

# Constructing and Mapping Fuzzy Thematic Clusters to Higher Ranks in a Taxonomy

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**Abstract.** We present a novel methodology for mapping a system such as a research department to a related taxonomy in a thematically consistent way. The components of the structure are supplied with fuzzy membership profiles over the taxonomy. Our method generalizes the profiles in two steps: first, by fuzzy clustering, and then by mapping the clusters to higher ranks of the taxonomy. To be specific, we concentrate on the Computer Sciences area represented by the taxonomy of ACM Computing Classification System (ACM-CCS). We build fuzzy clusters of the taxonomy leaves according to the similarity between individual profiles by using a novel, additive spectral, fuzzy clustering method that, in contrast to other methods, involves a number of model-based stopping conditions. The clusters are not necessarily consistent with the taxonomy. This is formalized by a novel method for parsimoniously elevating them to higher ranks of the taxonomy using an original recursive algorithm for minimizing a penalty function that involves “head subjects” on the higher ranks of the taxonomy along with their “gaps” and “offshoots”. An example is given illustrating the method applied to real-world data.

## 1 Introduction

The last decade has witnessed an unprecedented rise of the concept of ontology as a computationally feasible tool for knowledge maintenance. For example, the usage of Gene Ontology [6] for interpretation and annotation of various gene sets and gene expression data is becoming a matter of routine in bioinformatics (see, for example, [14] and references therein).

The goal of this paper is to develop a framework for representation of the activities of an organization or any other system under consideration, in terms of a taxonomy. We first build profiles for its constituent entities in terms of the taxonomy and then thematically generalize them to higher ranks of the taxonomy.

To represent a functioning structure over a taxonomy is to indicate those topics in the taxonomy that most fully express the structure’s working in its relation to the taxonomy. To make the representation thematically consistent and parsimonious, we have developed a two-phase generalization approach. The first phase generalizes over the structure by building clusters of taxonomy topics according to the functioning of the system. The second phase takes the clusters as query sets in the taxonomy and parsimoniously maps them to higher ranks of the taxonomy. Both entity profiles and thematic

clusters derived at the first phase are fuzzy in order to better reflect the real world objects, so that the elevating method applies to fuzzy clusters. It should be pointed out that both building fuzzy profiles and finding fuzzy clusters are research activities well documented in the literature; yet the issues involved in this project led us to develop original schemes of our own including an efficient method for fuzzy clustering combining the approaches of spectral and approximation clustering [12].

We apply these constructions in two areas: (i) to visualize activities of Computer Science research organizations; and (ii) to discern the complexes of mathematical ideas according to classes taught in regular teaching courses in a university department. We take the popular ACM Computing Classification System (ACM-CCS), a conceptual four-level classification of the Computer Science subject area as a pre-specified taxonomy for (i), and the three-layer Mathematics Subject Classification MSC2010 developed by the Mathematical Reviews and Zentralblatt Mathematics editors (see <http://www.ams.org/mathscinet/msc/msc2010.html>), for (ii). In what follows the focus is mainly on the application (i) to research organizations. The paper is organized according to the structure of our approach: Section 2 describes an e-system we developed for getting ACM-CCS leaves fuzzy membership profiles from Computer Science researchers, Section 3 describes our method for deriving fuzzy clusters from the profiles, and Section 4 presents our parsimonious elevation method to generalize to higher ranks in a taxonomy tree.

## 2 Taxonomy-based profiles

### 2.1 Representing over the ACM-CCS taxonomy

In the case of investigation of activities of a university department or center, a research team's profile can be defined as a fuzzy membership function on the set of leaf-nodes of the taxonomy under consideration so that the memberships reflect the extent of the team's effort put into corresponding research topics.

In this case, the ACM Computing Classification System (ACM-CCS) [1] is used as the taxonomy. ACM-CCS comprises eleven major partitions (first-level subjects) such as *B. Hardware*, *D. Software*, *E. Data*, *G. Mathematics of Computing*, *H. Information Systems*, etc. These are subdivided into 81 second-level subjects. For example, item *I. Computing Methodologies* consists of eight subjects including *I.1 SYMBOLIC AND ALGEBRAIC MANIPULATION*, *I.2 ARTIFICIAL INTELLIGENCE*, *I.5 PATTERN RECOGNITION*, etc. They are further subdivided into third-layer topics as, for instance, *I.5 PATTERN RECOGNITION* which is represented by seven topics including *I.5.3 Clustering*, *I.5.4 Applications*, etc.

