
where D1 ∈ D
where D1 ∈ D
where W1 ∈ W
where W1 ∈ W and A1 ∈ A

the actions may be pictured as follows (Figures 13 and 14):

![Diagram](image)

**Figure 13**
PUSH $W$ FROM $D_1$ TO $D_2$ onto $E$ IN $H$

SLIDE $E$ INTO $H$ FROM $D$

CLAMP $W$

UNCLAMP $W$

Figure 14

Describe this world as a data base in order to use WARPLAN to solve car assembly problems.
Logic program:

/* Operators definition */
:- op(600,fx,'insert'),
:- op(600,fx,'push'),
:- op(600,fx,'slide'),
:- op(600,fx,'clamp'),
:- op(600,fx,'unclamp'),
:- op(600,fx,'block_car_body_to'),
:- op(600,fx,'unblock_car_body_to'),
:- op(600,fx,'car_body_is_unblocked_to'),
:- op(600,fx,'car_body_is_blocked_to'),
:- op(600,xf,'is_free'),
:- op(600,xf,'is_clamped'),
:- op(500,xfy,'is_thru'),
:- op(500,xfy,'points'),
:- op(500,xfy,'is_opposite_of'),
:- op(500,xfy,'is_attached_to'),
:- op(400,yfx,'into'),
:- op(400,yfx,'from'),
:- op(400,yfx,'to'),
:- op(400,yfx,'onto'),
:- op(400,yfx,'in'),
:- op(300,xfy,'end_of'),
:- op(200,fx,'wheel'),
:- op(200,fx,'axle'),
:- op(200,fx,'hole'),

/* Definition of the goal state */
goal(T):- plans(axle A1 is_thru hole1 &
axle A2 is_thru hole2 &
wheel W1 is_attached_to left end_of axle A1 &
wheel W2 is_attached_to left end_of axle A2 &
wheel W3 is_attached_to right end_of axle A1 &
wheel W4 is_attached_to right end_of axle A2,T).

/* Database */
add(W is_attached_to E, insert E into W).
add(W is_attached_to E, push W from D1 to D2 onto E in H).
add(A is_thru H, slide D1 end_of A into H from D2).
add(wheel W is_clamped, clamp wheel W).
add(axle A is_clamped, insert D end_of axle A into W).
add(wheel W is_free, unclamp wheel W).
add(axle A is_free, unclamp axle A).
add(vice is_free, unclamp X).
add(car_body_is_blocked_to D, block_car_body_to D).
add(car_body_is_unblocked_to D, unblock_car_body_to D),
add(D1 end_of A points D, slide D1 end_of A into H from D2):-
    always(D is_opposite_of D2),
add(D end_of A points D2, slide D1 end_of A into H from D2):-
    always(D is_opposite_of D1),

can(insert D end_of axle A into wheel W, axle A is_free &
    D end_of axle A is_free &
    wheel W is_clamped),
can(push wheel W from D1 to D2 onto D end_of axle A in hole H,
    wheel W is_free &
    D end_of axle A is_free &
    axle A is_thru hole H &
    D end_of axle A points D1 &
    car_body_is_unblocked_to D1 &
    D2 is_opposite_of D1 &
    car_body_is_blocked_to D2),
can(slide D1 end_of axle A into hole H from D2,
    axle A is_free &
    D1 end_of axle A is_free &
    hole H is_free &
    car_body_is_unblocked_to D2),
can(clamp wheel W, wheel W is_free & vice is_free),
can(unclamp X, X is_clamped),
can(block_car_body_to D, true),
can(unblock_car_body_to D, true),
del(X is_free, U):- add(X is_clamped, U),
del(X is_free, U):- add(X is_attached_to Z, U),
del(X is_free, U):- add(Z is_attached_to X, U),
del(A is_free, slide D1 end_of A into H from D2),
del(H is_free, slide E into H from D2),
del(vice is_free, clamp W),
del(car_body_is_unblocked_to D, block_car_body_to D),
del(car_body_is_blocked_to D, unblock_car_body_to D),
del(Z is_clamped, unclamp Z),
del(W is_clamped, insert E into W),
imposs(axle A is_free & axle A is_thru hole H),
imposs(D end_of A is_free & W is_attached_to D end_of A),
imposs(wheel W is_free & wheel W is_attached_to E),
imposs(wheel W is_free & wheel W is_clamped),
imposs(hole H is_free & A is_thru hole H),
imposs(axle A is_free & axle A is_clamped),
imposs(vice is_free & X is_clamped),
imposs(car_body_is_blocked_to D & car_body_is_unblocked_to D),
always(true),
always(left is_opposite_of right),
always(right is_opposite_of left).
Problem 78 [WARREN, 1975b]

Verbal statement:

Consider the initial state of the car assembly process as it is pictured in Figure 15.

![Figure 15]

Describe this initial state in order to use the preceding problem and the program WARPLAN to solve the rest of the assembly process.
Logic Program:

This state is called the "middle state" just because a small part of the car is already assembled when the process starts.

/* Description of the middle state */

siven(middle, wheel W is_free):- member(W,[2,3,4]).
siven(middle, wheel 1 is_attached_to left end_of axle 1).
siven(middle, axle N is_thru hole N):- member(N,[1,2]).
siven(middle, D end_of axle A points D):=
    member(D,[left,right]),
    member(A,[1,2]).
siven(middle, right end_of axle A is_free):- member(A,[1,2]).
siven(middle, left end_of axle 2 is_free).
siven(middle, vice is_free).
siven(middle, car_body is_unblocked_to D):-
    member(D,[left,right]).

member(A,[A;_]).
member(A,[_;B]):- member(A,B).

Execution:

To run the program WARPLAN with such an initial state and such a database it is just needed to give the command: "!- goal(middle).".

The answer is:

  block_car_body_to right;
  push wheel2 from left to right onto left end_of axle 2 in hole 2;
  unblock_car_body to right;
  block_car_body to left;
  push wheel 3 from right to left onto right end_of axle 1 in hole 1;
  push wheel 4 from right to left onto right end_of axle 2 in hole 2.

PROBLEM 79 [WARREN,1975b]

Verbal statement:

Now consider the initial state of the car assembly process as in Figure 16.
Solve the preceding problem considering this initial state and taking into account the program WARPLAN.

Logic program:

/* Description of the start state */

given(start, wheel W is_free):- member(W, [1, 2, 3, 4]).
given(start, axle A is_free):- member(A, [1, 2]).
given(start, end_of_axle A is_free):- member(D, [left, right]), member(A, [1, 2]).

given(start, hole H is_free):- member(H, [1, 2]).
given(start, vice is_free).
given(start, car_body_is_unblocked_to D):- member(D, [left, right]).

member(A[A: ...]).
member(A, [..:B]):- member(A, B).
Execution:

Just give the command: `!- goal(start).` and the answer will be:

slide left end_of_axle 1 into hole 1 from left;
slide left end_of_axle 2 into hole 2 from left;
block_car_body_to_left;
push wheel 1 from right to left onto left end_of_axle 1 in hole 1;
push wheel 2 from right to left onto left end_of_axle 2 in hole 2;
unblock_car_body_to_left;
block_car_body_to_right;
push wheel 3 from left to right onto right end_of_axle 1 in hole 1;
push wheel 4 from left to right onto right end_of_axle 2 in hole 2.
3.6 MACHINE TRANSLATION (nos. 80 to 86)

PROBLEM 80

Verbal statement:

Transform a natural language sentence, taken as a string of characters with some spaces between them, into a list whose elements are its words.

Suggestion: 1) Consider the following cut marks: 'space', '?', '.', '!', line_feed', and 'CR'.

2) Suppose the sentences may finish by '?', '.', '!', or '!' .

3) Knowing that PROLOG cannot read word by word, you have to imagine a character by character transformation.

Logic Program:

```
sentence(F):- set(C), words(C,F).

words(C,[P:Ps]):- letter(C), word(C,C1,L),
                 name(F,L), words(C1,Ps).

words(44,[,];Ps):- set(C1), words(C1,Ps).

words(63,['?' ];).

words(46,[.];).

words(33,[!];).

words(_,P):- set(C), words(C,P).

word(C,C1,[C;Cs]):- set0(C2), (letter(C2), word(C2,C1,Cs);
                         C1=C2, Cs=[]).

letter(32):- !, fail.          /* space */
letter(43):- !, fail.          /* ? */
letter(46):- !, fail.          /* . */
letter(33):- !, fail.          /* ! */
letter(44):- !, fail.          /* ! */
letter(10):- !, fail.          /* line_feed */
letter(13):- !, fail.          /* CR */
letter(_),
```

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**Problem 81**

Verbal statement:

In the preceding problem, make the suitable modification in order that capital letters might be transformed into small letters, knowing that the internal codes of capital letter go from 64 to 90 and that the codes of the corresponding small letter can be obtained adding 32.

Logic programs:

/* Program 1

Define two new predicates 'set' and 'set0' as follows: */

```
set(C,A):- set(C),(C=<90,C>=64,A is C + 32 ; A=C).
set0(C,A):- set0(C),(C=<90,C>=64,A is C+32 ; A=C).
```

/* Replace the usual calls to 'set' and 'set0' by new calls of the above predicates, the resulting program will be (we will write only the new clauses): */

```
sentence(F):- set(C,A),words(A,F).
words([',','Ps]):- set(C1,A),words(A,P).
words(_,P):- set(C,A),words(A,P).
word(C,C1,[C;Cs]):- set0(C2,A,(letter(A),word(A,C1,Cs); C1=A, Cs=[])).
```

/* Program 2

Redefine the predicate 'letter' as follows: */

```
letter(32,...):- !,fail. /* space */
letter(63,...):- !,fail. /* ? */
letter(46,...):- !,fail. /* . */
letter(33,...):- !,fail. /* ! */
letter(44,...):- !,fail. /* , */
letter(10,...):- !,fail. /* line_feed */
letter(13,...):- !,fail. /* CR */
letter(L,NL):- (L=<90,L>=64,NL is L+32; L=NL).
```

/* Then we replace the calls of the old 'letter' by calls to the new 'letter': */

```
words(C,[P;Ps]):- letter(C,NC),word(NC,C1,L),
name(P,L),words(C1,P).
```

```
word(C,C1,[C;Cs]):- set0(C2),(letter(C2,NC2),word(NC2,C1,Cs);
C1 = C2, Cs = []).
```

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PROBLEM 82

Verbal statement:

Suppose you have a list L of atoms, for instance proper nouns. Output that list word by word, each of them with the first letter as a capital, and separate from the previous by a comma, the last one separate by 'and'.

Logic program:

```
output([N]):-capitals(N,N1),write(N1),write(',').
output([N,N1]):-capitals(N,N2),write(N2),write(' and '),
             output([N1]),
output([N:Ns]):-capitals(N,N1),write(N1),write(', '),
              output(Ns).
```

capitals(X,X1):-name(X,[A:L]),A>=97,
               B is A-32,name(X1,[B:L]).

capitals(X,X).

Remarks: 1) the second clause of 'capitals' is only needed when the word has already capital letter.

2) the output of the list [John,mary,james] will be:

   'John, Mary and James':

PROBLEM 83 [WARREN,1977b]

Verbal statement:

Consider the following BNF grammar and write it as a PROLOG program.

```
<Program> ::= <statements>
<statements> ::= <statement> ;
               <statement> ; <statements>
<statement> ::= <name> ! = <expr> !
               IF <test> THEN <statement> ELSE <statement> ;
               WHILE <test> DO <statement> ;
               READ <name> !
               WRITE <expr> !
               ( <statements> )
<test> ::= <expr> <comparison op> <expr>
<expr> ::= <expr> <op 2> <expr 1> !
          <expr 1>
<expr 1> ::= <expr 1> <op 1> <expr 0> !
          <expr 0>
<expr 0> ::= <name> !
           <integer> !
           ( <expr> )
<comparison op> ::= = ! < > ! = ! <= ! => ! = !
```

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Logic Program:

Program(Z0,Z,X) :- statements(Z0,Z,X).

statements(Z0,Z,X) :- statement(Z0,Z1,X0),
            restatements(Z1,Z,X0,X).

restatements((';',Z0),Z,X0,(X0,X)) :- statements(Z0,Z,X),
            restatements(Z,X,X).

statement(('=',Z0),Z,assign(name(V),Expr)) :-
            atom(V), Expr(Z0,Z,Expr).

statement(('if',Z0),Z,if(Test,Then,Else)) :-
            test(Z0,(then,Z1),Test),
            statement(Z1,(else,Z2),Then),
            statement(Z2,Z,Else).

statement(('while',Z0),Z,while(Test,Do)) :-
            test(Z0,(do,Z1),Test),
            statement(Z1,Z,Do).

statement(('read',V,Z),Z,read(name(V))) :-
            atom(V), Expr(Z0,Z,Expr).

statement(('write',Z0),Z,write(Expr)) :-
            Expr(Z0,Z,Expr).

statement(('''',Z0),Z,S) :- statements(Z0,(''',Z),S).

test(Z0,Z,test(Op,X1,X2)) :-
            Expr(Z0,(Op,Z1),X1), comparisonop(Op),
            Expr(Z1,Z,X2).

Expr(Z0,Z,X) :- subExpr(Z0,Z,X).

subExpr(N,Z0,Z,X) :- N>0, N1 is N-1,
            subExpr(N1,Z0,Z1,X0),
            restExpr(N,Z1,Z,X0,X).

subExpr(0,(X,Z),Z,name(X)) :- atom(X),

subExpr(0,(X,Z),Z,const(X)) :- integer(X).

subExpr(0,('''',Z0),Z,X) :- subExpr(Z0,'''',Z),X.

restExpr(N,(Op,Z0),Z,X1,X) :- op(N,Op), N1 is N-1,
            restExpr(N1,Z1,Z,X1,X2),
            restExpr(N,Z1,Z,Expr(Op,X1,X2),X).

comparisonop(=),
comparisonop(<),
comparisonop(>),
comparisonop(=\<),
comparisonop(\>=),
comparisonop(\=).

Op(2,*), Op(1,\+)
Op(2,\/), Op(1,-).
PROBLEM 84  [PEREIRA et al., 1978]

Verbal statement:

Construct a simple grammar which parses an arithmetic expression
(made up of digits and operators) and computes its value.
Consider "-2+3*5+1" as an example of an arithmetic expression.

Logic program:

expr(Z) -> term(X), '+', expr(Y), {Z is X+Y},
expr(Z) -> term(X), '-', expr(Y), {Z is X-Y},
expr(Z) -> term(Z).

term(Z) -> number(X), '*', term(Y), {Z is X*Y},
term(Z) -> number(X), '/', term(Y), {Z is X/Y},
term(Z) -> number(Z).

number(C) -> '+', number(C),
number(C) -> '-', number(X), {C is -X},
number(X) -> [C], {'0'=<C, C<='9'}, X is C-'0'.

Execution:

The question:  ?-expr(Z,'-2+3*5+1',[]).

will compute  Z=14

PROBLEM 85  [WARREN, 1974b]

Verbal statement:

Write a program able to translate the functional LISPish notation
into the usual PROLOG notation, for example translate

:rev([X:L]) = :app(:rev(L),[X]) &
:rev([]) = [] &

:app([X:L1],L2) = [X::app(L1,L2)] &
:app([],L) = L

into

rev([X:L1],L) :- rev(L1,L2), app(L2,[X],L),
rev([],[]).

app([X:L1],L2,[X:L3] :- app(L1,L2,L3),
app([],L,L).
Logic program:

:-op(300, yfx, &).
:-op(200, yfx, =).
:-op(100, fxy, !).

/* Translation from functional notation into
PROLOG notation */

let(P) :- let1(P).
let( ) .

let1(P & Q) :- !, let1(P),
let1(P & Q) :- !, let1(Q).
let1( T0 = V0 ) :- T0 = . . [F : A0], trans(V0, V, [ ], C),
                app(A0, [V], A1), T = . . [F : A1],
                write(T), output(C), nl, fail.

trans(T0, T0, C0, C0) :- var(T0, !).
trans( ! , T0 = . . [F : A0], translist(A0, A, [T; C0], C),
      app(A, [V], A1), T = . . [F : A1],
trans(T0, T, C0, C) :- T0 = . . [F : A0], translist(A0, A, C0, C),
      T = . . [F : A1],

translist([T0; A0], [T; A], C0, C) :- translist(A0, A, C0, C1),
                trans(T0, T, C1, C).
translist([ ], [ ], C0, C0).  

app([X|L1], L2, [X|L3]) :- app(L1, L2, L3),
app([ ], L, L).

output(X) :- write( ' ', ' ), nl, !.
output( X ) :- write( ' - ', output1(X).

output1([A]) :- write(A), write( ' ', ' ), nl, !.
output1([A; B]) :- write(A), write( ' ', ' ), output1(B).

Execution:

To perform the program give the command ':-let(P),' where P must
be what you want to translate into PROLOG, for example:

:-let( : rev([X|L]) = :app( :rev(L), [X]) &
 : rev([ ] ) = [] &
 : app([X|L1], L2) = [X|app(L1, L2)] &
 : app([ ], L) = L ),

rev([X|L], L1) :- rev(L, L2), app(L2, [X], L1),
rev([ ], [ ]).

app([X|L1], L2, [X|L3]) :- app(L1, L2, L3),
app([ ], L, L).

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PROBLEM 86

Verbal statement:

Write a program able to translate the PROLOG notation into pseudo-English.

Consider the following definitions as a start point:

\[
\begin{align*}
P & :- Q \quad \text{means} \quad P \text{ if } Q \\
P ; Q & \quad \text{means} \quad P \text{ and } Q \\
P : Q & \quad \text{means} \quad P \text{ or } Q
\end{align*}
\]

The program must also be able to achieve new definitions from the user and to retrovert English into PROLOG notation.

Logic program:

```prolog
:- op(300,xf,?).

begin:- asserta(definition(X,X)),
         asserta(definition((P;Q),(P;or,Q))),
         asserta(definition((P:-Q),(P;if,Q))),
         asserta(definition((P;Q),(P;and,Q))),
         repeat nl nl read(T),(T=stop;Process(T),fail).

Process(T-D):- !,asserta(definition(T,D)).
Process([T1:T2]):- retrovert(T,[T1:T2]),!,nl,write(T),
Process(T):- translate(T,D),nl,output(D),!
Process(_):- nl,write(untranslatable),nl.

/* Retroversion process */
retrovert(T,D):- definition(T1,D),!,T1=..[N:L],
                 retrovert_args(args,L), T=..[N!Args].
retrovert_args([A:Args],[L:Ls]):- retrovert(A,L),
retrovert_args([],[]).

/* Translation process */
translate(X,X):- var(X),!.
translate(T,D):- T=..[N:Args],args(Args,L),
                T1=..[N!L],definition(T1,D).
args([A:Args],[L:Ls]):- translate(A,L),args(Args,L),
args([],[]).

/* Output process */
output([X:S]):- var(X),write(X),write(’,’),output(S).
output([X:S]):- output(X),write(X),write(’,’),output(S),
output([X:L:S]):- write(’,’),output([X:L]),
                write(’,’),output(S).
```

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output([X;S]):- write(X),write(‘ ’),output(S),
output([]).

Execution:

As an example of this program we are going to see the translation of some of its clauses.

(\-LC)
(\-op(300,xf,?))

Process(_73,_96) if (! and asserta(definition(_73,_96)))

Process(_78!_101)? if (retrovert(_133,[_78;_101] and (! and
(n1 and (write(_133) and put([46]) ))))

Process(_73) if (translate(_73,_118) and (n1 and (output(_118)
and ! )))

Process(_73) if (n1 and (write(untranslatable) and n1 ))

retrovert(_73,_73) if (var(_73) and ! )

retrovert(_73,_94) if (definition(_124,_94) and (! and
(_124=..[_177;_200] and (retrovert_args(_228,_200) and
_73=..[_177;_228] ))))

translate(_73,_73) if (var(_73) and !)

translate(_73,_94) if (_73=..[_134;_157] and (args(_157,_201)
and (_222=..[_134;_201] and definition(_222,_94) )))
3.7 NATURAL LANGUAGE (nos. 87 to 95)

PROBLEM 87

Verbal statement:

Write a simple grammar G1 for analysing the sentences:

' the giraffe dreams'
' the giraffe eats apples'

Logic program:

\[ \text{sent}(X, Y) :\neg \text{np}(X, U), \text{vp}(U, Y). \]
\[ \text{np}(X, Y) :\text{det}(X, U), \text{noun}(U, Y). \]
\[ \text{vp}(X, Y) :\text{iverb}(X, Y). \]
\[ \text{vp}(X, Y) :\text{tverb}(X, U), \text{np}(U, Y). \]
\[ \text{det}([\text{the}!Y], Y). \]
\[ \text{noun}([\text{giraffe}!Y], Y). \]
\[ \text{noun}([\text{apples}!Y], Y). \]
\[ \text{iverb}([\text{dreams}!Y], Y). \]
\[ \text{tverb}([\text{dreams}!Y], Y). \]
\[ \text{tverb}([\text{eats}!Y], Y). \]

PROBLEM 88

Verbal statement:

Reconsider the previous grammar G1 in order to deal with the following context-sensitive aspects:

1) the number of a noun phrase agrees with that of the corresponding verb phrase;

2) the number of a noun phrase need not be determined by the noun only (this fish—these fish) and not by the 'th-word' only (the giraffe—the giraffes), but number is a feature of the entire noun phrase;

3) a noun phrase need not have a determiner (giraffes dream) presumably provided that the noun phrase is plural.
Logic program:

sent(X,Y) :- np(N,X,Y), vp(N,Y).
np(N,X,Y) :- th(N,X,U), noun(N,U,Y).
np(plu,X,Y) :- noun(plu,X,Y).
vp(N,X,Y) :- verb(i,N,X,Y).
vp(N,X,Y) :- verb(t,N,X,U), np(M,Y).
noun(sin,[U:Y],Y) :- npf(U,V).
noun(plu,[U:Y],Y) :- npf(U,V).
verb(T,sin,[U:Y],Y) :- conj(T,U,V).
verb(T,plu,[U:Y],Y) :- conj(T,U,V).
npf(giraffe,siraffes).
npf(fish,fishes).
npf(dream,dreams).
conj(T,dreams,dream).
conj(T,eats,eat).
th(N,[the:Y],Y).
th(sin,[this:Y],Y).
th(plu,[these:Y],Y).

Problem 89

Verbal statement:

Write a simple grammar able to parse sentences, such as

"John ate the cake"

and to construct their corresponding deep tree structures.

Suggestion: use the definite clause grammars formalism.

Logic program:

sentence(s(T1,T2)) --> noun_phrase(T1), verb_phrase(T2).
noun_phrase(np(T1,T2)) --> determiner(T1), noun(T2).
verb_phrase(vp(T1,T2)) --> verb(T1), noun_phrase(T2).
determiner(det(the)) --> [the],
determiner(det([])) --> [].
noun(n(john)) --> [john].
noun(n(cake)) --> [cake].
verb(v(ate)) --> [ate].