Taxonomy structures such as the ACM-CCS are used, mainly, as devices for annotation and search for documents or publications in collections such as that on the ACM portal [1]. The ACM-CCS tree has been applied also as: a gold standard for ontologies derived by web mining systems such as the CORDER engine [17]; a device for determining the semantic similarity in information retrieval [9] and e-learning applications [18, 5]; and a device for matching software practitioners' needs and software researchers' activities [4].

Here we concentrate on a different application of ACM-CCS – a generalized representation of a Computer Science research organization that can be used for over-viewing scientific subjects that are being developed in the organization, assessing the scientific issues in which the character of activities in organizations does not fit well onto the classification – these can potentially be the growth points, and help with planning the restructuring of research and investment.

## 2.2 E-Screen survey tool

Fuzzy profiles are derived from either automatic analysis of documents posted on the web by the teams or by explicitly surveying the members of the department. The latter option is especially convenient in situations in which the web contents do not properly reflect the developments, for example, in non-English speaking countries with relatively underdeveloped internet infrastructures for the maintenance of research results. We developed an interactive survey tool that provides two types of functionality: i) collection of data about ACM-CCS based research profiles of individual members; ii) statistical analysis and visualization of the data and results of the survey on the level of a department. The respondent is asked to select up to six topics among the leaf nodes of the ACM-CCS tree and assign each with a percentage expressing the proportion of the topic in the total of the respondent’s research activity for, say, the past four years. Figure 1 shows a screenshot of the baseline interface for a respondent who has chosen six ACM-CCS topics during her survey session.

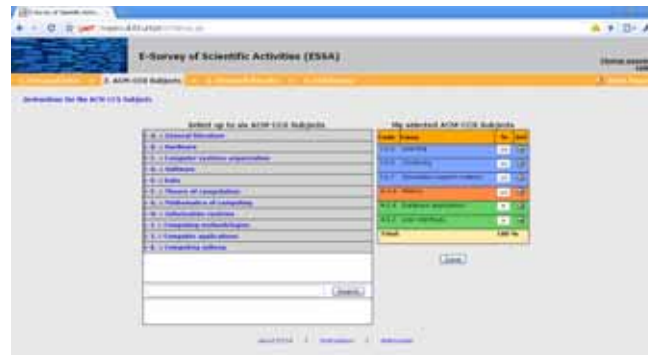


Fig. 1: Screenshot of the interface survey tool for selection of ACM-CCS topics.

The set of profiles supplied by respondents forms an  $N \times M$  matrix  $F$  where  $N$  is the number of ACM-CCS topics involved in the profiles and  $M$  the number of respondents. Each column of  $F$  is a fuzzy membership function, rather sharply delineated because only six topics may have positive memberships in each of the columns.

### 3 Representing research organization by fuzzy clusters of ACM-CCS topics

#### 3.1 Deriving similarity between ACM-CCS research topics

We represent a research organization by clusters of ACM-CCS topics to reflect thematic communalities between activities of members or teams working on these topics. The clusters are found by analyzing similarities between topics according to their appearances in the profiles. The more profiles contain a pair of topics  $i$  and  $j$  and the greater the memberships of these topics, the greater is the similarity score for the pair.

Consider a set of  $V$  individuals ( $v = 1, 2, \dots, V$ ), engaged in research over some topics  $t \in T$  where  $T$  is a pre-specified set of scientific subjects. The level of research effort by individual  $v$  in developing topic  $t$  is evaluated by the membership  $f_{tv}$  in profile  $f_v$  ( $v = 1, 2, \dots, V$ ).

Then the similarity  $w_{tt'}$  between topics  $t$  and  $t'$  is defined as

$$w_{tt'} = \sum_{v=1}^V \frac{n_v}{n_{max}} f_{tv} f_{t'v}, \quad (1)$$

where the ratios are introduced to balance the scores of individuals bearing different numbers of topics.