PROBLEM 90 [PEREIRA&WARREN,1978]

Verbal statement:

Write a context-free grammar that covers the following sentences,

'John loves Mary',

'every man that lives loves a woman'

and that formalises the mapping between English and formulae of classical logic.

Suggestion: use the definite clause grammars formalism

Logic program:

:-op(900,xfx,=).
:-op(800,xfy,&).
:-op(300,xfx,;).

sentence(P) --> noun_phrase(X,P1,P), verb_phrase(X,P1).
noun_phrase(X,P1,P) -->
determiner(X,P2,P1,P), noun(X,P3), rel_clause(X,P3,P2),
noun_phrase(X,P,P) --> name(X),
verb_phrase(X,P) --> trans_verb(X,Y,P1), noun_phrase(Y,P1,P),
verb_phrase(X,P) --> intrans_verb(X,P).
rel_clause(X,P1,P1&P2) --> [that], verb_phrase(X,P2),
rel_clause(_,P,P) --> [].
determiner(X,P1,P2, all(X):(P1=P2) ) --> [every],
determiner(X,P1,P2, exists(X):(P1&P2) ) --> [a],
noun(X,man(X)) --> [man],
noun(X,woman(X)) --> [woman],
name(john) --> [john],
trans_verb(X,Y,loves(X,Y)) --> [loves],
intrans_verb(X,lives(X)) --> [lives].
Problem 91 [PEREIRA;WARREN, 1978]

Verbal statement:

Write a grammar that covers the following sentences,

- 'Fred shot John'
- 'Mary was liked by John'
- 'Fred told Mary to shot John'
- 'John was believed to have been shot by Fred'
- 'Was John believed to have told Mary to tell Fred'

Suggestion: use the definite clause grammars formalism.

Logic program:

\[
\begin{align*}
\text{sentence}(S) & \rightarrow \\
& \{ \text{aux-verb}(W, \text{Verb}, \text{Tense}) \}, \\
& \text{noun-phrase}(G \text{-Subj}), \\
& \text{rest-sentence}(o, G \text{-Subj}, \text{Verb}, \text{Tense}, S). \\
\text{sentence}(S) & \rightarrow \\
& \text{noun-phrase}(G \text{-Subj}), \\
& \{ \text{verb}(W, \text{Verb}, \text{Tense}) \}, \\
& \text{rest-sentence}(\text{del}, G \text{-Subj}, \text{Verb}, \text{Tense}, S). \\
\text{rest-sentence}(\text{Type}, G \text{-Subj}, \text{Verb}, \text{Tense}, \\
& \text{s}(\text{Type}, L \text{-Subj}, \text{tns}(\text{Tense1}), \text{VP})) & \rightarrow \\
& \text{rest-verb}(\text{Verb}, \text{Tense}, \text{Verb1}, \text{Tense1}), \\
& \{ \text{verbtype}(\text{Verb1}, \text{VT} \text{-Type}) \}, \\
& \text{complement}(\text{VT} \text{-Type}, \text{Verb1}, G \text{-Subj}, L \text{-Subj}, \text{VP}). \\
\text{rest-verb}(\text{have}, \text{Tense}, \text{Verb}, \text{(Tense, perfect)}) & \rightarrow \\
& \{ \text{past-participle}(W, \text{Verb}) \}, \\
& \text{rest-verb}(\text{Verb}, \text{Tense}, \text{Verb}, \text{Tense}) & \rightarrow \text{[]} \text{.} \\
\text{complement}(\text{copula}, \text{be}, \text{Obj}, \text{Subj}, \text{vp}(v(\text{Verb}), \text{Obj1}) & \rightarrow \\
& \{ \text{past-participle}(W, \text{Verb}), \text{transitive}(\text{Verb}) \}, \\
& \text{rest-object}(\text{Obj}, \text{Verb}, \text{Obj1}), \\
& \text{agent}(\text{Subj}). \\
\text{complement}(\text{transitive}, \text{Verb}, \text{Subj}, \text{Subj}, \text{vp}(v(\text{Verb}), \text{Obj1}) & \rightarrow \\
& \text{noun-phrase}(\text{Obj}), \\
& \text{rest-object}(\text{Obj}, \text{Verb}, \text{Obj1}). \\
\text{complement}(\text{intransitive}, \text{Verb}, \text{Subj}, \text{Subj}, \text{vp}(v(\text{Verb})) & \rightarrow \text{[]} \text{.} \\
\text{rest-object}(\text{Obj}, \text{Verb}, \text{S}) & \rightarrow \\
& \{ \text{s-transitive}(\text{Verb}) \}, \\
& \{ \text{to}, \text{Verb1} \}, \{ \text{infinitive}(\text{Verb1}) \}, \\
& \text{rest-sentence}(\text{del}, \text{Obj}, \text{Verb1}, \text{present}, \text{S}), \\
& \text{rest-object}(\text{Obj}, \text{Verb}, \text{Obj}) & \rightarrow \text{[]} \text{.}
\end{align*}
\]
agent(Subj) --> [by], noun_phrase(Subj),
agent(nP(Pro(someone))) --> [].
noun_phrase(nP(Det,adj(Adjs),n(Noun))) -->
  [Det], {determiner(Det)},
  adjectives(Adjs),
  [Noun], {noun(Noun)}.
noun_phrase(nP(nP(PN))) --> [PN], {proper_noun(PN)}.

adjectives([Adj|Adjs]) -->
  [Adj], {adjective(Adj)},
  adjectives(Adjs),
  adjectives([]) --> [].

aux_verb(W,V,T) :- verb(W,V,T), auxiliary(V).

auxiliary(be),
auxiliary(have),
verb(is,be,present),
verb(was,be,perfect),
verb(tell,tell,present),
verb(told,tell,perfect),
verb(shoot,shoot,present),
verb(shot,shoot,perfect),
verb(like,like,present),
verb(liked,like,perfect),
verb(believe,believe,present),
verb(believed,believe,perfect),

proper_noun(john),
proper_noun(fred),
proper_noun(mary),
determiner(the),
adjective(nice),
noun(book),
verbtype(be,copula),
verbtype(V,transitive) :- transitive(V),
verbtype(V,intransitive) :- intransitive(V).

transitive(V) :- s_transitive(V),
transitive(shoot),
s_transitive(tell),
s_transitive(believe),
s_transitive(like).
infinitive(be),
infinitive(shoo),
infinitive(tell),
infinitive(have),
past_participle(been, be),
past_participle(shot, shoot),
past_participle(told, tell),
past_participle(liked, like),
past_participle(believed, believe).

**Problem 92** [COLMERAUER, 1977]

Verbal statement:

Write a simple Portuguese grammar for analysing sentences, such as:

"helder habita em caparica" (helder lives at caparica)

"helder e' mais velho que luis" (helder is older than luis)

Consider the input sentence as a list.

Logic program:

```prolog
:- op(500, xfy, '->').

/* Dialogue control */
ola:- nl,read(X),phrase(R,X,[]),answer(R),nl.
answer(X):- X!1, display('Sim'),nl,nl,
answer(X):- display('Nao'),nl,nl.

/* Deductive block */
and(X,Y):- X,Y.
local(X):- file(_,_,X),
type(X):- file(X,_,_),
live_at(X,Y):- file(X,_,Y),
older_than(X,Y):- file(X,I1,L1),file(Y,I2,L2),
                 I2 < I1.

/* Grammar */
phrase(03) --> np(X,02,03),vp([suj-X;L],01),
          compls(L,01,02).
```

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compls([],0,0) --> !.
compls([X-X:L],0,0,3) --> compls(L,0,1,2), case(K),
\[ np(X,0,2,3). \]
np(X,0,2,04) --> art(X,0,1,02,03), name([su-X-X:X],01),
\[ compls(L,0,3,04). \]
np(X,0,0) --> [X], {ind(X)}.

ind(X):- type(X).

ind(X):- local(X).

case(em) --> [em].

case(que) --> [que].

case(dir) --> [].

art(X,0,1,02,\text{and}(01,02)) --> [um].
art(X,0,1,02,\text{not}(\text{and}(01,02))) --> [nenhum].
art(X,0,1,02,\text{not}(\text{and}(01,\text{not}(02)))) --> [cada].

name([su-X-X],type(X)) --> [tipo], [pessoa].
name([su-X-X],local(X)) --> [local], [morada].

vp([su-X-X,em-Y],live_at(X,Y)) --> [habita].
vp([su-X-X,que-Y],older_than(X,Y)) --> ['e', 'mais velho].

/* Data base */

file(luis,29,carparica).
file(helder,33,restelo).
file(fernando,26,alvalade).
file(carlos,36,olivais).

PROBLEM 93

Verbal statement:

Write a simple program able to derive Portuguese relative constructions, given their sentential components.

Hint:

Consider the following two sentences,

"eu vi o rapaz" (I saw the boy)
"o rapaz comprou o livro" (The boy bought the book)

build up its deep structure and analyse how it may be transformed to represent the corresponding relative sentence.
Logic program:

go!:- frase(F),write(F),nl
    sent(T,F,[I]),nl,write(T),
    transrel(T,V),nl,write(V),nl,
    sent(V,TR,[J]),nl,write(TR),nl.

/* Grammar */

sent([fr,X,Y,Z]) --> su(X),aux(Y),sv(Z).

sn([sn,X])  --> n(X),
sn([sn,X,Y]) --> det(X),n(Y),
sn([sn,X])  --> pro(X),
sn([sn,X,Y]) --> sn(X),sent(Y).

sv([sv,X])  --> v(X),
sv([sv,X,Y]) --> cop(X),adj(Y),
sv([sv,X,Y]) --> v(X),sn(Y),
sv([sv,X])  --> cop(X),sn(Y).

aux([aux,X])  --> tpo(X).

/* lexicon */

tpo([tpo,pass])  --> [pass],
cop([cop,estar]) --> [estar],
cop([cop,ser])  --> [ser],
adj([adj,conte]) --> [conte],
pro([pro,que])   --> [que],
n([n,eu])       --> [eu],
n([n,rapaz])    --> [rapaz],
n([n,livro])    --> [livro],
det([det,o])    --> [o],
v([v,ver])      --> [ver],
v([v,comprar])  --> [comprar].

/* transformations for the grammar */

transrel(T,V):- change([sn,[sn,ST1],R],
    [sn,[sn,ST1],[fr,ST2]],
    T,
    V),
    change([sn,[pro,que]],
    [sn,ST1]
    [fr,ST2],
    R).
/* useful predicates */

change(CH,T,T,CH):- !, change(CH,ST,[OP,T;TS],[OP,R;TS]):= change(CH,ST,T,R), change(CH,ST,[OP,T;TS],[OP,T;R]):= change1(CH,ST,TS,R).

change1(CH,ST,[T;TS],[R;TS]): change(CH,ST,T,R), change1(CH,ST,[T;TS],[T;R]):= change1(CH,ST,TS,R).

/* Sentences */

frase([eu,fass,ver,or,rapaz,or,rapaz,fass,comprar,ro,livro]).

E&ROBLEM 94

Verbal statement:

Write a program able to interpret document titles and to be included in a question-answering system, due to implement an automatic library service.

The program goal consists of proposing categories to the user by reading the document titles, and interpreting the role played by prepositions.

Consider the following title:

"Logic for problem solving".

Logic program:

/*+++++++++++++++++++++++++++++++*/ /* TITLE INTERPRETATION */ /*+++++++++++++++++++++++++++++++*/

:-op(400,xfy, '~/').

/* Using the title definition of a text for classification purposes */

/* Grasping meaning for the title entities of a document */

parser(T,C):-
title(Out,T,[[]]),semant(Out,C1,C2),
output(C1,C2),append(C1,C2,C).

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output([],[]):-!.
output([],C2):-display('I recommend as categories: '),
                   print_ph(C2),nl!,
output(C1,C2):-display('I recommend as categories: ')
                   print_ph(C1),display('and '),print_ph(C2),nl.

/* Basic grammar rules governing the title construction */

title([np(X),Y,Z]) --> bp(X,Y),!,title(Z),
title([np(X)]) --> np(X).

bp([],P) --> prep(P),
bp([Y:L],P) --> det(Y),!,bp(L,P),
bp([n(X):Y],P) --> [X],bp(Y,P).
	np([Y:L]) --> det(Y),!,np1(L),
	np(X) --> np1(X),
	np1([n(X):Y]) --> [X],np1(Y),

/* Dictionary: lexical units */

prep(prep(for)) --> [for],
det([a]) --> [a],
det([an]) --> [an],
det([the]) --> [the].

/* Prepositional cases: ordering plans for conversation */

prep_case(for,X,Y):-
   assert(case(tool->X,ap|lication->Y)),nl,nl,
   write('your document deals with '),
   print_ph(X),write(''),
   write('as a tool'),nl,
   write('with the objective to contribute to '),
   print_ph(Y),write(''),nl,nl,hypothesis1(X,Y).

hypothesis1(X,Y):-
   write('My first hypothesis for classifying it '),
   write('is to take its nouns as hints'),
   nl,write('So '),print_ph(X),write(''),
   write('will drive us, in order '),
   write('to attain the main category, and'),
   nl,write(''),print_ph(Y),
   write(''),write('towards other categories'),nl,nl.
/* Gathering of clues, given by user, for classifying a document */

semant([np(X)], X, Y).
semant([np(X), prep(Y), [np(Z)]], W, T):-
    list_nouns(X, Z, U, V),
    pre_case(Y, U, V),
    drive_in(W, T).

/* Driving the conversation about title content */

drive_in(W, V):- case(X, Y),
    drive(X, U), drive(Y, V), test(X, U, W),
    drive(X->Y, C):- move(X, Y), plan(X, L), state(X, L, C), !,
    drive(X->Y, []).

move(X, Y):- write('Do you want to follow the idea that '),'print_ph(Y), write('is an AI'),
    write(X), write(?), nl, agreement(yes),
    write('OK. Let us talk about this hypothesis'),
    write(' and fix the kind of '),
    write(X), write(!), nl, !.

agreement(Input):- read(Input).

state(_, [], []):- !.
state(A, X, Y):-
    write('During our dialogue I grasp the following: '), nl,
    print_ph(X), write(' as core topics of your text: '), nl,
    under(A, X, Y), state1(Y), nl, !.

state1([]):- !.
state1(Y):- write('So I conclude it may be under '),
    write(' the categories: '),
    print_ph(Y).

under(A, [X:L], [N:NL]):- choose(A, X, N), under(_, L, NL),
    under(_, [], []).

choose(tool, X, Y):- g_tool(X, Y).
choose(application, X, Y):- g_application(X, Y).
choose(_, _, []).
/\* Plan 1: through the tree of tools */

plan(tool,L):-
  try(t([techniques,programming_languages],
    [t([reasoning,representational,searching],
    [t([puzzle_solving,question_answering,common_sense],
    [t([deduction,planning],[[]],[[])]),
    t([predicate_calculus,semantic_nets],[[]],[[])]),
    t([state_space,problem_reduction],[[]],[[])]),
    t([numerical_languages,ai_languages],[[]],
    t([list_type,predicate_logic_type],[[]],[[])]),L,tool]),!).

/\* Plan 2: through the tree of applications */

plan(application,L):-
  try(t([cognition,other_fields],[t([activities,abilities],
    t([intellectual_skills,motor_skills],
    t([playing,proving],[[]],
    t([theorems,programs],[[]],[[])],[[])]),
    t([language,vision],[[]],[[])],[[])],L,application),

  try(t([X:_,[T:_,]),[X:L],C):-
    request(X,C),!,try(T,L,C),

  try(t([_[X:TN],_[TN]],L,C):-try(t(XN,TN),L,C),

  try(_,[_,_],).

request(X,C):-write('Is '),write(X),
  write(' an adequate '),write(C),
  write(' worked out in your text?'),nl,
  agreement(yes).

/* testing return to a previous conversation */

test(X->Y,[Z],Z):-
  write('As no conclusion was taken about core topics of '),
  write(X),nl,
  write('I suggest we restart our conversation!'),
  nl,write('Do you agree?'),nl,
  agreement(yes),
  test(_,Y,Y).

Execution:

:-parser.

Document title?
[logic,for,problem-solving].

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Your document deals with 'logic' as a tool, with the objective to contribute to 'problem solving'.

My first hypothesis for classifying it is to take its nouns as hints. So 'logic' will drive us, in order to attain the main category, and 'problem solving' towards other categories.

Do you want to follow the idea that logic is an AI tool? yes.
Ok. Let us talk about this hypothesis and fix the kind of tool! Is techniques an adequate tool worked out in your text?
yes.
Is reasoning an adequate tool worked out in your text? yes.
Is puzzle-solving an adequate tool worked out in your text? no.
Is question-answering an adequate tool worked out in your text? no.
Is common-sense an adequate tool worked out in your text? no.
During our dialogue I grasp the following: techniques reasoning as core topics of your text. So I conclude it may be under the categories: [] 364

Do you want to follow the idea that 'problem solving' is an AI application?
Ok. Let us talk about this hypothesis and fix the kind of application!
Is cognition an adequate application worked out in your text? yes.
Is activities an adequate application worked out in your text? no.
Is abilities an adequate application worked out in your text? yes.
Is language an adequate application worked out in your text? yes.
During our dialogue I grasp the following: cognition abilities language as core topics of your text. So I conclude it may be under the categories: [] 336 365
I recommend as categories: [] 364 and [] 336 365

PROBLEM 95

Verbal statement:

Write a program to generate the deep structure (tree) of a natural language sentence.

Logic program:

\[
sentence(s(T1, T2)) \rightarrow noun\_phrase(T1), 
verb\_phrase(T2).
\]
nounPhrase(np(T1,T2)) \rightarrow\text{determiner}(T1),\text{noun}(T2).

verbPhrase(vp(T1,T2)) \rightarrow\text{verb}(T1),\text{nounPhrase}(T2).

determiner(det(the)) \rightarrow [\text{the}].
determiner(det([])) \rightarrow [].

noun(n(john)) \rightarrow [\text{John}].
noun(n(cake)) \rightarrow [\text{cake}].

verb(v(ate)) \rightarrow [\text{ate}].
3.8 GRAPH THEORY (nos. 96 to 100)

PROBLEM 96

Verbal statement:

Find a path from A to Z in the following directed graph (Figure 17).

![Graph Diagram]

Figure 17

Logic program:

\[
\text{go}(X,Y) :- \text{go}(X,Z), \text{write}('Path!'), \text{nl}, \text{write}((X,Z)), \\
\text{go}(Z,Y), \text{write}((Z,Y)), \text{nl}
\]

\[
\text{go}(a,b), \quad \text{go}(x,z), \\
\text{go}(a,c), \quad \text{go}(y,z), \\
\text{go}(b,d), \quad \text{go}(u,y), \\
\text{go}(b,e), \quad \text{go}(v,y), \\
\text{go}(e,x).
\]

Execution:

\[-\text{go}(a,z).\]
PROBLEM 97  [EMDEN, 1976e]

Verbal statement:

Let the interpretation I be

\(<G(A,B), G(A,C), G(A,D), G(B,F), G(C,F), G(E,F), G(F,C)\>\)

![Diagram](image)

Figure 18

Calculate:

- \(Q_1 = G(x_1, x_2) \land G(y_1, y_2)\)
- \(Q_2 = G(x, y) \land G(y, z)\)
- \(Q_3 = G(x, x)\)
- \(Q_4 = \exists y . G(x, y)\)
- \(Q_5 = \exists y . G(x, y) \land G(y, z)\)

Logic program:

\(a1(X_1, X_2, Y_1, Y_2) \vdash s(X_1, X_2), s(Y_1, Y_2)\).
\(a2(X, Y, Z) \vdash s(X, Y), s(Y, Z)\).
\(a3(X) \vdash s(X, X)\).
\(a4(X) \vdash s(X, \_2)\).
\(a5(X, Z) \vdash s(X, Y), s(Y, Z)\).

\(s(a, b), s(a, c), s(a, d),
\(s(b, f), s(c, f), s(e, f), s(f, c)\).

\(\text{answer 1}: - a1(X_1, X_2, X_3, X_4),
\text{write}((X_1, X_2, X_3, X_4)), n1.
\text{answer 1}.\)
PROBLEM 98  [SZEREDI, 1977]

Verbal statement:

Construct a program for drawing a picture (a graph), such as Figure 19, using a continuous line.

![Graph Image]

Figure 19

Logic program:

\[-op(600,xy,\sim).\]

\[
\text{draw}(G,[P,Q[L]]):- \text{choose}(G,P-Q,G1),
\text{draw}(G1,[Q:L]).
\]

\[
\text{draw}([], []).
\]

\[
\text{choose}([P-Q:L],[P-Q,G]).
\]

\[
\text{choose}([P-Q:L],[Q-P,G]).
\]

\[
\text{choose}([E:L1],[E:L11])\vdash \text{choose}(G,F,G1).
\]

Execution:

\[-\text{draw}([a-b,a-c,a-d,b-c,b-d,c-d,c-e,d-e,L]),
\text{output}(L).\]

The result is output on line-printer by execution of procedure output to be specified.
PROBLEM 99

Verbal statement:

It is required a graph generator able to:

1) generate all possible graphs with one-way edges from an initial given graph;

2) fix some nodes for each generated graph, i.e. erase the edges connecting to those nodes;

3) determine the end nodes;

4) determine which nodes (and their number) may attain the previous end nodes.

Logic program:

begin:- display('list of nodes ?'), nl, read(L), record(nds(L)),
       display('list of edges ?'), nl, read(X), record(ed(X)),
       display('list of relevant origin ?'), nl, read(Y),
       record(or(Y)), matizes.

matrix:- recorded(ed(L), Pt), erase(Pt), compact(L, L1),
        calc(L1), fail.
matrix:- display('Done, '), nl, nl, nl.

compact([], []). compact([m(X,Y);B], R):- in(m(X,Y), B, D), !,
                                        (R=[m(X,Y);C] ; R=[m(Y,X);C]),
                                        compact(D, C).
compact([A1:B], [A1:C]) :- compact(B, C).

in(m(A,B), [m(B,A);X], X).
in(m(A,B), [C;X],[C;R]) :- in(m(A,B), X, R).

calc(L1) :- ?or(Y), in(A, Y), name(A, A1),
        X=[78, 79, 46|A1], name(X1, X), tell(X1),
        slash(out_of_list(A1, L1, L2)), ?nds(L),
        slash(look(L, L2, L3)), calcul(L2, L3).

calcul(L2, L3) :- in(B, L3),
                 test(B), complete(L2, B).

complete(L2, B) :- ?nds(L), oris(L2, B, L, 0), length(0, No), put( ' '),
                  test(No), output(0), nl, !.

oris(L2, B, [N|Ns], [N|N0]) :- path(N, B, L2),
oris(L2, B, [N|Ns], [N|N0]) :- path(N, B, L2),
oris(L2, B, Ns, 0).
oris(L2, B, L, [Ns|N0]) :- oris(L2, B, Ns, 0),
oris(_, _, []) !- oris(L2, B, Ns, 0).