To make the cluster structure in the similarity matrix sharper, we apply the spectral clustering approach to pre-process the similarity matrix  $W$  using the so-called Laplacian transformation [8]. First, an  $N \times N$  diagonal matrix  $D$  is defined, with  $(t, t)$  entry equal to  $d_t = \sum_{t' \in T} w_{tt'}$ , the sum of  $t$ 's row of  $W$ . Then unnormalized Laplacian and normalized Laplacian are defined by equations  $L = D - W$  and  $L_n = D^{-1/2} L D^{-1/2}$ , respectively. Both matrices are semipositive definite and have zero as the minimum eigenvalue. The minimum non-zero eigenvalues and corresponding eigenvectors of the Laplacian matrices are utilized then as relaxations of combinatorial partition problems [16, 8]. Of comparative properties of these two normalizations, the normalized Laplacian, in general, is considered superior [8]. Since the additive clustering approach described in the next section relies on maximum rather than minimum eigenvalues, we use the Laplacian pseudoinverse transformation, Lapin for short, defined by

$$L_n^-(W) = \tilde{Z} \tilde{\Lambda}^{-1} \tilde{Z}'$$

where  $\tilde{\Lambda}$  and  $\tilde{Z}$  are defined by the spectral decomposition  $L_n = Z \Lambda Z'$  of matrix  $L_n = D^{-1/2} (D - W) D^{-1/2}$ . To specify these matrices, first, set  $T'$  of indices of elements corresponding to non-zero elements of  $\Lambda$  is determined, after which the matrices are taken as  $\tilde{\Lambda} = \Lambda(T', T')$  and  $\tilde{Z} = Z(:, T')$ . The choice of the Lapin transformation can be explained by the fact that it leaves the eigenvectors of  $L_n$  unchanged while inverting the non-zero eigenvalues  $\lambda \neq 0$  to those  $1/\lambda$  of  $L_n^-$ . Then the maximum eigenvalue of  $L_n^-$  is the inverse of the minimum non-zero eigenvalue  $\lambda_1$  of  $L_n$ , corresponding to the same eigenvector.

### 3.2 Additive-spectral fuzzy clustering

In spite of the fact that many fuzzy clustering algorithms have been developed already [2], [7], most of them are ad hoc and, moreover, they all involve manually specified parameters such as the number of clusters or threshold of similarity without providing any guidance for choosing the. We apply a model-based approach of additive clustering, combined with the spectral clustering approach, to develop a novel fuzzy clustering method that is both practical and supplied with model-based parameters helping to choose the right number of clusters.

Thematic similarities  $a_{tt'}$  between topics are but manifested expressions of some hidden patterns within the organization which can be represented by fuzzy clusters in exactly the same manner as the manifested scores in the definition of the similarity  $w_{tt'}$  (1). We propose to formalize a thematic fuzzy cluster as represented by two items: (i) a membership vector  $u = (u_t)$ ,  $t \in T$ , such that  $0 \leq u_t \leq 1$  for all  $t \in T$ , and (ii) an intensity  $\mu > 0$  that expresses the extent of significance of the pattern corresponding to the cluster, within the organization under consideration. With the introduction of the intensity, applied as a scaling factor to  $u$ , it is the product  $\mu u$  that is a solution rather than its individual co-factors. Given a value of the product  $\mu u_t$ , it is impossible to tell which part of it is  $\mu$  and which  $u_t$ . To resolve this, we follow a conventional scheme: let us constrain the scale of the membership vector  $u$  on a constant level, for example, by a condition such as  $\sum_t u_t = 1$  or  $\sum_t u_t^2 = 1$ , then the remaining factor will define the value of  $\mu$ . The latter normalization better suits the criterion implied by our fuzzy clustering method and, thus, is accepted further on.

Our additive fuzzy clustering model follows that of [15, 10, 13] and involves  $K$  fuzzy clusters that reproduce the pseudo-inverted Laplacian similarities  $a_{tt'}$  up to additive errors according to the following equations:

$$a_{tt'} = \sum_{k=1}^K \mu_k^2 u_{kt} u_{kt'} + e_{tt'}, \quad (2)$$

where  $u_k = (u_{kt})$  is the membership vector of cluster  $k$ , and  $\mu_k$  its intensity.

The item  $\mu_k^2 u_{kt} u_{kt'}$  expresses the contribution of cluster  $k$  to the similarity  $a_{tt'}$  between topics  $t$  and  $t'$ , which depends on both the cluster's intensity and the membership values. The value  $\mu^2$  summarizes the contribution of intensity and will be referred to as the cluster's weight.