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slash(P) :- call(P), !.

Path(A, B, L) :- in(m(A, B), L).
Path(A, B, L) :- in(m(A, C), L), slash(out_of_list(C, L, L1)), Path(C, B, L1).
out_of_list(A, [m(\_, A); X], Y) :- out_of_list(A, X, Y).
out_of_list(A, [B; X], [B; Y]) :- out_of_list(A, X, Y).
out_of_list(\_, [\_; \_])
look([N; Ns], L2, Y) :- in(m(N, \_), L2), look(Ns, L2, Y).
look([N; Ns], L2, [N; Y]) :- in(m(\_, N), L2), look(Ns, L2, Y).
look([N; Ns], L2, Y) :- look(Ns, L2, Y).
look([\_; \_; \_])
in(A, [A; \_]),
in(A, [\_; B]) :- in(A, B).

output([A]) :- put(" * "), test(A).
output([A; B]) :- put(" * "), test(A), output(B).

test(A) :- A<10, put(" * "), write(A), !.
test(A) :- write(A), !.

PROBLEM 100

Verbal statement:

Write a program to test connections between nodes in a given graph. Apply your program to the graph in Figure 20 in order to test connections between A and D, and A and E.

![Figure 20](image-url)

**Figure 20**

Remark: This problem exemplifies the use of 'ancestors'. Observe that your program must prevent loops caused by the circuits of the graph. Use the built-in procedure "ancestors".
Logic program:

Program 1:

/* connections test */
connections(X,Y):- connections(X,Y),
connections(Y,X),
write('yes,'),nl.
connections(_,_):- write('no,'),nl.

connected(X,Y):- ancestors(L),
in2(connected(X,Y),L),!/fail.
connected(X,Y):- edge(X,Y).
connected(X,Y):- edge(X,Z),connected(Z,Y).

in2(A,[A|B]):- in(A,B).
in2(A,[_|B]):- in2(A,B).
in(A,[A|_]),
in(A,[_|B]):- in(A,B).

/* Graph description */

edge(a,b),
edge(b,c),
edge(e,d),

Program 2:

/* connection test */

connections(X,Y):(connected(X,Y),connected(Y,X)),
write('yes,'),nl.
connections(_,_):- write('no,'),nl.

connected(X,Y):- edge(X,Y).
connected(X,Y):- edge(X,Z),
(subgoal_of(connected(Z,Y)),!/fail; connected(Z,Y)).

/* Graph description */

edge(a,b),
edge(b,c),
edge(e,d),

edge(d,a),
edge(e,b).

Execution:

:-connections(a,d).

yes.

:-connections(a,e).

no.
PROBLEM 101

Verbal statement:

Specify the differentiation function.

Logic program:

:- op(700,xfx,!).
:- op(500,xfy,[+,-]).
:- op(400,xfy,[*,#]).
:- op(300,xfy,@).  % xfy(A,B,C) :- A=@ B C
:- op(300,fy,[-,exp,log,sin,cos,tan]).

dv!-repeat,read(T),( T=stop ; derive(T),fail).

derive(T:X) :- T : X, !.

X : [V] :- X : V.

X : [U;V] :- d(X;U,W), simplify(W,Z), Z : V.

X : Y :- d(X,Y,W), simplify(W,Z),

    ttypn1, output(Z), ttypn1, ttypn1.

    d(X,X,1).

    d(T,X,0)!- atom(T) ; number T.

    d(U+V,X,A+B) :- d(U,X,A), d(V,X,B).

    d(U-V,X,A+(-B)) :- d(U,X,A), d(V,X,B).

    d(-T,X,-R)!- d(T,X,R).

    d(K*X,X,K+W) :- number K, d(U,X,W).


    d(U/V,X,W) :- d(U*V@(-1),X,W).

    d(U@V,X,V*W@U@V(V+(-1))) :- number V, d(U,X,W).

    d(U@V,X,Z*log(U)*U@V+V*W@U@V(V+(-1))) :-


    d(log T,X,R*T@(-1)) :- d(T,X,R).
d(exp T,X,R*exp T):- d(T,X,R).
d(sin T,X,R*cos T):- d(T,X,R).
d(cos T,X,-R*sin T):- d(T,X,R).
simplify(X,X):- atomic(X).
simplify(X,Y):- X =..[Op,Z], simplify(Z,Z1), rewrite(Op,Z1,Y).
simplify(X,Y):- X =..[Op,Z,W], simplify(Z,Z1), simplify(W,W1), rewrite(Op,Z1,W1,Y).
rewrite(-A+B,C+D):- unary(-A,C), unary(-B,D).
rewrite(X,Y,Z):- unary(X,Y,Z).
rewrite(@,Y*X@(-1),-Z,W):- binary(@,Y*X@(-1),Z,W).
unary(-,X,X).
unary(-,0,O).
unary(-,X,Y):- Y is X.
unary(log,1,0).
unary(sin,0,1).
unary(cos,0,1).
unary(Op,X,Y):- Y =..[Op,X].

binary(+,X,0,X).
binary(+,X,-X,0).

binary(+,A+B+C,R+C):- R is A+B.
binary(+,A+B+C,R+B):- R is A+C.
binary(+,(sin X)@2,(cos X)@2,1).
binary(+,(cos X)@2,(sin X)@2,1).
binary(+,X,Y,Z):- Z is X+Y.
binary(+,A,B,B+A):- number B.

binary(*,X,1,X).
binary(*,0,-,0).
binary(*,-1,X,-X).
binary(*,X@(-1),1).

binary(*,A*B,C,R*C):- R is A*B.
binary(*,A*B,C,R*B):- R is A*C.
binary(*,X,Y,Z):- Z is X*Y.
binary(*,A,B,B*A):- number B.

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binary(0,1,_,1).
binary(0,X,1,X).
binary(0,_,0,1).

binary(0P,X,Y,Z):- Z =..[0P,X,Y].

output(X):- clean(X,Y), write(Y).

clean(X,X):- atom(X); number X.
clean(X,Y):- X =..[0P,Z], clean(Z,Z1), Y =..[0P,Z1],
clean(X,Y):- X =..[0P,Z,W], clean(Z,Z1), clean(W,W1),
U =..[0P,Z1,W1], change(U,Y).

change(-1+X,X-1).
change(X+(Y),X-Y).
change(X*Y@(-1),X/Y).
change(X@(-1)*Y,Y/X).
change(X,X).

PROBLEM 102 [EMDEN, 1976c]

Verbal statement:

Define the exponentiation function:

\[
\exp(x,y,z) \text{ iff } x = z
\]

The following properties of integer exponentiation are taken as the defining ones:

\[
x = 1 \text{ i.e. } x \exp(x,0,1)
\]

and

\[
x = x \times x \text{ i.e. } x \times y \times z \exp(x,y-1,z) = \exp(x,y,x,z)
\]

It is taken for granted that the following defining property can be added without altering the relation defined and yet making the definition more efficient:

\[
x = (x) \text{ i.e. } x = (x) \text{ i.e. } x \times y \times z \exp(x,x,y/2,z) \text{ even}(y) = \exp(x,y,z)
\]

Logic Program:

\[
\exp(X,0,1).
\exp(X,Y,Z) :- \text{even}(Y), R \text{ is } Y/2, P \text{ is } X \times X,
\exp(P,R,Z).
\exp(X,Y,Z) :- R \text{ is } Y-1, \exp(X,T,Z1), Z \text{ is } Z1 \times X.
\text{even}(Y) :- R \text{ is } Y \text{ mod } 2, R = 0.
\]
Execution:
\[ \text{:- exp}(2,10,Z), \text{write}(Z), \text{nl}. \]
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PROBLEM 103

Verbal statement:
Write a program describing the Fibonacci function.

Logic program:
\[
\begin{align*}
\text{fib}(0,1), \\
\text{fib}(1,1), \\
\text{fib}(X,F) :- Z \text{ is } X-2, \ Y \text{ is } Z+1, \ \text{fib}(Y,Y1), \text{fib}(Z,Z1), \\
& \quad \text{F is } Y1+Z1.
\end{align*}
\]
3.10 ARITHMETIC  (nos. 104 to 116)

PROBLEM 104
Verbal statement:
Find the absolute value of an integer.
Logic Program:
\[
\begin{align*}
\text{abs}(X,X) &: X \geq 0, \\
\text{abs}(X,Y) &: Y \text{ is } -X.
\end{align*}
\]

PROBLEM 105
Verbal statement:
Define factorial.
Logic Program:
\[
\begin{align*}
\text{factorial}(0,1) & , \\
\text{factorial}(N,F) &: M \text{ is } N-1, \text{factorial}(M,G), \\
& F \text{ is } N\times G.
\end{align*}
\]
Execution:
\[
:-\text{factorial}(10,Y),\text{write}(Y),\text{nl}.
3628800
\]

PROBLEM 106
Verbal statement:
Define factorial with recursion on the right.
Logic Program:
\[
\begin{align*}
\text{factorial2}(N,F) &: \text{fact}(N,1,F), \\
\text{fact}(0,F,F), \\
\text{fact}(N,X,F) &: M \text{ is } N-1, Y \text{ is } X\times N, \\
& \text{fact}(M,Y,F).
\end{align*}
\]

PROBLEM 107  [CLARK & KOWALSKI 1977]

Verbal statement:
Define factorial in a bottom-up way.

Logic program:

\[ \text{fact}(U,FU) :- \text{bufact}(0,1,U,FU). \]
\[ \text{bufact}(X,FX,X,FX). \]
\[ \text{bufact}(X,FX,U,FU) :- \text{NX is X+1, FNX is NX*FX,} \]
\[ \text{bufact}(NX,FNX,U,FU). \]

PROBLEM 108  [adapted from BRUYNOOGHE 1978]

Verbal statement:
Generate primes in first N integers and call them \text{primes}(N,CP).

Logic program:

\[ \text{primes}(N,[1;LP]) :- M \text{ is } N-1, \]
\[ \text{integers}(2,M,LI), \]
\[ \text{sift}(LI,LP). \]
\[ \text{integers}(N,0,[N]). \]
\[ \text{integers}(N,M,[N;LI]) :- R \text{ is } M-1, \]
\[ Q \text{ is } N+1, \]
\[ \text{integers}(Q,R,LI). \]
\[ \text{sift}([],[]). \]
\[ \text{sift}([P;LI],[P;LP]) :- \text{filter}(P,LI,NLI), \]
\[ \text{sift}(NLI,LP). \]
\[ \text{filter}(P,[]). \]
\[ \text{filter}(P,[N;LI],[N;NL;LI]) :- \text{divide}(P,N,\text{false}), \]
\[ \text{filter}(P,LI,NLI). \]
\[ \text{filter}(P,[N;LI],NL;LI) :- \text{divide}(P,N,\text{true}), \]
\[ \text{filter}(P,LI,NLI). \]
\[ \text{divide}(P,N,\text{true}) :- 0 \text{ is } N-P*(N/P). \]
\[ \text{divide}(P,N,\text{false}). \]

The method is the 'sieve of Erastosthenes'. It consists in generating the list of integers from 2 to \(M\), and in deleting from that list all the integers multiple of some element in the list.
PROBLEM 109

Verbal statement:

Define Euclid's algorithm: maximum common divisor and minimum common multiple.