To fit the model in (2), we apply the least-squares approach, thus minimizing the sum of all  $e_{tt'}^2$ . Since  $A$  is definite semi-positive, its first  $K$  eigenvalues and corresponding eigenvectors form a solution to this if no constraints on vectors  $u_k$  are imposed. Additionally, we apply the one-by-one principal component analysis strategy for finding one cluster at a time this makes the computation feasible and is crucial for determining the number of clusters. Specifically, at each step, we consider the problem of minimization of a reduced to one fuzzy cluster least-squares criterion

$$E = \sum_{t,t' \in T} (b_{tt'} - \xi u_t u_{t'})^2 \quad (3)$$

with respect to unknown positive  $\xi$  weight (so that the intensity  $\mu$  is the square root of  $\xi$ ) and fuzzy membership vector  $u = (u_t)$ , given similarity matrix  $B = (b_{tt'})$ .

At the first step,  $B$  is taken to be equal to  $A$ . Each found cluster changes  $B$  by subtracting the contribution of the found cluster (which is additive according to model (2)), so that the residual similarity matrix for obtaining the next cluster will be  $B - \mu^2 uu^T$  where  $\mu$  and  $u$  are the intensity and membership vector of the found cluster. In this way,  $A$  indeed is additively decomposed according to formula (2) and the number of clusters  $K$  can be determined in the process.

Let us specify an arbitrary membership vector  $u$  and find the value of  $\xi$  minimizing criterion (3) at this  $u$  by using the first-order condition of optimality:

$$\xi = \frac{\sum_{t,t' \in T} b_{tt'} u_t u_{t'}}{\sum_{t \in T} u_t^2 \sum_{t' \in T} u_{t'}^2},$$

so that the optimal  $\xi$  is

$$\xi = \frac{\mathbf{u}' B \mathbf{u}}{(\mathbf{u}' \mathbf{u})^2} \quad (4)$$

which is obviously non-negative if  $B$  is semi-positive definite.

By putting this  $\xi$  in equation (3), we arrive at

$$E = \sum_{t,t' \in T} b_{tt'}^2 - \xi^2 \sum_{t \in T} u_t^2 \sum_{t' \in T} u_{t'}^2 = S(B) - \xi^2 (\mathbf{u}' \mathbf{u})^2,$$

where  $S(B) = \sum_{t,t' \in T} b_{tt'}^2$  is the similarity data scatter.

Let us denote the last item by

$$G(u) = \xi^2 (\mathbf{u}' \mathbf{u})^2 = \left( \frac{\mathbf{u}' B \mathbf{u}}{\mathbf{u}' \mathbf{u}} \right)^2, \quad (5)$$

so that the similarity data scatter is the sum:

$$S(B) = G(u) + E \quad (6)$$

of two parts,  $G(u)$ , which is explained by cluster  $(\mu, u)$ , and  $E$ , which remains unexplained.

An optimal cluster, according to (6), is to maximize the explained part  $G(u)$  in (5) or its square root

$$g(u) = \xi \mathbf{u}' \mathbf{u} = \frac{\mathbf{u}' B \mathbf{u}}{\mathbf{u}' \mathbf{u}}, \quad (7)$$

which is the celebrated Rayleigh-Ritz quotient, whose maximum value is the maximum eigenvalue of matrix  $B$ , which is reached at its corresponding eigenvector, in the unconstrained problem.

This shows that the spectral clustering approach is appropriate for our problem. According to this approach, one should find the maximum eigenvalue  $\lambda$  and corresponding normed eigenvector  $z$  for  $B$ ,  $[\lambda, z] = \Lambda(B)$ , and take its projection to the set of admissible fuzzy membership vectors.

Our clustering approach involves a number of model-based criteria for halting the process of sequential extraction of fuzzy clusters:

1. The optimal value of  $\xi$  (4) for the spectral fuzzy cluster becomes negative.
2. The contribution of a single extracted cluster becomes too low, less than a pre-specified  $\tau > 0$  value.
3. The residual scatter  $E$  becomes smaller than a pre-specified  $\epsilon$  value, say less than 5% of the original similarity data scatter.