Logic program:

\[
\text{gcd}(N, 0, N), \\
\text{gcd}(N, M, D):= \text{R is } N \mod M, \text{gcd}(M, R, D), \\
\text{lcm}(N, M, E):= \text{gcd}(N, M, D), E \equiv (N \times M)/D.
\]

PROBLEM 110

Verbal statement:

Define the roman to arabic number conversion.

Logic program:

\[
\text{convert}:= \text{repeat, read(R), (R == stop, roman(R), fail). } \\
\text{roman}(R):= \text{roman}(D, R, [], !, !, n1, } \\
\text{write(D), n1, n1.} \\
\text{roman}(R) \rightarrow \text{value}(X), \text{value}(Y), (X < Y), \\
\text{roman}(R1), \{ R \equiv Y - X + R1 \}, \\
\text{roman}(R) \rightarrow \text{value}(X), \text{roman}(R1), \{ R \equiv X + R1 \}. \\
\text{roman}(0) \rightarrow [ ]. \\
\text{value}(1) \rightarrow 'I', \\
\text{value}(5) \rightarrow 'V', \\
\text{value}(10) \rightarrow 'X', \\
\text{value}(50) \rightarrow 'L', \\
\text{value}(100) \rightarrow 'C', \\
\text{value}(500) \rightarrow 'D', \\
\text{value}(1000) \rightarrow 'M'.
\]

PROBLEM 111

Verbal statement:

Compute the maximum of two numbers.

Logic program:

\[
\text{max}(X, X, X), \\
\text{max}(X, Y, Y):= X < Y, \\
\text{max}(X, Y, X):= Y < X.
\]

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PROBLEM 112

Verbal statement:
Define an arithmetic for rational expressions.

Logic program:

/* Package 1 : A and B non negative integers */

rinf(A,B):- somreel(B,-A,C),signal(C,1).

rdiff(A,B):- equal(A,B),!,fail.
rdiff(A,B).

absdiff(X,Y,Z):- rinf(X,Y),!,somreel(Y,-X,Z).
absdiff(X,Y,Z):- somreel(X,-Y,Z).

somreel(A,B,C):- decom$p(A,S1,A1,A2),
decom$p(B,S2,B1,B2),
ppcm(A2,B2,F,A12,B12),
N1 is A1*A12,N2 is B1*B12,
som(S1,N1,S2,N2,S,N),
pgcd(N,F,D,H,K),
decom$p(C,S,H,K).

som(S,A,S1,A1,1,0):- S==S1,!,
som(S,A,S,B,S,C):- !, C is A+B,
som(S,A,S1,B,S,C):- B<A,!,C is A-B,
som(S,A,S1,B,S1,C):- C is B-A.

subreel(-A,-B,C):- !,somreel(-A,B,C).
subreel(-A,B,C):- !,somreel(-A,-B,C).
subreel(A,-B,C):- !,somreel(A,B,C).
subreel(A,B,C):- !,somreel(A,-B,C).

prodreel(A,B,C):- decom$p(A,S1,A1,A2),
decom$p(B,S2,B1,B2),
sisprod(S,S2,S),
C1 is A1*B1,C2 is A2*B2,
pgcd(C1,C2,D,C11,C12),
decom$p(C,S,C11,C12).

divreel(A,B,C):- decom$p(A,S1,A1,A2),
decom$p(B,S2,B1,B2),
sisprod(S1,S2,S),
N1 is A1*B2,D1 is A2*B1,
pgcd(N1,D1,G,N,D),
decom$p(C,S,N,D).

sisprod(S,S,1):- !.
sisprod(S,S,1,-1).

pgcd(A,B,C,D,E):- B<A,!,pgcd(A,B,C),
D is A/C,E is B/C.
\[ \text{pscd}(A, B, C, D, E) \overset{\text{s}}{\Rightarrow} \text{scd}(B, A, C), \]
\[ D \text{ is } A/C, \ E \text{ is } B/C. \]
\[ \text{scd}(A, 0, A) \overset{\text{!}}{\Rightarrow} \]
\[ \text{scd}(A, B, D) \overset{\text{C is } A \mod B}{\Rightarrow} \text{scd}(B, C, D). \]
\[ \text{ppcm}(A, B, P, C, E) \overset{\text{pscd}(A, B, D, E, C)}{\Rightarrow} \]
\[ Q \text{ is } A*B, \ P \text{ is } Q/D. \]
\[ \text{signal}(\sim A, -(1)) \overset{\text{!}}{\Rightarrow} \text{signal}(A, 1), \]
\[ \text{signal}(\sim A, 1) \overset{\text{!}}{\Rightarrow} \text{fail}, \]
\[ \text{signal}(A, -(1)) \overset{\text{!}}{\Rightarrow} \text{fail}, \]
\[ \text{signal}(0, 0) \overset{\text{!}}{\Rightarrow} \]
\[ \text{signal}(0, 1) \overset{\text{!}}{\Rightarrow} \text{fail}, \]
\[ \text{signal}(A, 1). \]
\[ \text{decomp}(\sim A, -S, A1, A2) \overset{\text{!}}{\Rightarrow} \text{decomp}(A, S, A1, A2), \]
\[ \text{decomp}(A \setminus B, 1, A, B) \overset{\text{B==1, !}}{\Rightarrow} \]
\[ \text{decomp}(A, 1, A, 1). \]
\[ \text{equal}(A, A) \overset{!}{\Rightarrow} \]
\[ \text{equal}(A, B) \overset{\text{somreel}(A, -B, C)}{\Rightarrow} \]
\[ \text{somreel}(C, -(1\setminus1000), R1), \]
\[ \text{somreel}(C, 1\setminus1000, R2), \]
\[ \text{signal}(R1, -(1)), \]
\[ \text{signal}(R2, 1). \]

```c
/* Package 2 */

:-op(700,xfy,[[isr,norms_to,denorms_to]]).
:-op(300,xfy,^).

X isr Y :- rat(Y,X),!.

rat(U+V,W) :- integer(U),integer(V),W is U+V;
rat(U,X) :- rat(V,Y),
X norms_to X1/X2,Y norms_to Y1/Y2,
1cm(X2,Y2,F,X12,Y12),
Z is X1*X12+Y1*Y12,
scd(Z,F,_,W1,W2),
W1/W2 denorms_to W.

rat(U*V,W) :- integer(U),integer(V),W is U*V;
rat(U,X) :- rat(V,Y),
X norms_to X1/X2,Y norms_to Y1/Y2,
Z1 is X1*Y1,Z2 is X2*Y2,
scd(Z1,Z2,_,W1,W2),
W1/W2 denorms_to W.

rat(-U,V) :- integer(U),V is -U;
rat(U,V),
U norms_to U1/U2,V1 is -U1,
V1/U2 denorms_to V.
rat(U-V,W) :- rat(-V,V1),rat(U+V1,W),
rat(U/V) :- rat(U,V).
```
rat(U/V,W):- rat(U,X),rat(V,Y),
  X norms_to X1/X2,Y norms_to Y1/Y2,
  sign(Y1,S,A),
  Z1 is X1*Y2*S,Z2 is X2*A,
  scd(Z1,Z2,_,W1,W2),
  W1/W2 denoms_to W.
rat(U/V,W):- rat(V,Y),integer(Y),
  rat(U,X),X norms_to X1/X2,
  sign(Y1,_,E),expt(X1,E,Z1),expt(X2,E,Z2),
  (Y<0,sign(Z1,S,W1),W2 is S*Z2,W2/W1 denoms_to W; Z1/Z2 denoms_to W).
rat(U,U):- integer(U).
X norms_to X/1:- integer(X),!.
X/Y norms_to X/Y:- integer(X),integer(Y),Y>0.
X/1 denoms_to X/-!.
X denoms_to X.
number(X):- X norms_to _.
sign(X,S,A):- X<0,!,S is -1,A is -X.
sign(X,1,X).
1cm(A,B,F,C,E):- scd(A,B,D,E,C),F is A*B/D.
scd(A,B,D,E):- sign(A,_,A1),sign(B,_,B1),
  (B1<A1,!,scd1(A1,B1,C);
   scd1(B1,A1,C)),
  D is A/C,E is B/C.
scd1(A,0,A):- !.
scd1(A,B,D):- C is A mod B,scd1(B,C,D).
expt(X,1,X):- !.
expt(_,0,1):- !.
expt(1,_,1).
expt(X,E,Y):- even(E),E1 is E+1,expt(X,E1,Y1),Y is Y1*Y1;
  E1 is E-1,expt(X,E1,Y1),Y is X*Y1.

PROBLEM 113

Verbal statement:

Consider Spencer Brown's 'The laws of form' (Bantam Books,1973) and write a program to implement his primary arithmetic (ps.12-24).

Logic program:
:- op(500,'xfy',[\$]).
read! = repeat, read(X),
  (X = end; value(X,Y,Why),
   tttynl,ttynl,display(’one has proved ’),
   value_is(X,Y,Why),
   tttynl,ttynl,ttynl,fail).

value([[]],0,cancel):- !,
value([[]],[[]],condense):- !.

value(0;0,0,...):- !,
value(0;[[]],[[]]):- !,
value([[]];0,[[]]):- !,
value([[]],[[]];0):- !,
value([0],[[]];0):- !,
value(0;0,...):- !.

value(X;Y,Z,...):- value(X,XX,Why),
  value(Y,YY,Why2),
  value(XX;YY,Z,...),
  since, value_is(X,XX,Why),
  and, value_is(Y,YY,Why2),
  value_is(X;Y,Z,...).

value([X];Y,...):- value(X,Z,Why),value([Z];Y,...),
  since, value_is(X,Z,Why),value_is([X];Y,...),
  since:- tttynl,ttynl,display(’since ’),
  and:- tttynl,display(’and ’),
  value_is(X,Y,Why):- (Why = not_given;
    Why = cancel,display(’by cancellation’);
    Why = condense,display(’by condensation’)),
    !,tttynl,
    show(X),display(’ ’),show(Y).

show(0):- !,
show(X;Y):- !,show(X),display(’;’),show(Y),
show([X]):- !,display(’[’),show(X),display(’]’),
show(X):- display(X).

PROBLEM 114

Verbal statement:

Write an adder for numbers with twenty digits.

Consider: 34832965 + 12469328.

(Suggestion: Consider the number 34832965 as n(0,0,3483,2965))
Logic program:

```prolog
adder(n(A1,B1,C1,D1),n(A2,B2,C2,D2)): -
    X is (D1 + D) / 100000, B2 is (D1+D) mod 100000,
    Y is (C1 + C + X) / 100000, C2 is (C1+C+X) mod 100000,
    Z is (B1+B+Y) / 100000, B2 is (B1+B+Y) mod 100000,
    A2 is A1+A+Z.
```

Execution:

The result is 47302293 (that is n(0,0,4730,2293))

**Problem 115**

Verbal statement:

Write a multiplier for numbers with different number of digits.

Logic program:

```prolog
product(n(R1,R2,R3,R4),Pt,t(A,B),Rt,n(Nr1,Nr2,Nr3,Nr4)): -
    N1 is (Pt*Rt) mod 100000, N2 is (Pt*Rt) / 100000,
    P1 is (A*N1) mod 100000, P2 is (A*N1) / 100000,
    P3 is (A*N2) mod 100000, P4 is (A*N2) / 100000,
    P5 is (B*N2) mod 100000, P6 is (B*N2) / 100000,
    P7 is (A*N2) mod 100000, P8 is (A*N2) / 100000,
    Nr4 is (P1*R4) mod 100000, T3 is (P1+R4) / 100000,
    Nr3 is (T3+P2+P3+P5+R3) mod 100000,
    T2 is (T3+P2+P5+R3) / 100000,
    Nr2 is (T2+P4+P6+P7+R2) mod 100000,
    T1 is (T2+P4+P6+P7+R2) / 100000,
    Nr1 is T1+P8+R1.
```

**Problem 116**

Verbal statement:

Specify the distribution of '*' by '+'.