The described one-by-one fuzzy additive-spectral thematic cluster extraction algorithm is referred to as the FADDI-S. It combines three different approaches: additive clustering [15, 10, 13], spectral clustering [16, 8, 20], and relational fuzzy clustering [2, 3] and adds an edge to each. In the context of additive clustering, fuzzy approaches were considered only by [13], yet in a very restricted setting: (a) the clusters intensities are assumed constant there, (b) the number of clusters is pre-specified, and (c) the fitting method is very local and computationally intensive - these all restrictions are overcome in FADDI-S. The spectral clustering approach is overtly heuristic, whereas FADDI-S is model-based. The criteria used in relational fuzzy clustering are ad hoc whereas that of FADDI-S is model-based, and, moreover, its combined belongingness function values  $\mu_u$  are not constrained by the unity as is the case in relational clustering, but rather follow the scales of the relation under investigation, which is in line with the original approach by L. Zadeh [19]. We also carried out experiments to compare the effectiveness of FADDI-S with other popular methods. For example, in recent experiments, [3] compared several most popular relational fuzzy clustering approaches and showed that combining the popular fuzzy c-means approach with an initialization routine was superior to the others; yet FADDI-S outperformed that on the data generated according to the recipe from [3] (details and more experiments are described in [12]).

## 4 Parsimonious elevating Method

To generalize the contents of a thematic cluster, we propose a method for elevating it to higher ranks of the taxonomy so that if all or almost all children of a node in an upper layer belong to the cluster, then the node itself is taken to represent the cluster at this higher level of the ACM-CCS taxonomy (see Fig. 2). Depending on the extent of inconsistency between the cluster and the taxonomy, such elevation can be done differently, leading to different portrayals of the cluster on ACM-CCS tree depending on the relative weights of the events taken into account. A major event is the so-called “head subject”, a taxonomy node covering (some of) leaves belonging to the cluster, so that the cluster is represented by a set of head subjects. The penalty of the representation to be minimized is proportional to the number of head subjects so that the smaller that number the better. Yet the head subjects cannot be elevated too high in the tree because of the penalties for associated events, the cluster “gaps” and “offshoots” the number of them depends on the extent of inconsistency of the cluster versus the taxonomy.

The gaps are head subject’s children topics that are not included in the cluster. An offshoot is a taxonomy leaf node that is a head subject (not elevated). It is not difficult

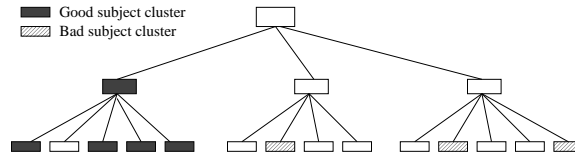


Fig. 2: Two clusters of second-layer topics, presented with checked and diagonal-lined boxes, respectively. The checked box cluster fits within one first-level category (with one gap only), whereas the diagonal line box cluster is dispersed among two categories on the right. The former fits the classification well; the latter does not.

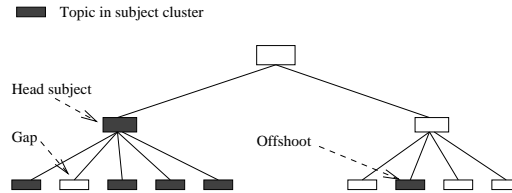


Fig. 3: Three types of features in mapping of a subject cluster to the taxonomy.

to see that the gaps and offshoots are determined by the head subjects specified in an elevation (see Fig. 3).

The total count of head subjects, gaps and offshoots, each weighted by both the penalties and leaf memberships, is used for scoring the extent of the cluster misfit needed for elevating a grouping of research topics over the classification tree. The smaller the score, the more parsimonious the elevation and the better the fit. Depending on the relative weighting of gaps, offshoots and multiple head subjects, different elevations can minimize the total misfit, as illustrated on Fig. 5 later.

Altogether, the set of topic clusters together with their optimal head subjects, offshoots and gaps constitute a parsimonious representation of the organization. Such a representation can be easily accessed and expressed. It can be further elaborated by highlighting those subjects in which members of the organization have been especially successful (i.e., publication in best journals or awards) or distinguished by a special feature (i.e., industrial use or inclusion in a teaching program). Multiple head subjects and offshoots, when they persist at subject clusters in different organizations, may show some tendencies in the development of the science, that the classification has not taken into account yet.

We have proved that a parsimonious lift of a subject cluster can be achieved by recursively building a parsimonious representation for each node of the ACM-CCS tree based on parsimonious representations for its children. In this, we assume that any head subject is automatically present at each of the nodes it covers, unless they are gaps (as presented on Fig. 3). Our algorithm is set as a recursive procedure over the tree starting at leaf nodes.



The procedure determines, at each node of the tree, sets of head gain and gap events to iteratively raise them to those of the parents, under each of two different assumptions that specify the situation at the parental node. One assumption is that the head subject has been inherited at the parental node from its own parent, and the second assumption is that it has not been inherited but gained in the node only. In the latter case the parental node is labeled as a head subject. Consider the parent-children system as shown in Fig. 4, with each node assigned with sets of gap and head gain events under the above two inheritance of head subject assumptions.

Let us denote the total penalty, to be minimized, under the inheritance and non-inheritance assumptions by  $p_i$  and  $p_n$ , respectively. An elevation result at a given node is defined by a pair of sets (H, G), representing the tree nodes at which events of head gains and gaps, respectively, have occurred in the subtree rooted at the node. We use  $(H_i, G_i)$  and  $(H_n, G_n)$  to denote elevation results under the inheritance and non-inheritance assumptions, respectively. The algorithm computes parsimonious representations for parental nodes according to the topology of the tree, proceeding from the leaves to the root in the manner which is similar to that described in [11] for a mathematical problem in bioinformatics.

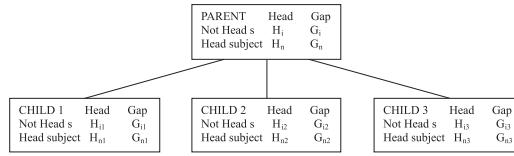


Fig. 4: Events in a parent-children system according to a parsimonious lift scenario.

For the sake of simplicity, we present only a version of the algorithm for crisp clusters obtained by a defuzzification step. Given a crisp topic cluster  $S$ , and penalties  $h$ ,  $o$  and  $g$  for being a head subject, offshoot and gap, respectively, the algorithm is initialized as follows.

At each leaf  $l$  of the tree, either  $H_n = \{l\}$ , if  $l \in S$ , or  $G_i = \{l\}$ , otherwise. The other three sets are empty. The penalties associated are  $p_i = 0$ ,  $p_n = o$  if  $H_n$  is not empty, that is, if  $l \in S$ , and  $p_i = g$ ,  $p_n = 0$ , otherwise. This is obviously a parsimonious arrangement at the leaf level.

The recursive step applies to any node  $t$  whose children  $v \in V$  have been assigned with the two couples of  $H$  and  $G$  sets already (see Figure 4 at which  $V$  consists of three children):  $(H_i(v), L_i(v))$ ;  $(H_n(v), L_n(v))$  along with associated penalties  $p_i(v)$  and  $p_n(v)$ .

(I) Deriving the pair  $H_i(t)$  and  $G_i(t)$ , under the inheritance assumption, the one of the following two cases is to be chosen depending on the cost:

(a) The head subject has been lost at  $t$ , so that  $H_i(t) = \cup_{v \in V} H_n(v)$  and  $G_i(t) = \cup_{v \in V} G_n(v) \cup \{t\}$ . (Note different indexes,  $i$  and  $n$  in the latter expression.) The penalty in this case is  $p_i = \sum_{v \in V} p_n(v) + g$ ;

or

(b) The head subject has not been lost at  $t$ , so that  $H_i(t) = \emptyset$  (under the assumption that no gain can happen after a loss) and  $G_i = \cup_{v \in V} G_i(v)$  with  $p_i = \sum_{v \in V} p_i(v)$ .

The case that corresponds to the minimum of the two  $p_i$  values is returned then.

(II) Deriving the pair  $H_n(t)$  and  $G_n(t)$ , under the non-inheritance assumption, the one of the following two cases is to be chosen that minimizes the penalty  $p_n$ :

(a) The head subject has been gained at  $t$ , so that  $H_n(t) = \cup_{v \in V} H_i(v) \cup \{t\}$  and  $G_n(t) = \cup_{v \in V} G_i(s)$  with  $p_n = \sum_{v \in V} p_i(v) + h$ ;

or (b) The head subject has not been gained at  $t$ , so that  $H_n(t) = \cup_{v \in V} H_n(v)$  and  $G_n = \cup_{v \in V} G_n(v)$  with  $p_n = \sum_{v \in V} p_n(v)$ .