Logic program:

```prolog
multiply(X+Y,Z,X1+Y1): - multiply(X,Z,X1),
                        multiply(Y,Z,Y1).
multiply(Z,X+Y,X1+Y1): - multiply(Z,X,X1),
                        multiply(Z,Y,Y1).
multiply(X,Y,X*Y).
```
3.11 MISCELLANEOUS (nos. 117 to 120)

PROBLEM 117 [PEREIRA et al, 1978]

Verbal statement:

Write a PROLOG interpreter in PROLOG, and illustrate the use of a variable goal.

In this mini-interpreter, goals and clauses may be represented as ordinary PROLOG data structures (i.e., terms). Terms representing clauses may be specified using the unary predicate 'clause', e.g.,

\[
\text{clause( (grandparent(X,Z):- parent(X,Y),parent(Y,Z) ) )}
\]

A unit clause may be represented by a term such as:

\[
( \text{parent(John,mary):- true})
\]

Logic program:

\[
\begin{align*}
\text{execute}(true):- !, \\
\text{execute}(P,Q):- !, \text{execute}(P), \text{execute}(Q), \\
\text{execute}(P):- \text{clause}((P:Q)), \text{execute}(Q), \\
\text{execute}(P):- P.
\end{align*}
\]

PROBLEM 118

Verbal statement:

Extend the mini-interpreter considered in the previous problem, in order to deal with the 'cut' symbol.

Logic program:

\[
\begin{align*}
\text{execute}(true,\_). \\
\text{execute}(!,\_). \\
\text{execute}(!,\text{cut}). \\
\text{execute}(P,Q,V):- !, \text{execute}(P,C), \\
\quad (C=\text{cut}, V=\text{cut} ; \\
\quad \text{execute}(Q,V)). \\
\text{execute}(P,V):- \text{clause}((P:Q)), \\
\quad \text{execute}(Q,V), \\
\quad (V=\text{cut}, !, \text{fail}; true). \\
\text{execute}(P,\_):- P.
\end{align*}
\]
PROBLEM 119  [PEREIRA et al, 1978]

Verbal statement:

Illustrate the use of the meta-predicates 'var' and '=='. The procedure call 'variables(Ierm, L, [])' instantiates variable L to a list of all the variable occurrences in the term Ierm. e.g. variables(d(U*V*X, DU*V+U*DV), [U, V, X, DU, V, U, DV], []).

Logic program:

variables(X,[X:L],L):- var(X),!.
variables(T,L0,L):- T == [F:A], variables1(A, L0, L).
variables1([T:A],L0,L):- variables(T, L0, L1), variables1(A, L1, L).
variables1([],L,L).

PROBLEM 120

Verbal statement:

Define conditional.

Logic program:

:- op(1050,xfy, '->').
(P -> Q; R):- P, !, Q, R.
(P; Q):- P.
(P; Q):- Q.
(P, Q):- P, Q.
true.
:- repeat, read(X), (X=end -> true;
   X -> write((Yes;)), fail,
   write((no;)), fail).

Execution:

24 > 23.
yes
23 > 23.
no
23 >= 23.
yes
end.
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## APPENDIX 1

### PROLOG IMPLEMENTATIONS

<table>
<thead>
<tr>
<th>Computer System</th>
<th>Programming Language</th>
<th>Implementation</th>
<th>Year</th>
<th>Authors</th>
<th>Site or University</th>
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{1} This version differs significantly from other systems in the control primitives.
# APPENDIX 2

## LIST OF PROLOG APPLICATIONS

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<th>AUTHORS</th>
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</table>
APPENDIX 3

PROLOG RELEVANT ADDRESSES

BUDAPEST

NIM IGUSZI
1363 Budapest
P.U.B. 33
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EDINBURGH

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Scotland

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Katholieke Univ.
Leuven
Belgium

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Laboratório Nacional de Engenharia Civil
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Portugal

LISBON

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Universidade Nova de Lisboa
Seminário dos Olivais
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Portugal
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England

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de Luminy
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13009 Marseille
France

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Department of Computer Science University of Stockholm
106 91 Stockholm
Sweden

WATERLOO

Computer Science Department University of Waterloo
Waterloo, Ontario
Canada
APPENDIX 4

PROLOG BUILT-IN PROCEDURES

Built-in procedures are also referred to as evaluable predicates.

4.1 INPUT / OUTPUT

A total of fourteen I/O streams may be open at any one time for input and output. An extra stream is available, for input and output to the user’s terminal. A stream to a file $F$ is opened for input by the first *(see(F))* executed. $F$ then becomes the current input stream. Similarly, a stream to file $H$ is opened for output by the first *(tell(H))* executed. $H$ then becomes the current output stream. Subsequent calls to *(see(F))* or to *(tell(H))* make $F$ or $H$ the current input or output stream, respectively. Any input or output is always to the current stream.

When no input or output stream has been specified, the standard ersatz file ‘user’, denoting the user’s terminal, is utilized for input and/or output. Terminal output is only displayed after a newline is written or ‘ttyflush’ is called. When the terminal is waiting for input on a new line, the prompt ‘!’ is displayed.
When the current input and/or output stream is closed, the user's terminal becomes the current input and/or output stream.

No file except the ersatz file 'user' can be simultaneously open for input and output.

A file is referred to by its name, written as an atom, e.g.,

myfile
'123'
'DATA.LST'
'DTA1:ABC.PL'

Note that reference to directories other than the user's is not possible at present.

consult(F)

Instructs the interpreter to read file F. When a directive is read it is immediately executed. When a clause is read it is put after any clauses already read by the interpreter for that procedure. The consulted file may define its own character convention ('LC' or 'NOLC') without affecting the convention prevailing outside.

reconsult(F)

Like 'consult' except that any procedure defined in the
"reconsulted" file erases any clauses for that procedure already present in the interpreter. 'reconsult', used in conjunction with 'save' and 'restore', facilitates the amendment of a program without having to consult again from scratch all the files which make up the program. The file 'reconsulted' is normally a temporary 'patch' file containing only the amended procedure(s). Note that it is possible to call 'reconsult(user)' and then enter a patch directly on the terminal (ending with '!-end,' or ^Z). This is only recommended for small, tentative patches.

see(F)

File F becomes the current input stream.

seeing(F)

F is unified with the name of the current input file.

seen

Closes current input stream.

tell(F)

File F becomes the current output stream.

telling(F)

F is unified with the name of the current output file.
told

Closes the current output stream.

close(F)

File F, currently open for input or output, is closed.

read(X)

The next term, delimited by a "fullstop" (i.e. a "." followed by <cr> or a space), is read from the current input stream and unified with X. The syntax of the term must accord with current operator declarations. If a call 'read(X)' causes the end of the current input stream to be reached, X is unified with the term "i-end." Further calls to 'read' for the same stream will then cause an error failure.

write(X)

The term X is written to the current output stream according to current operator declarations.

nl

A new line is started on the current output stream.
display(X)

The term X is displayed on the terminal in standard
parenthesised prefix notation.

ttynl

A new line is started on the terminal and the buffer is
flushed.

ttyflush

Flushes the terminal output buffer.

ttyset0(N)

N is the ASCII code of the next character input from the
terminal.

ttyset(N)

N is the ASCII code of the next non-blank printable
character from the terminal.

ttyskip(N)

Skips to just past the next ASCII character code N from the
terminal. N may be an integer expression.
**ttyput(N)**

The ASCII character code N is output to the terminal. N may be an integer expression.

**set0(N)**

N is the ASCII code of the next character from the current input stream.

**set(N)**

N is the ASCII code of the next non-blank printable character from the current input stream. N may be an integer expression.

**skip(N)**

Skips to just past the next ASCII character code N from the current input stream. N may be an integer expression.

**put(N)**

ASCII character code N is output to the current output stream. N may be an integer expression.

**tab(N)**

N spaces are output to the current output stream. N may be an integer expression.
putatom(X)

The name of atom X is output to the current output stream.

fileerrors

Undoes the effect of 'nofileerrors'.

nofileerrors

After a call to this predicate, the I/O error conditions
'incorrect file name...', 'can't see file...', 'can't tell
file...' and 'end of file...' cause a call to 'fail'
instead of the default action, which is to type an error
message and then call 'abort'.

rename(F,N)

If file F is currently open, closes it and renames it to N.
If N is '[]', deletes the file.

log

Enables the logging of terminal interaction to file
PROLOG.LOG. It is the default.

nolog

Disables the logging of terminal interaction.
Arithmetic is performed by built-in procedures which take as arguments integer expressions and evaluate them. An integer expression is a term built from evaluable functors, integers and variables. At the time of evaluation, each variable in an integer expression must be bound to an integer, or, for the interpreter ONLY, to an integer expression. Although Prolog integers must be in the range \(-2^{17}\) to \(2^{17}-1\), the integers in arguments to arithmetic procedures and the intermediate results of the evaluation may range from \(-2^{35}\) to \(2^{35}-1\).

Each evaluable functor stands for an arithmetic operation. The evaluable functors are as follows, where \(X\) and \(Y\) are integer expressions:

\[
\begin{align*}
X+Y & \quad \text{integer addition} \\
X-Y & \quad \text{integer subtraction} \\
X*Y & \quad \text{integer multiplication} \\
X/Y & \quad \text{integer division} \\
X \mod Y & \quad X \ modulo \ Y \\
-X & \quad \text{unary minus} \\
X\&Y & \quad \text{bitwise conjunction} \\
X\vert Y & \quad \text{bitwise disjunction}
\end{align*}
\]
\X \text{ bitwise negation}

X\ll Y \text{ bitwise left shift of } X \text{ by } Y \text{ places}

X\gg Y \text{ bitwise right shift of } X \text{ by } Y \text{ places}

!(X) \text{ the number in the range } 0 \text{ to } 2^{18}-1 
\text{ which is equal to } X \text{ modulo } 2^{18}

%(X) \text{ the number in the range } -2^{17} \text{ to } 2^{17}-1 
\text{ which is equal to } X \text{ modulo } 2^{18}

[X] \text{ evaluates to } X \text{ if } X \text{ is an integer}
\text{(therefore e.g. "A" behaves within arithmetic expressions as an integer constant which is the ASCII code for letter A)}

The arithmetic built-in procedures are as follows, where \( X \) and \( Y \) stand for arithmetic expressions, and \( Z \) for some term:

\( Z \) is \( X \)

Integer expression \( X \) is evaluated and the result, reduced modulo \( 2^{18} \) to a number in the range \( -2^{17} \) to \( 2^{17}-1 \), is unified with \( Z \). Fails if \( X \) is not an integer expression.

\( X:=:=Y \)

The values of \( X \) and \( Y \) are equal.
$X = \neq Y$

The values of $X$ and $Y$ are not equal.

$X < Y$

The value of $X$ is less than the value of $Y$.

$X > Y$

The value of $X$ is greater than the value of $Y$.

$X = \leq Y$

The value of $X$ is less than or equal to the value of $Y$.

$X \geq Y$

The value of $X$ is greater than or equal to the value of $Y$.

4.3 CONVENIENCE

$P, Q$

$P$ and $Q$

$P \lor Q$

$P$ or $Q$
true

Always succeeds.

X=Y

Defined as if by clause "Z=Z.".

length(L,N)

L must be instantiated to a list of determinate length. This length is unified with N.

4.4 EXTRA CONTROL

See Section 2.3.

not(P)

If the goal P has a solution, fail; otherwise succeed. It is defined as if by:

not(P) :- P, !, fail.
not(_).

Not yet available for compiled code.
\[ P \rightarrow Q ; R \]

Analogous to

'if \( P \) then \( Q \) else \( R \)'

ie. defined as if by:

\[ P \rightarrow Q ; R : - P, \!, Q. \]
\[ P \rightarrow Q ; R : - R. \]

Not yet available for compiled code.

\[ P \rightarrow Q \]

When occurring other than as one of the alternatives of a disjunction, is equivalent to:

\[ P \rightarrow Q ; \text{fail}. \]

Not yet available for compiled code.

repeat

Generates an infinite sequence of backtracking choices. It behaves (but doesn't use store!) as if defined by the clauses:

\[ \text{repeat.} \]
\[ \text{repeat : - repeat.} \]
fail

Always fails.

abort

Aborts the current execution.

4.5 META-LOGICAL

\texttt{var(X)}

Tests whether \( X \) is currently instantiated to a variable.

\texttt{nonvar(X)}

Tests whether \( X \) is currently instantiated to a non-variable term.

\texttt{atom(X)}

Checks that \( X \) is currently instantiated to an atom (ie. a non-variable term of arity 0, other than an integer).

\texttt{integer(X)}

Checks that \( X \) is currently instantiated to an integer.
atomic(X)

Checks that X is currently instantiated to an atom or integer.

X == Y

Tests if the terms currently instantiating X and Y are literally identical (in particular, variables in equivalent positions in the two terms must be identical).

X \not= Y

Tests if the terms currently instantiating X and Y are not literally identical.

functor(T,F,N)

The principal functor of term T has name F and arity N, where F is either an atom or, provided N is 0, an integer. Initially, either T must be instantiated to, respectively, either an atom and a non-negative integer or an integer and 0. If these conditions are not satisfied, an error message is given. In the case where T is initially not instantiated to a variable, the result of the call is to instantiate T to the most general term having the principal functor indicated.
arg(I,T,X)

Initially, I must be instantiated to a positive integer and T to a compound term. The result of the call is to unify X with the Ith argument of term T. (The arguments are numbered from 1 upwards.) If the initial conditions are not satisfied or I is out of range, the call merely fails.

X = .. Y

Y is a list whose head is the atom corresponding to the principal functor of X and whose tail is the argument list of that functor in X.  e.g. :

\texttt{product(0,N,N-1) =.. [product,0,N,N-1]}
\texttt{N-1 =.. [-,N,1]}
\texttt{product =.. [product]}

If X is instantiated to a variable, then Y must be instantiated to a list of determinate length whose head is atomic (i.e. an atom or integer).

name(X,L)

If X is an atom or integer then L is a list of the ASCII codes of the characters comprising the name of X.  e.g.:

\texttt{name(product,[112,114,111,100,117,99,116])}

i.e. name(product,"product")
name(1976,[49,57,55,54])

name(:-,[58,45])

name([],[],[])

If X is instantiated to a variable, L must be instantiated to a list of ASCII character codes. e.g.:

?-name(X,[58,45]),

X = :-

?-name(X,[:-:]),

X = :-

call(X)

If X is instantiated to a term which would be acceptable as body of a clause, the goal 'call(X)' is executed exactly as if that term appeared textually in place of 'call(X)'. In particular, any cut ('!') occurring in X is interpreted as if it occurred in the body of the clause containing 'call(X)', unless that clause is a compiled clause, in which case only the alternatives in the execution of X are cut. If X is not instantiated as described above, an error message is printed and 'call' fails.

X

(where X is a variable) Exactly the same as 'call(X)'.

202
assert(C)

The current instance of C is interpreted as a clause and is added to the current interpreted program (with new private variables replacing any uninstantiated variables). The position of the new clause within the procedure concerned is implementation-defined. C must be instantiated to a non-variable.

asserta(C)

Like 'assert(C)', except that the new clause becomes the first clause for the procedure concerned.

clause(P,Q)

P must be bound to a non-variable term, and the current interpreted program is searched for clauses whose head matches P. The head and body of those clauses are unified with P and Q respectively. If one of the clauses is a unit clause, Q will be unified with 'true'.

assertz(C)

Like 'assert(C)', except that the new clause becomes the last clause for the procedure concerned.

retract(C)

The first clause in the current interpreted program that
matches C is erased. C must be initially instantiated to a non-variable, and becomes unified with the value of the erased clause. The space occupied by the erased clause will be recovered when instances of the clause are no longer in use. On backtracking it will erase the next clause that matches C.

retractall(P)

All clauses in the current interpreted program whose head matches P are 'retract'ed. P must be bound to a non-variable term.

listing(A)

Lists in the current output stream all the interpreted clauses for predicates with name A, where A is bound to an atom.

listing

Lists in the current output stream all the clauses in the current interpreted program.

NOTE: If a clause contains any atom or functor whose name has to be written in quotes, the listing of that clause will be still readable, but syntactically incorrect. Otherwise, clauses listed to a file by 'listing(A)' or 'listing' can be consulted back.
numbervars(X,N,M)

Unifies each of the variables in term X with a special term, so that write(X) prints each of these variables as 'I', where the Is are consecutive integers from N to M-1. N must be instantiated to an integer.

ancestors(L)

Unifies L with a list of ancestor goals for the current clause. The list starts with the parent goal and ends with the most recent ancestor coming from a 'call' in a compiled clause. Not available for compiled code.

subgoal_of(S)

The goal 'subgoal_of(S) is equivalent to the sequence of goals:

ancestors(L), in(S,L)

where the predicate 'in' successively matches its first argument with each of the elements of its second argument. Not available for compiled code.
4.6 INTERNAL DATABASE

These predicates remain in the system purely for compatibility reasons, and will be removed at some future date.

record(X)

The current instance of X is 'recorded' in the internal database at some implementation-defined position in the sequence of terms which constitutes the internal database (with new private variables replacing any uninstantiated variables). X must be instantiated to a non-variable.

recorda(X)

Like 'record(X)', except that the new term is 'recorded' at the 'top' of the internal database.

recordz(X)

Like 'record(X)', except that the new term is 'recorded' at the 'bottom' of the internal database.

?(X)

The internal database is searched for previously 'recorded' terms which match the current instance of X (which must not be a variable). These terms are successively unified with
$X$ in the order in which they are recorded in the internal database.

`recorded(X,P)`

The database is searched for previously "recorded" terms that match the current instance of $X$ (which must not be a variable). These terms are successively unified with $X$ in the order in which they are recorded in the internal database. $P$ is unified with a "pointer" which identifies the "recorded" term matching $X$. (A "pointer" is a term whose internal structure is implementation-defined).

`instance(P,X)`

$X$ is unified with the database term identified by "pointer" $P$.

`erase(P)`

The database term identified by "pointer" $P$ is erased from the internal database. The space occupied by the erased term will be recovered when instances of the term are no longer in use.

`eraseall(X)`

All the database terms matching the current instance of $X$ are "erased", in the sense of 'erase(-)'.
4.7 ENVIRONMENTAL

'NOLC'

Establishes the 'no lower-case' convention.

'LC'

Establishes the 'full character set' convention. It is the default setting.

trace

Enable trace.

notrace

Disable trace. It is the default setting.

leash

Enable 'leashed' mode for tracing. It is the default setting.

unleash

Disable 'leashed' mode for tracing.
OP(PRIORITY, TYPE, NAME)

Treat name as an operator of the stated type and priority. name may also be a list of names in which case all are to be treated as operators of the stated type and priority.

break

Causes the current execution to be interrupted at the next interpreted procedure call. Then the message ' % break: ' is displayed. The interpreter is then ready to accept input as though it was at top level. To close the break and resume the execution which was suspended, the command ':end. ' or Z must be typed. Execution will be resumed at the procedure call where it had been suspended. Alternatively, the suspended execution can be aborted by giving the command ':abort. '.

save(F)

The system saves the current state of the system into file F.

restore(F)

The supervisor is returned to the system state previously saved to file F.
maxdepth(D)

Positive integer D specifies the maximum depth, i.e., invocation level, beyond which the system will induce an automatic failure. Top level has zero depth. This is useful for guarding against loops in an untested program, or for curtailing infinite execution branches.

depth(D)

Integer D will give indication of current level of invocation.

scguide(N)

N must be instantiated to an integer from 0 to 512, indicating the desirable threshold of global stack pages below which garbage collection should be avoided if possible. The default is N=6.

sc

Enables garbage collection of the global stack (the default).

nosc

Disables garbage collection of the global stack.

trimcore

Reduces free space on the stacks and trail as much as
possible and, in virtual memory Monitors only, releases core no longer needed, thereby reducing the size of the low segment. The interpreter automatically calls 'trimcore' after each directive at top-level, after an 'abort' and after a (re)consult.

statistics

Display on the terminal statistics relating to core usage, run time, garbage collection of the global stack and stack shifts.

statistics(K,V)

This allows a program to gather various execution statistics. For each of the possible keys K, V is unified with a list of values, as follows:

<table>
<thead>
<tr>
<th>Key</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>core</td>
<td>low_segment</td>
</tr>
<tr>
<td></td>
<td>high_segment</td>
</tr>
<tr>
<td>hear</td>
<td>size</td>
</tr>
<tr>
<td></td>
<td>free</td>
</tr>
<tr>
<td>global_stack</td>
<td>size</td>
</tr>
<tr>
<td></td>
<td>free</td>
</tr>
<tr>
<td>local_stack</td>
<td>size</td>
</tr>
<tr>
<td></td>
<td>free</td>
</tr>
<tr>
<td>trail</td>
<td>size</td>
</tr>
<tr>
<td></td>
<td>free</td>
</tr>
<tr>
<td>runtime</td>
<td>since start</td>
</tr>
<tr>
<td></td>
<td>of PROLOG</td>
</tr>
<tr>
<td></td>
<td>since previous</td>
</tr>
<tr>
<td></td>
<td>'statistics'</td>
</tr>
<tr>
<td>garbage_collection</td>
<td>no. of GCs</td>
</tr>
<tr>
<td></td>
<td>words freed</td>
</tr>
<tr>
<td></td>
<td>time spent</td>
</tr>
<tr>
<td>stack_shifts</td>
<td>no. of local</td>
</tr>
<tr>
<td></td>
<td>shifts</td>
</tr>
<tr>
<td></td>
<td>no. of trail</td>
</tr>
<tr>
<td></td>
<td>shifts</td>
</tr>
<tr>
<td></td>
<td>time spent</td>
</tr>
</tbody>
</table>
Times are in miliseconds, sizes of areas in words. If a time exceeds 129.071 sec., it will be returned as a term:

\[ xwd(T1, T2) \]

representing:

\[ T1 \times 2^{18} + T2 \mod 2^{18} \]

Note that such a term occurs in an interpreted arithmetic expression, it will be evaluated correctly.
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<table>
<thead>
<tr>
<th>Page</th>
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<th>Where is</th>
<th>Must be</th>
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<tbody>
<tr>
<td>18</td>
<td>8</td>
<td>tail [H1:T1]</td>
<td>tail LT1</td>
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<td></td>
<td>27,28</td>
<td>:-sort ([c,q,w,e,r,t,y,u,i,o,p,a,s,d,f,g,h,j,k,l,z,x,c,v,b,n,m],S), write (S).</td>
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<td>compact (L1, linked (X,Y), :-cat (X,-,Y,-)), linked (X,Z), :-cat (X,-,Y,-), linked (Y,Z).</td>
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<td>below preserved (_,true). retrace 1 (true,V,C,true).</td>
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