After all tree nodes  $t$  have been assigned with the two pairs of sets, accept the  $H_n$ ,  $L_n$  and  $p_n$  at the root. This gives a full account of the events in the tree.

This algorithm leads indeed to an optimal representation; its extension to a fuzzy cluster is achieved through using the cluster memberships in computing the penalty values at tree nodes.

## 5 An application to a real world case

Let us illustrate the approach by using the data from a survey conducted at the Centre of Artificial Intelligence, Faculty of Science & Technology, New University of Lisboa (CENTRIA-UNL). The survey involved 16 members of the academic staff of the Centre who covered 46 topics of the third layer of the ACM-CCS.

With the algorithm FADDI-S applied to the  $46 \times 46$  similarity matrix, two clusters have been sequentially extracted, after which the residual matrix has become definite negative (stopping condition (a)). Cluster 1 is of pattern recognition and its applications to physical sciences and engineering including images and languages, with offshoots to general aspects of information systems. In cluster 2, all major aspects of computational mathematics are covered, with an emphasis on reliability and testing, and with applications in the areas of life sciences. Overall these results are consistent with the informal assessment of the research conducted in the research organization. Moreover, the sets of research topics chosen by individual members at the ESSA survey follow the cluster structure rather closely, falling mostly within one of the two.

Figure 5 shows the representation of CENTRIA's cluster 2 in the ACM-CCS taxonomy with penalties of  $h = 1$ ,  $o = 0.8$ , and  $g = 0.1$ .

## 6 Conclusion

We have proposed a novel method for knowledge generalization that employs a taxonomy tree. The method constructs fuzzy membership profiles of the entities constituting the structure under consideration in terms of the taxonomys leaves, and then it generalizes them in two steps. These steps are:

(i) fuzzy clustering research topics according to their thematic similarities, ignoring the topology of the taxonomy, and

(ii) elevating clusters mapped to the taxonomy to higher ranked categories in the tree.

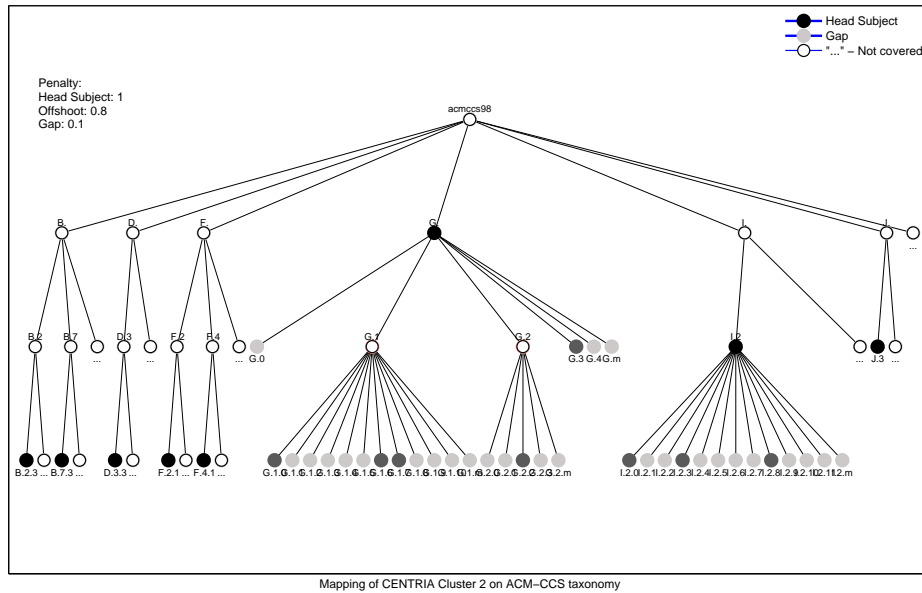


Fig. 5: Mapping of CENTRIA cluster 2 onto the ACM-CCS tree with penalties  $h = 1$ ,  $o = 0.8$  and  $g = 0.1$ : two head subjects along with 10 and 16 gaps, respectively.

These generalization steps thus cover both sides of the representation process: the empirical – related to the structure under consideration – and the conceptual – related to the taxonomy hierarchy.

Potentially, this approach could lead to a useful instrument for comprehensive visual representation of developments in any field of organized human activities.

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